

Runtime Safety Filtering for Learned Small UAS Separation Policies under GNSS Degradation

Action filtering vs observation filtering

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Department of Mechanical and Aerospace Engineering
George Washington University, Washington, DC, USA.

01 MOTIVATION

A learned separation policy can resolve conflicts

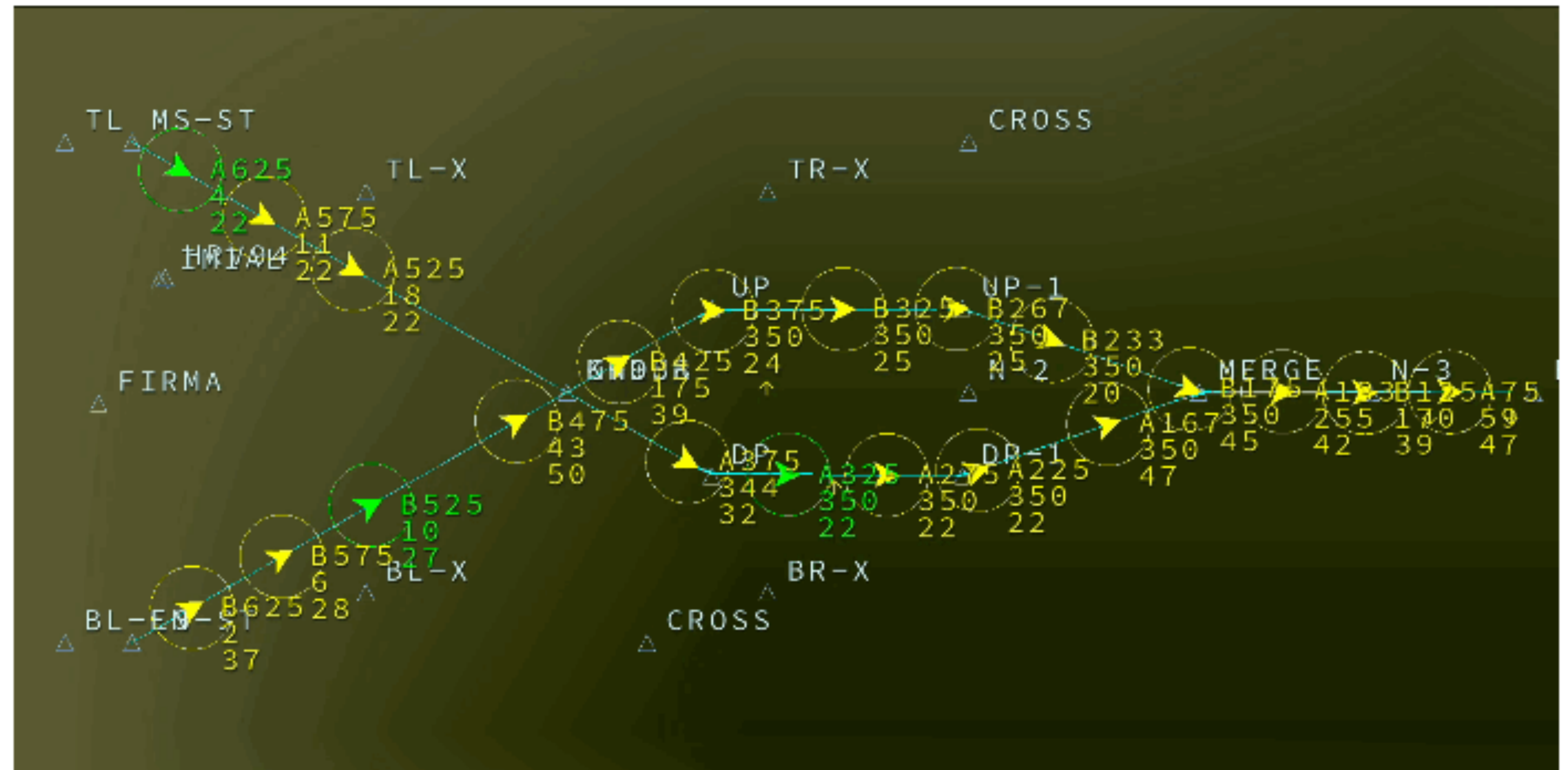
SIMULATION · NO GNSS DEGRADATION (NOMINAL GNSS)

With nominal GNSS, the policy produces a **separation-preserving action**.

The policy uses nearby aircraft information to adjust ownship speed in real time.

100 m separation standard
10 km routes

Next: What information does the policy receive, and how can GNSS degradation corrupt it?



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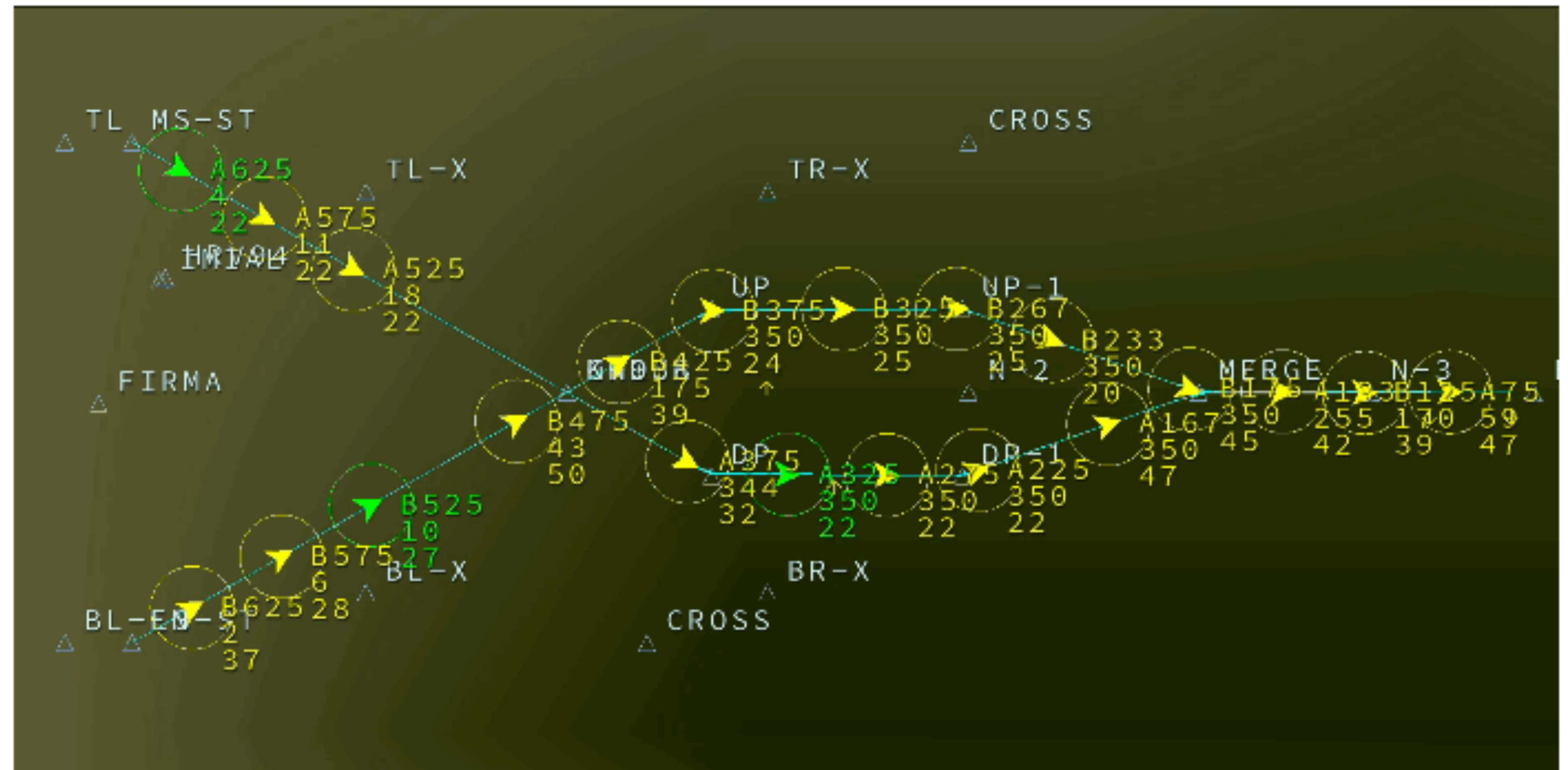
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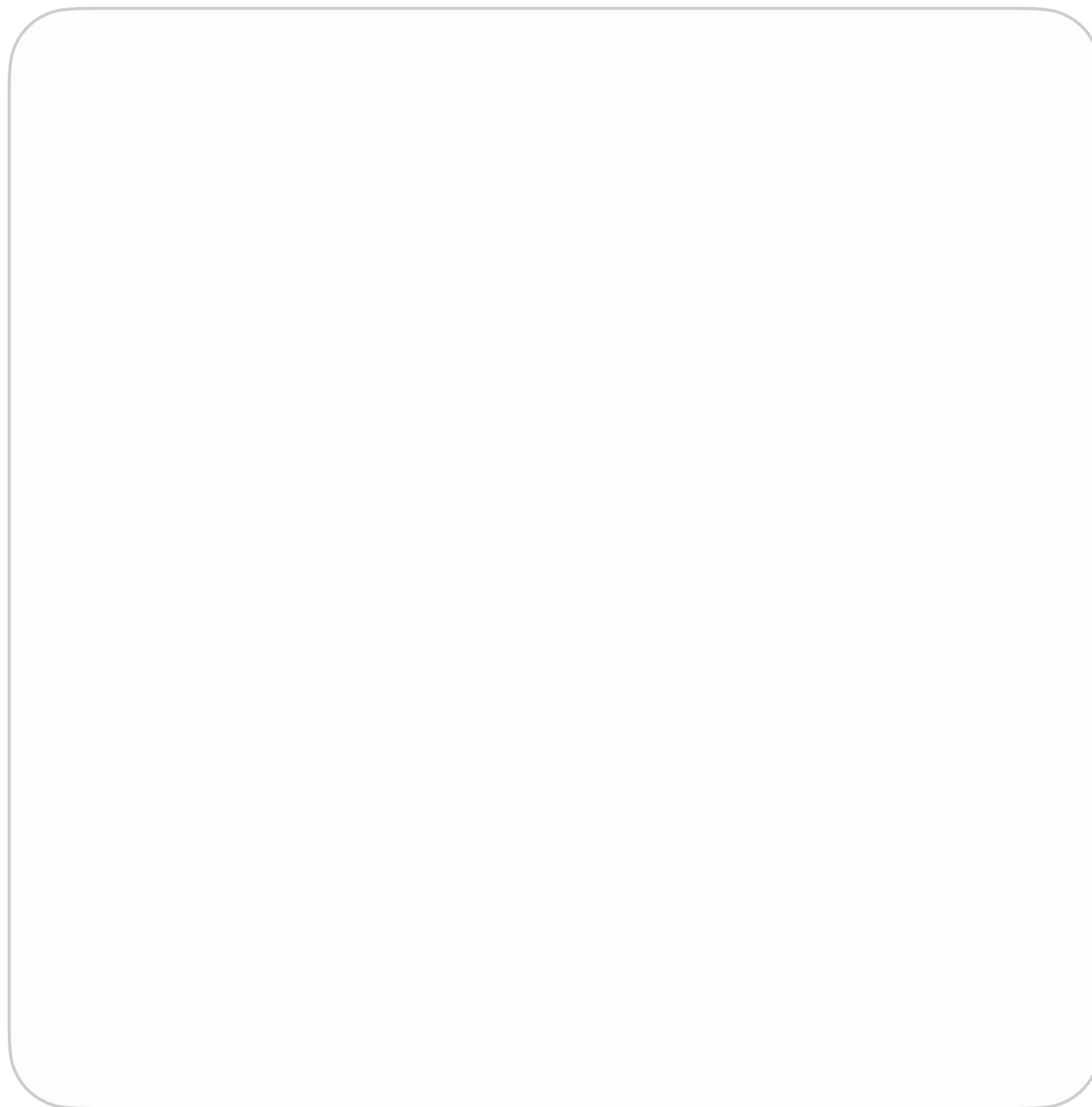
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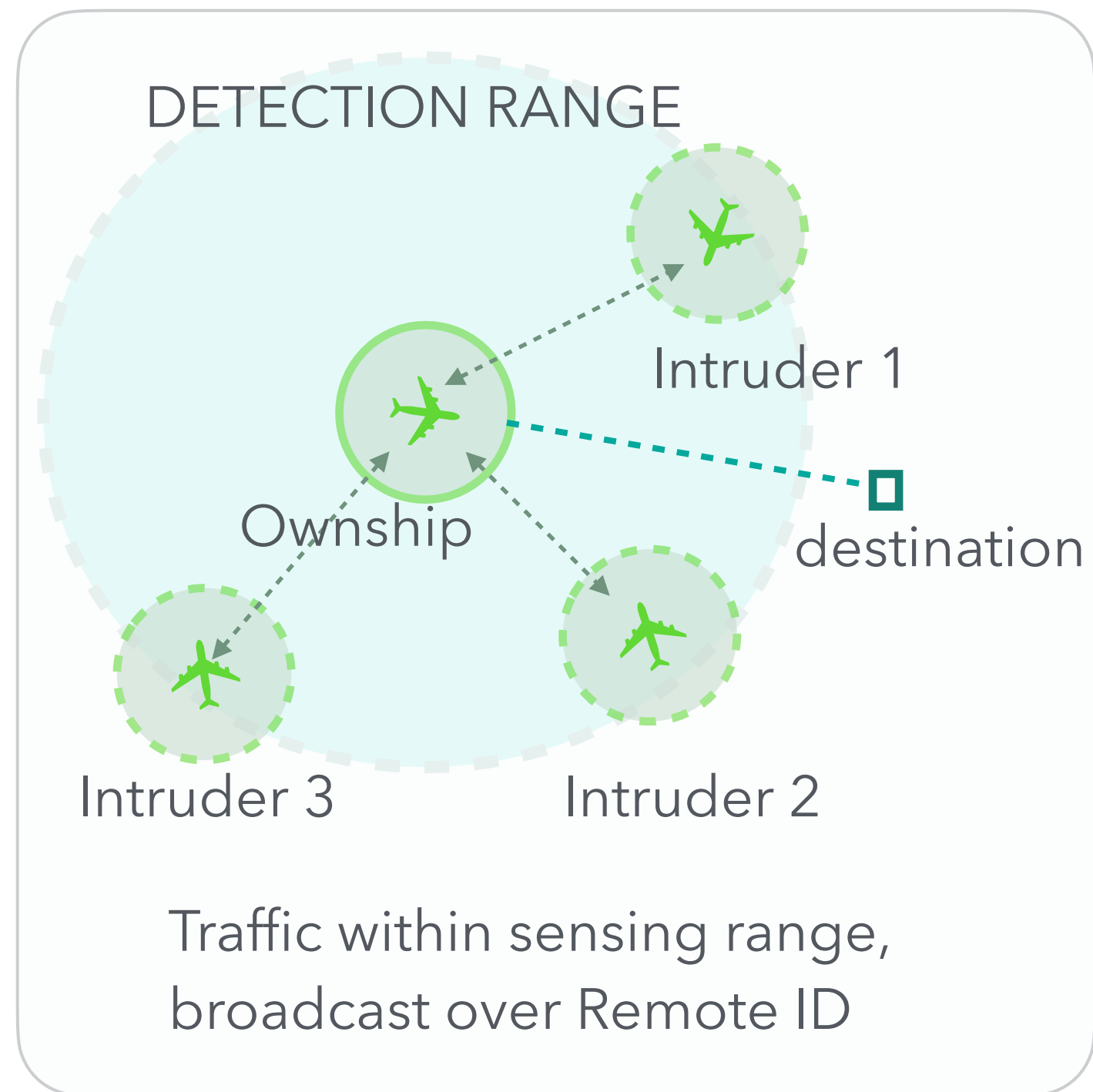
How a decentralized learned separation policy works

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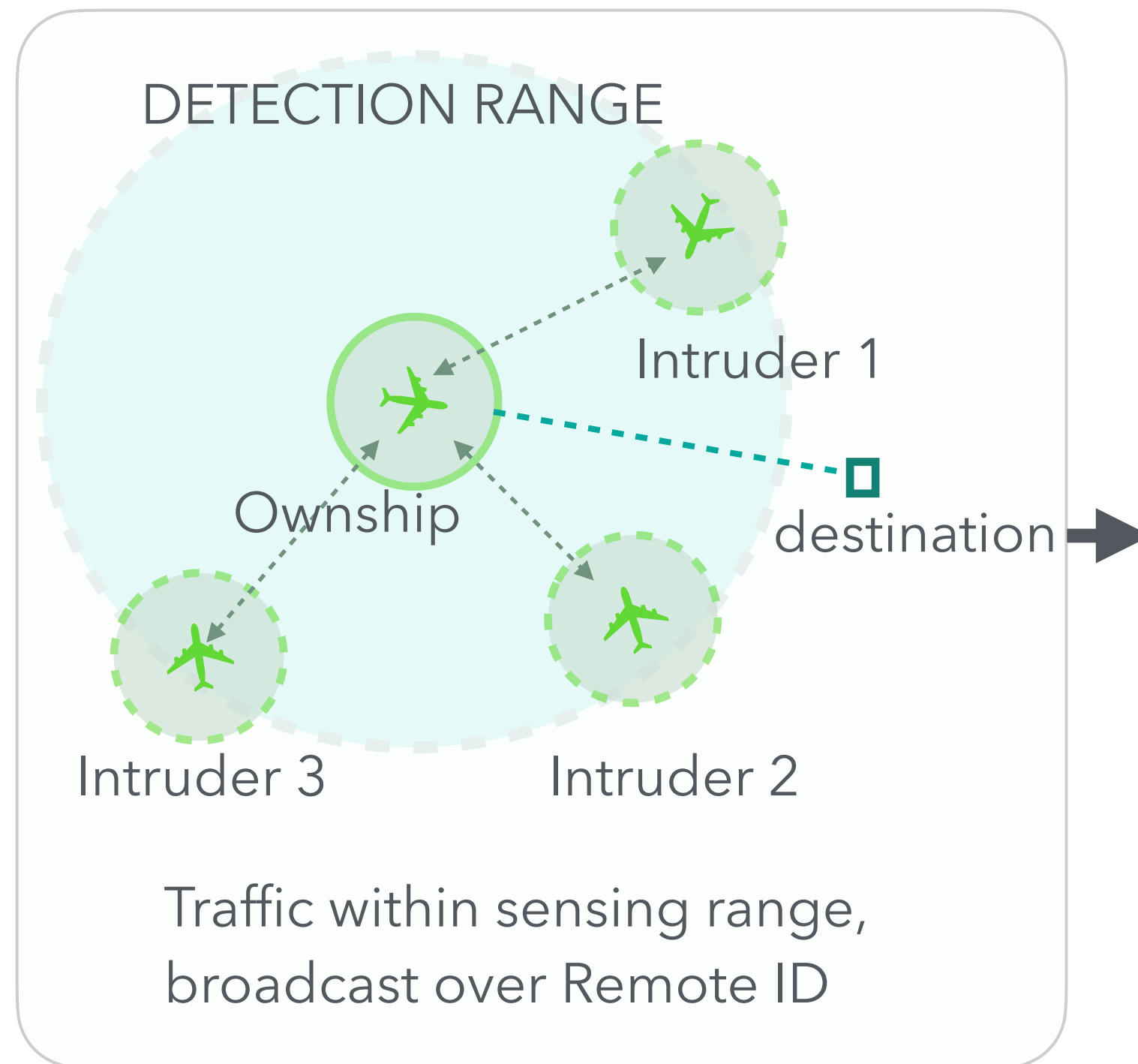
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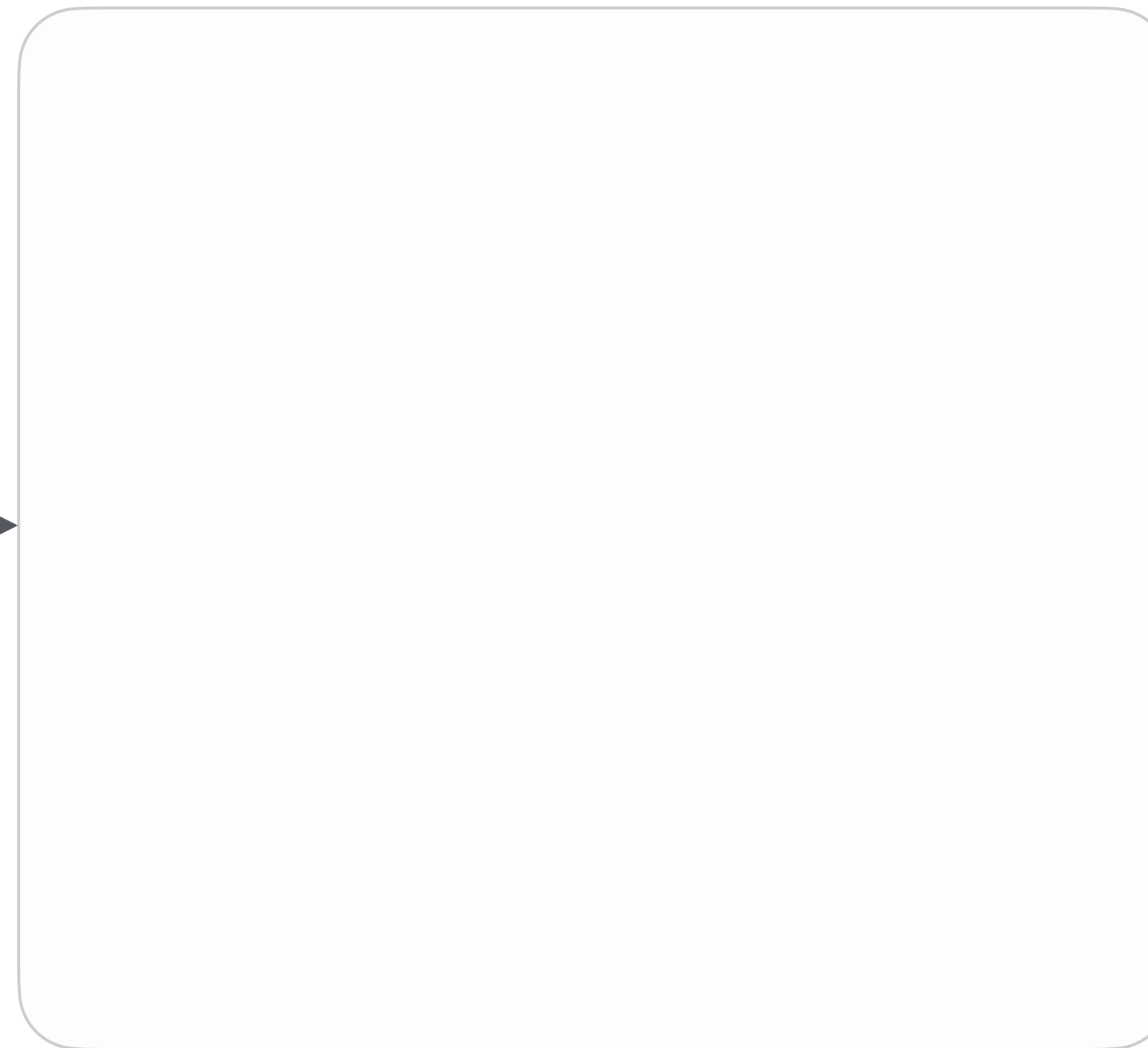


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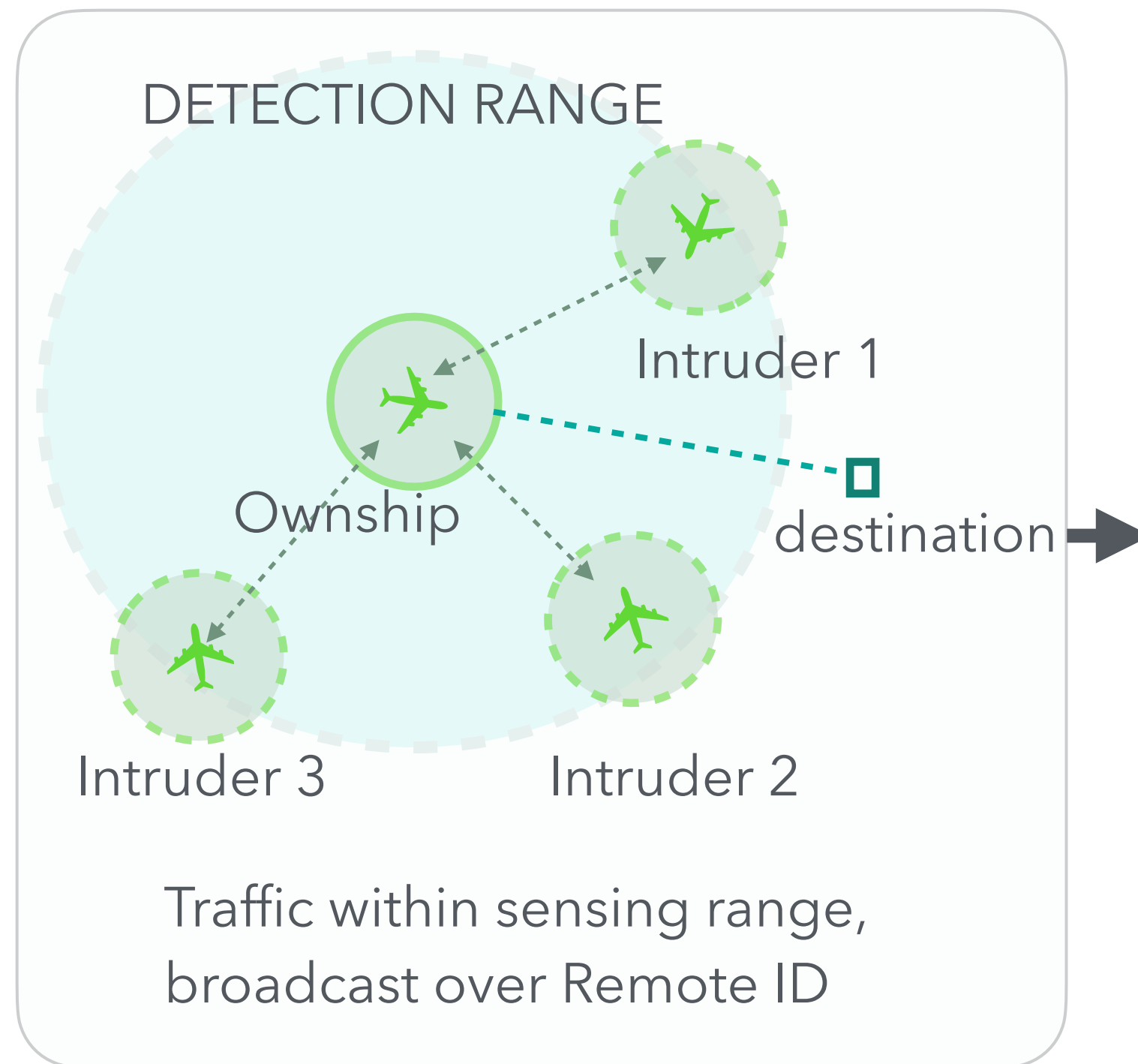


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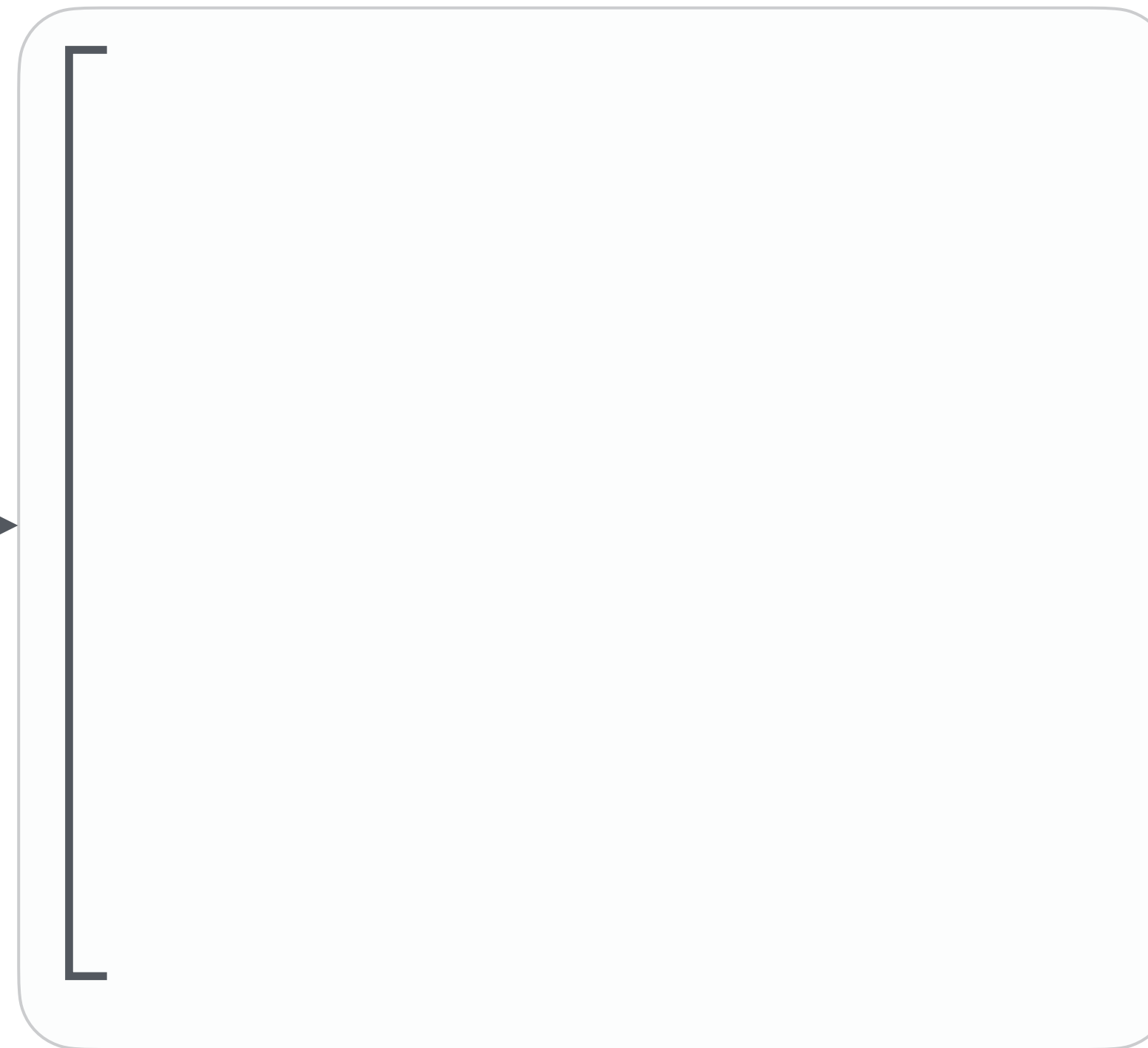


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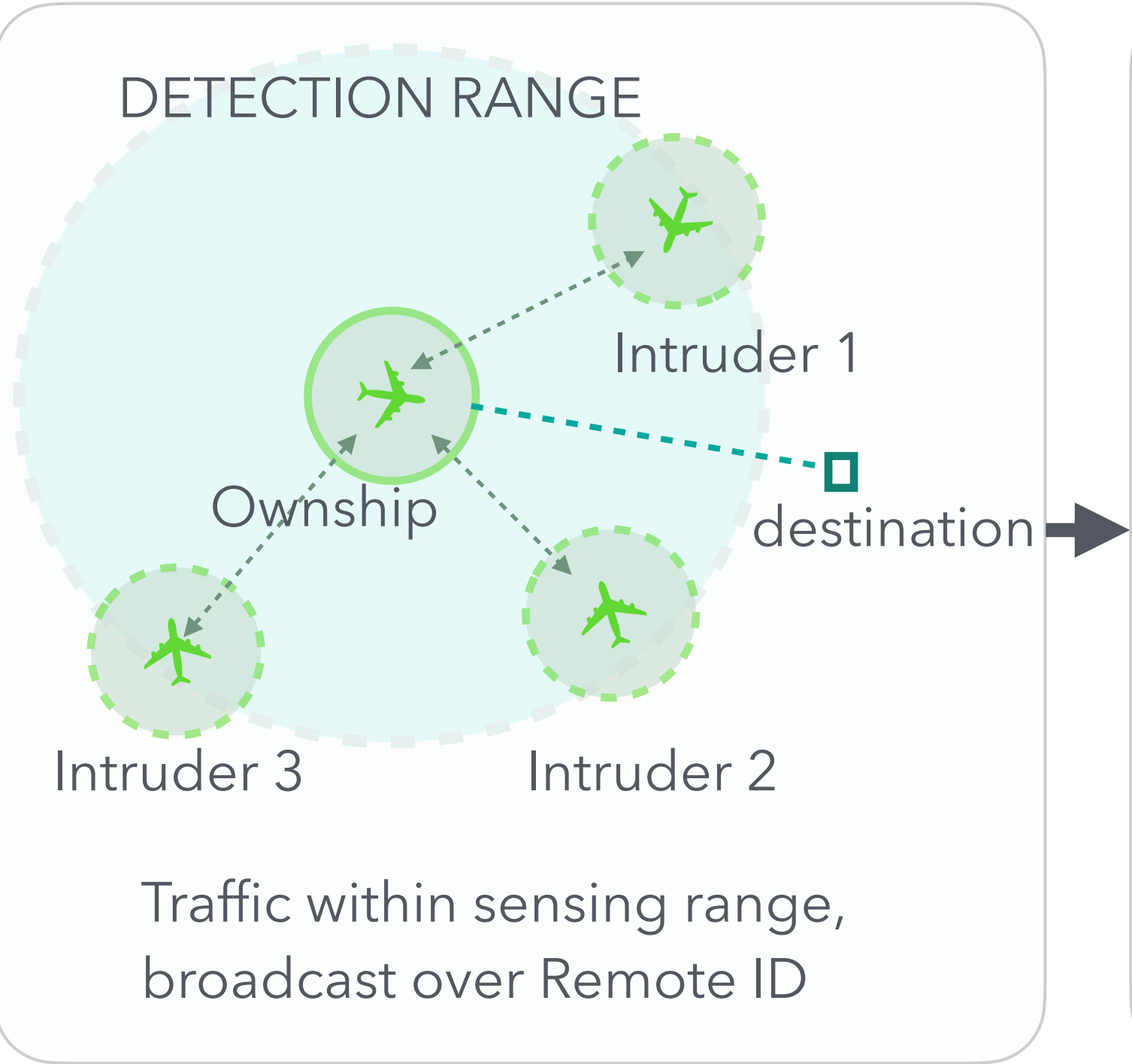


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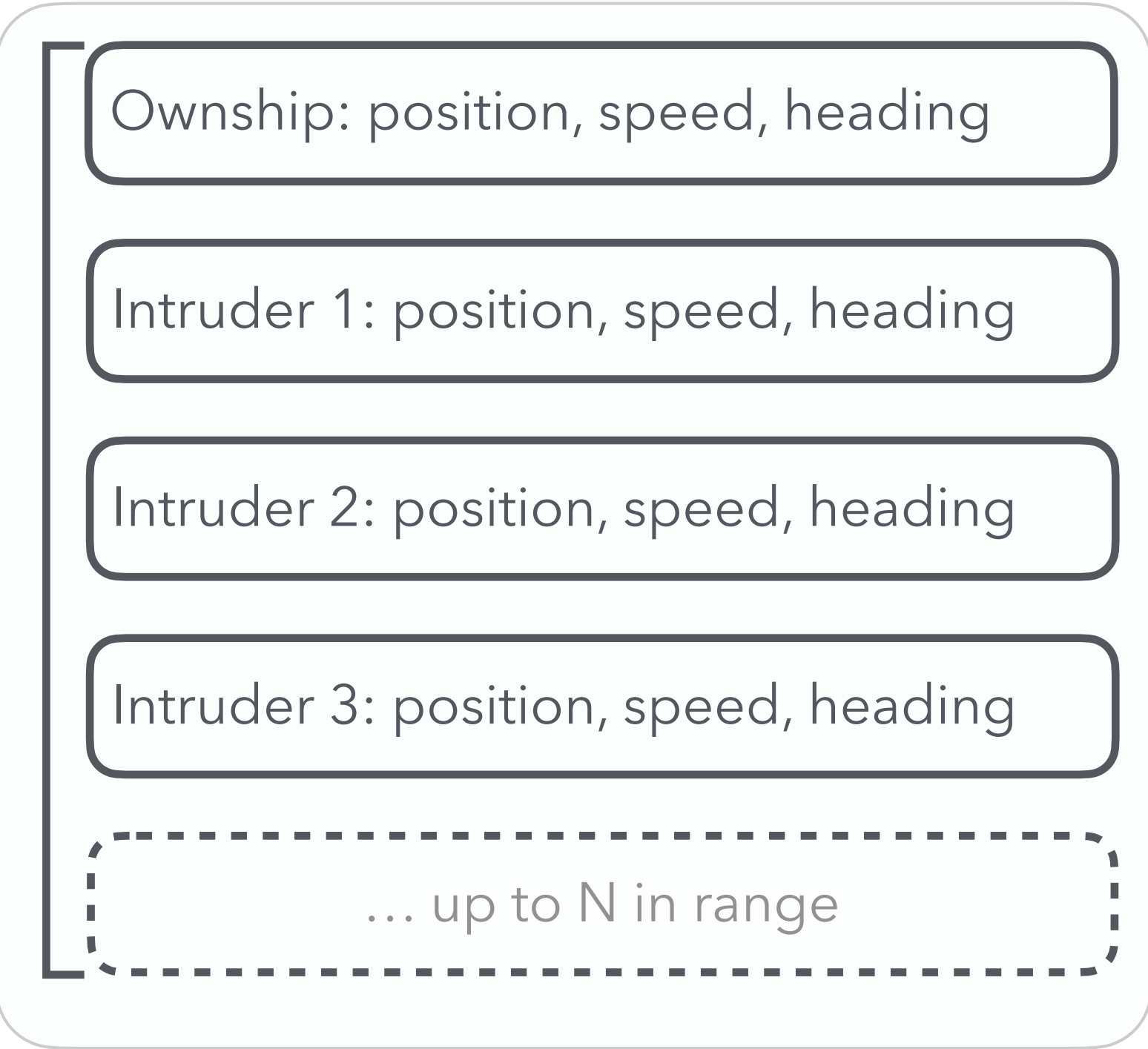


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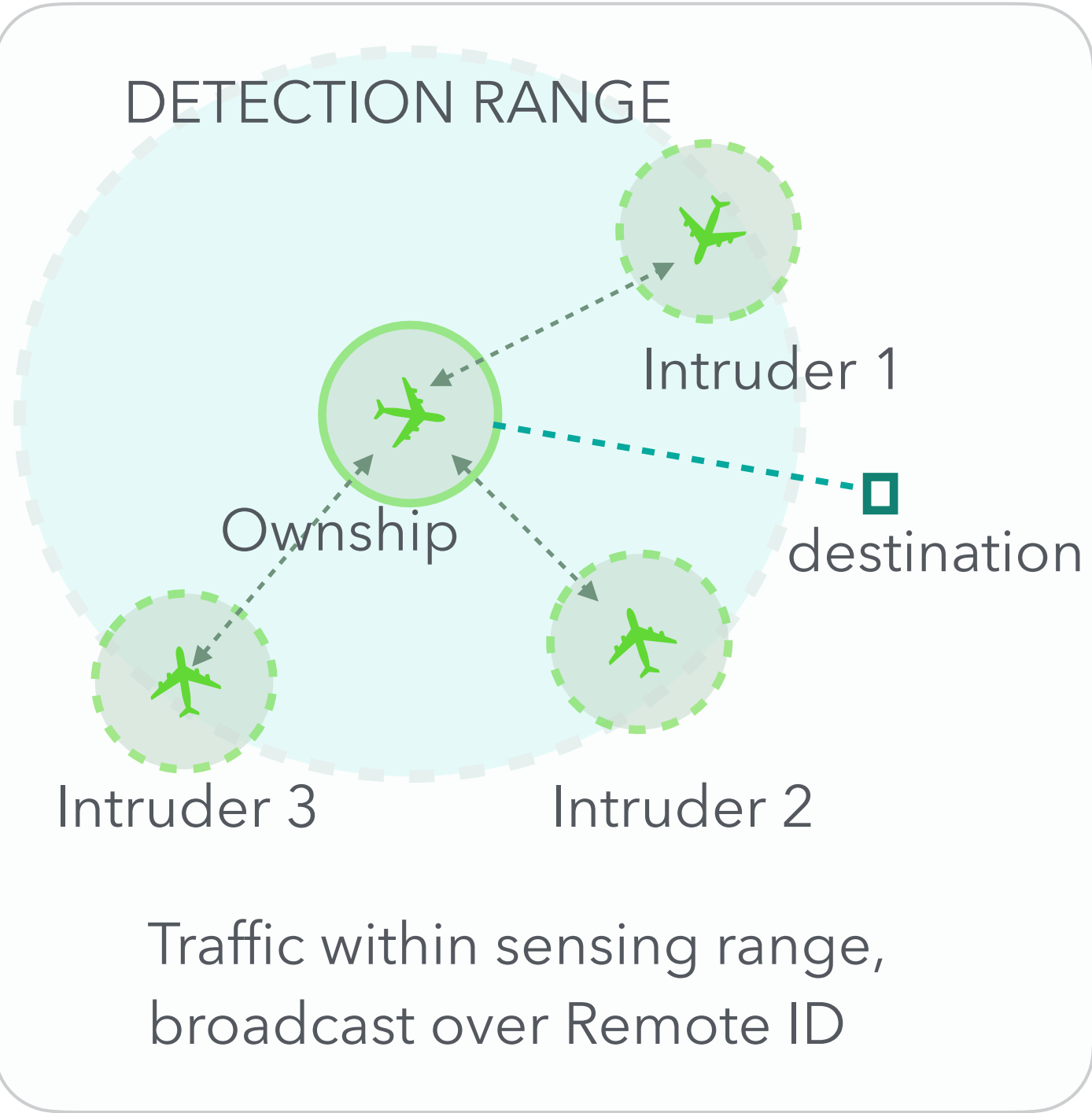


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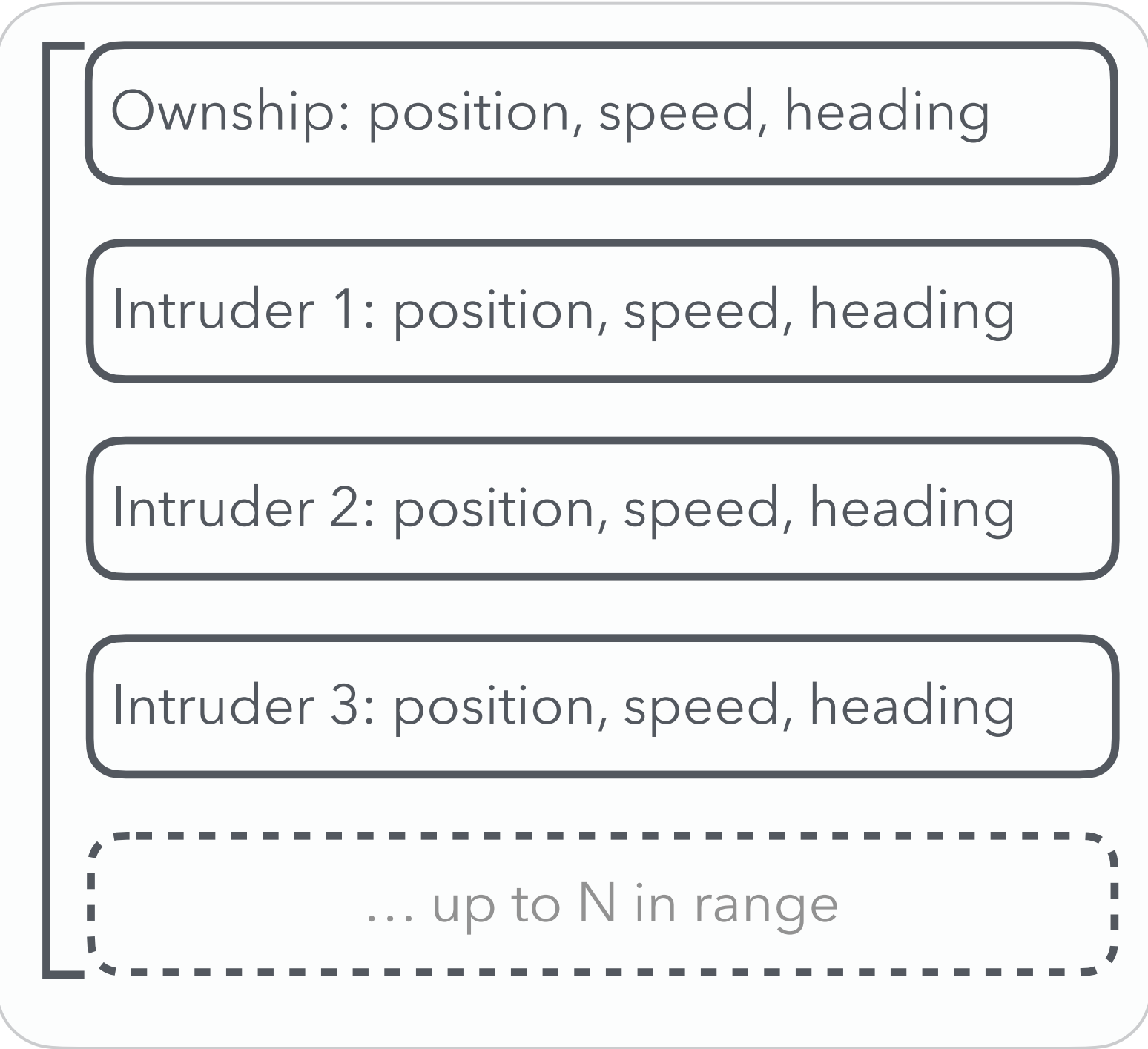


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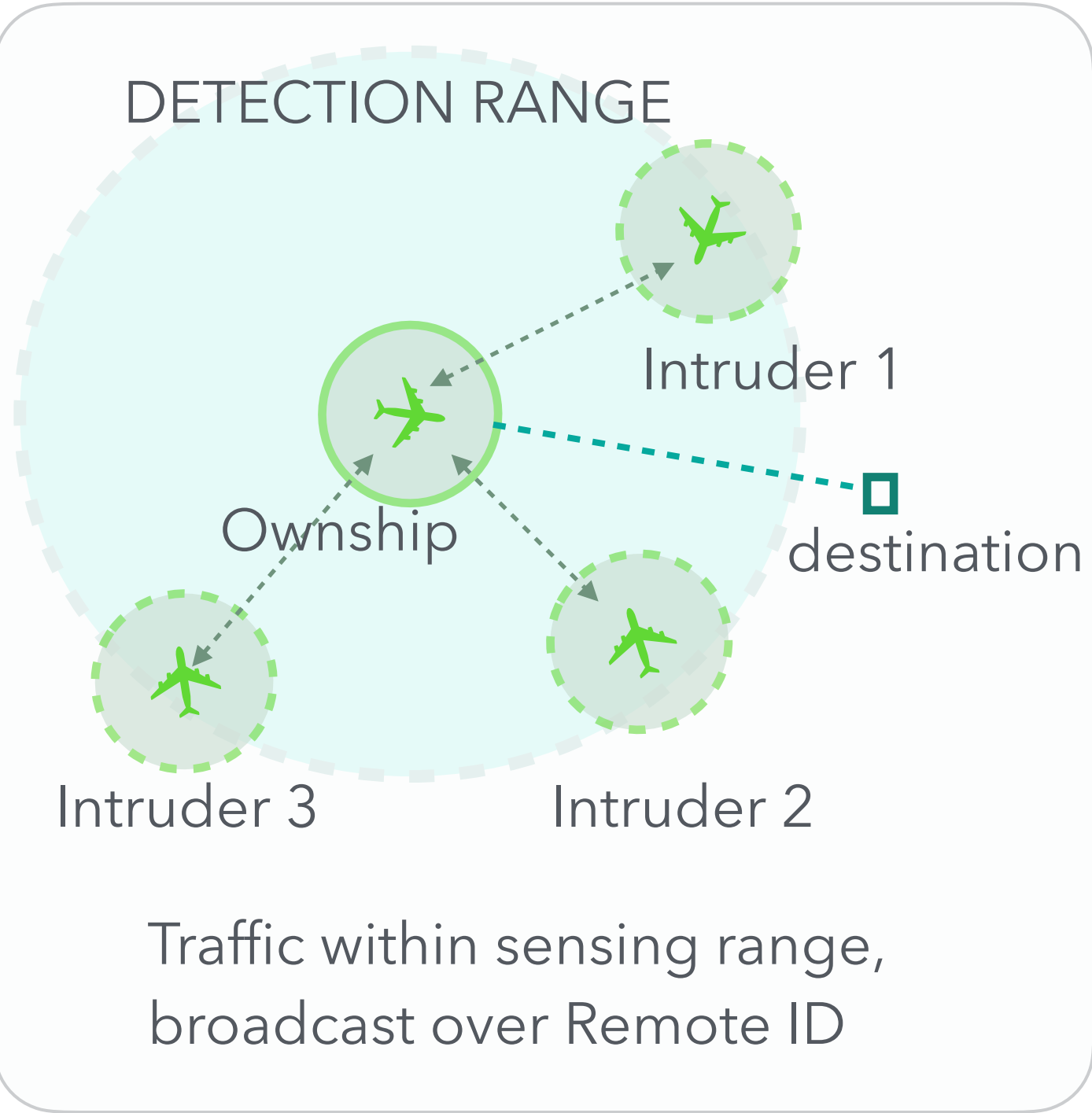


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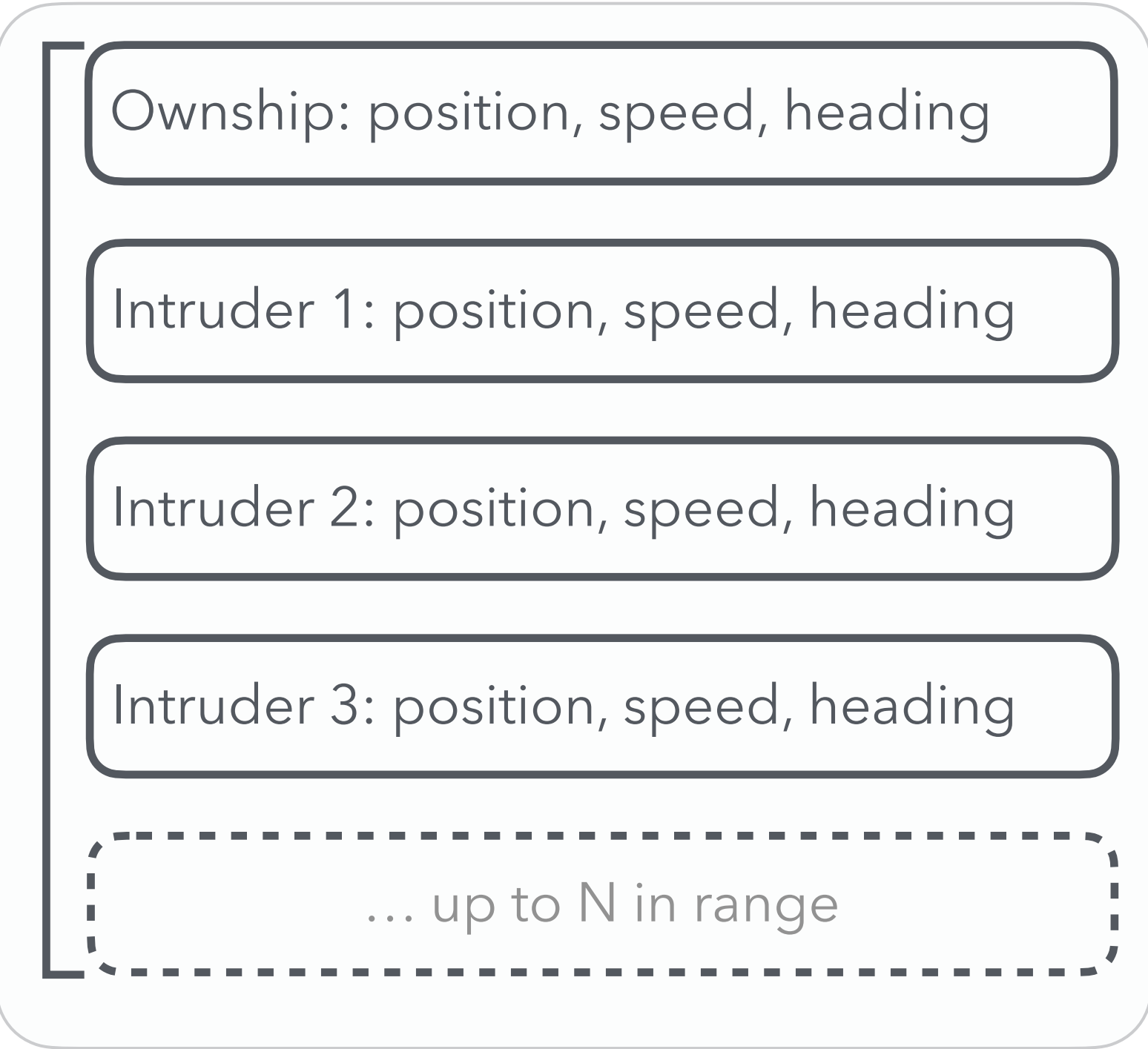


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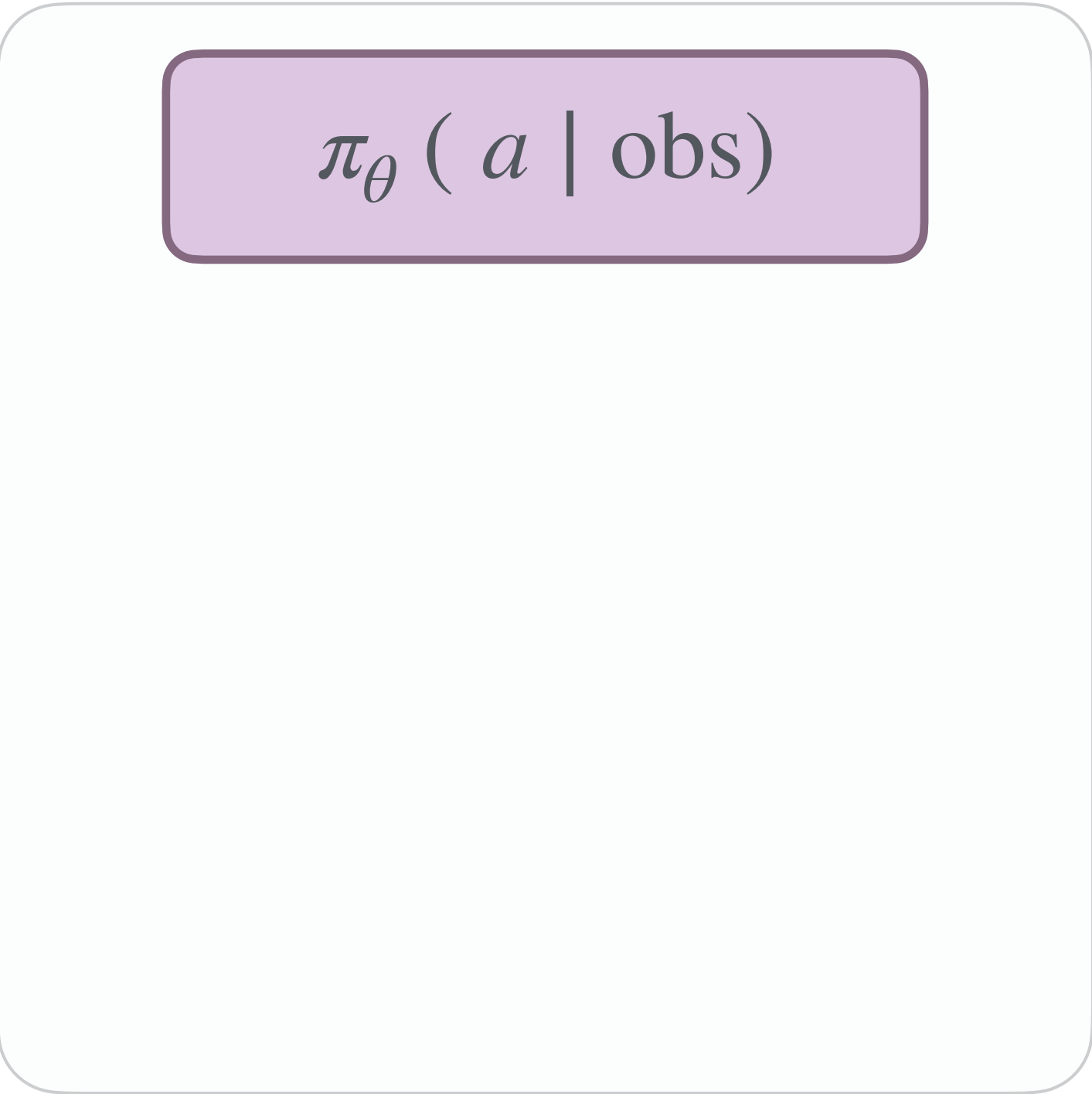
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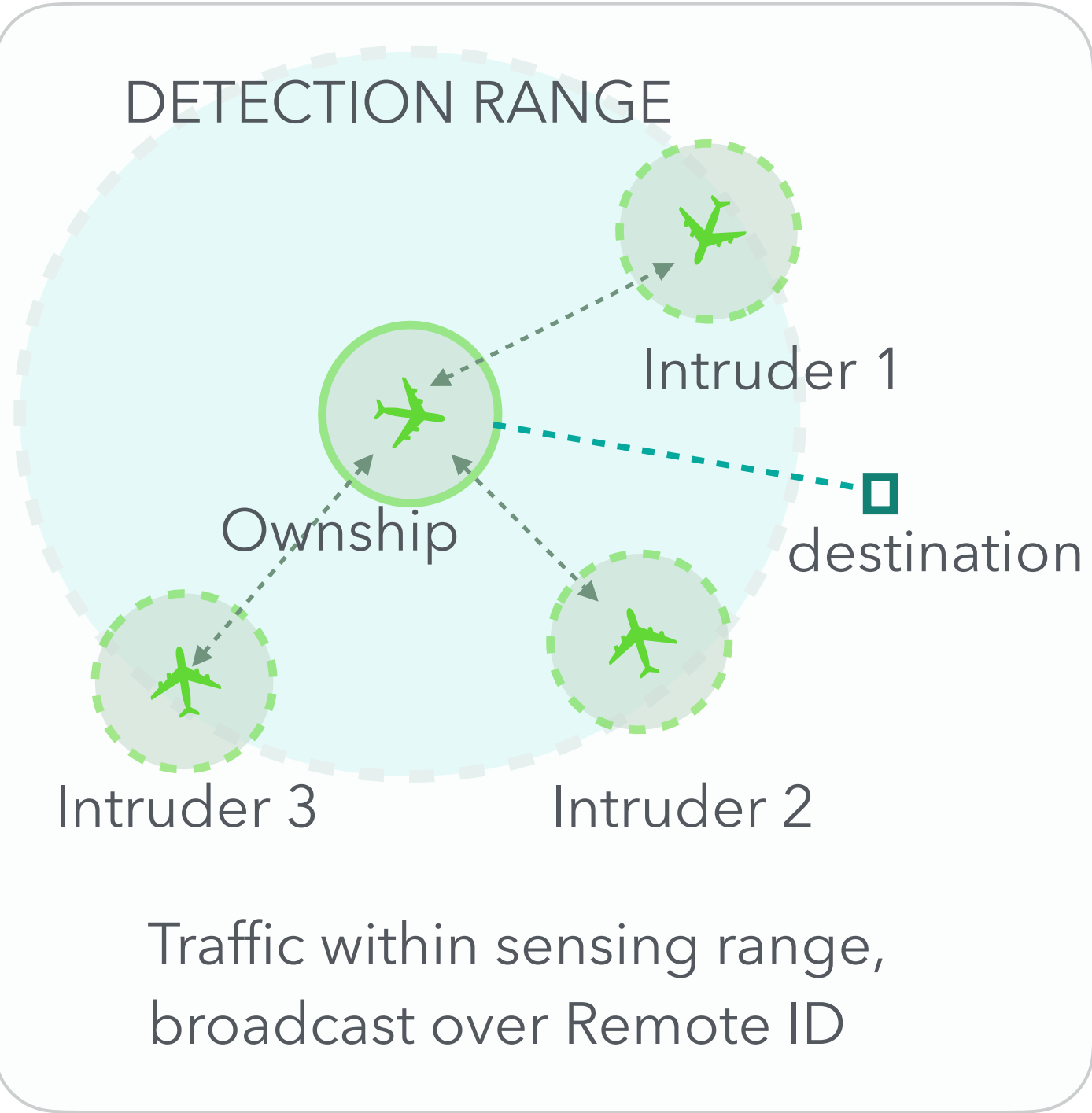


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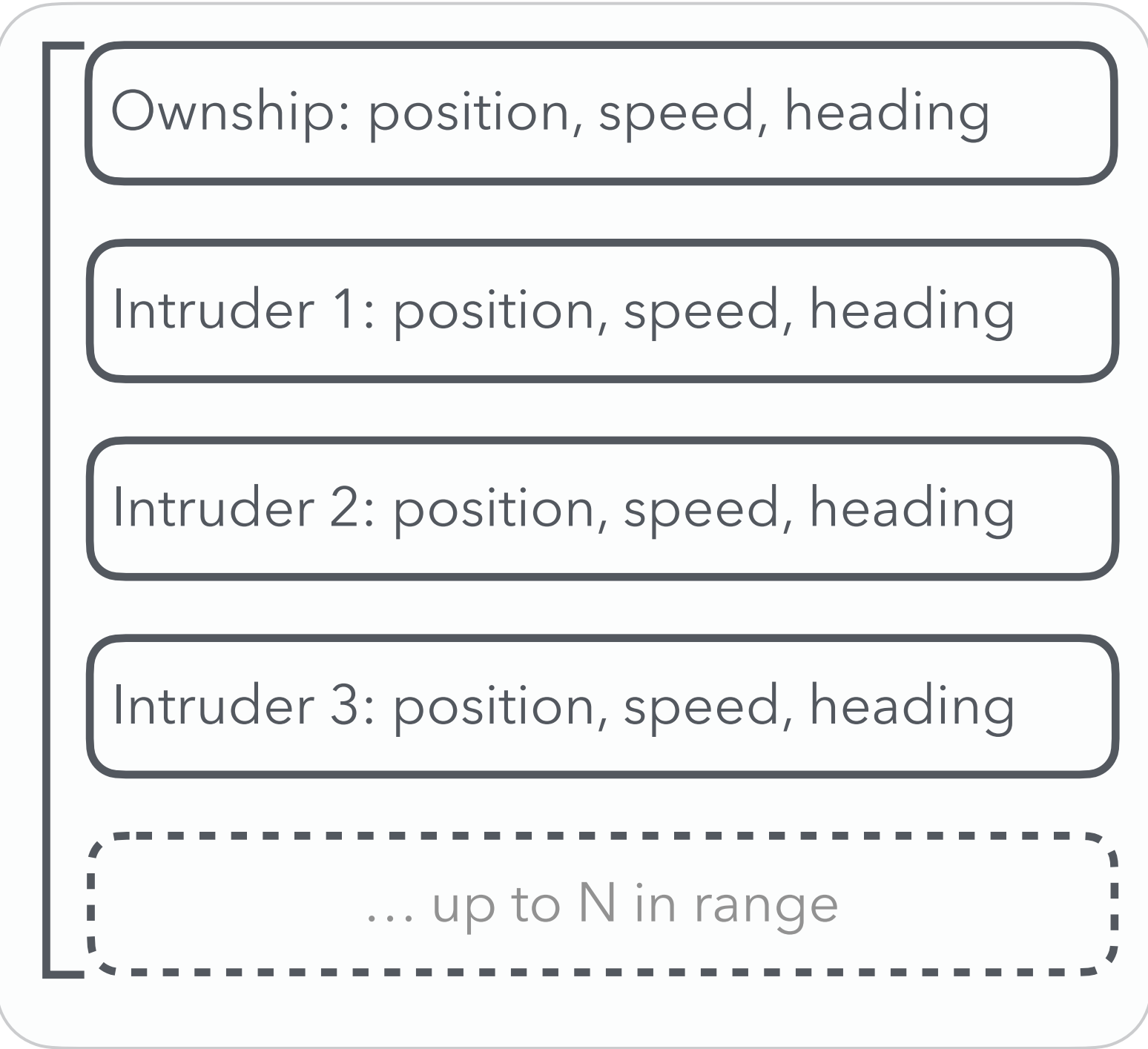


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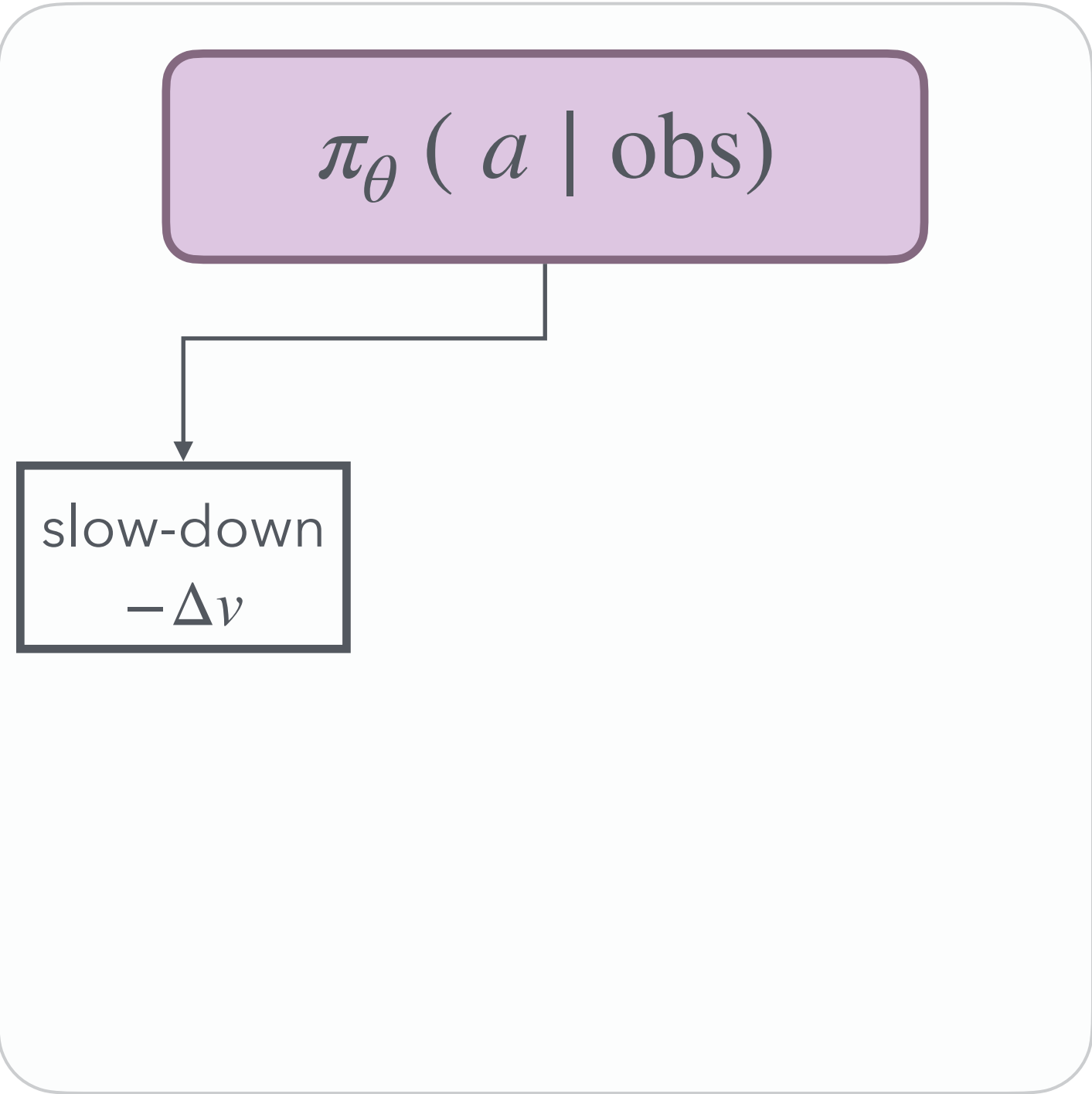
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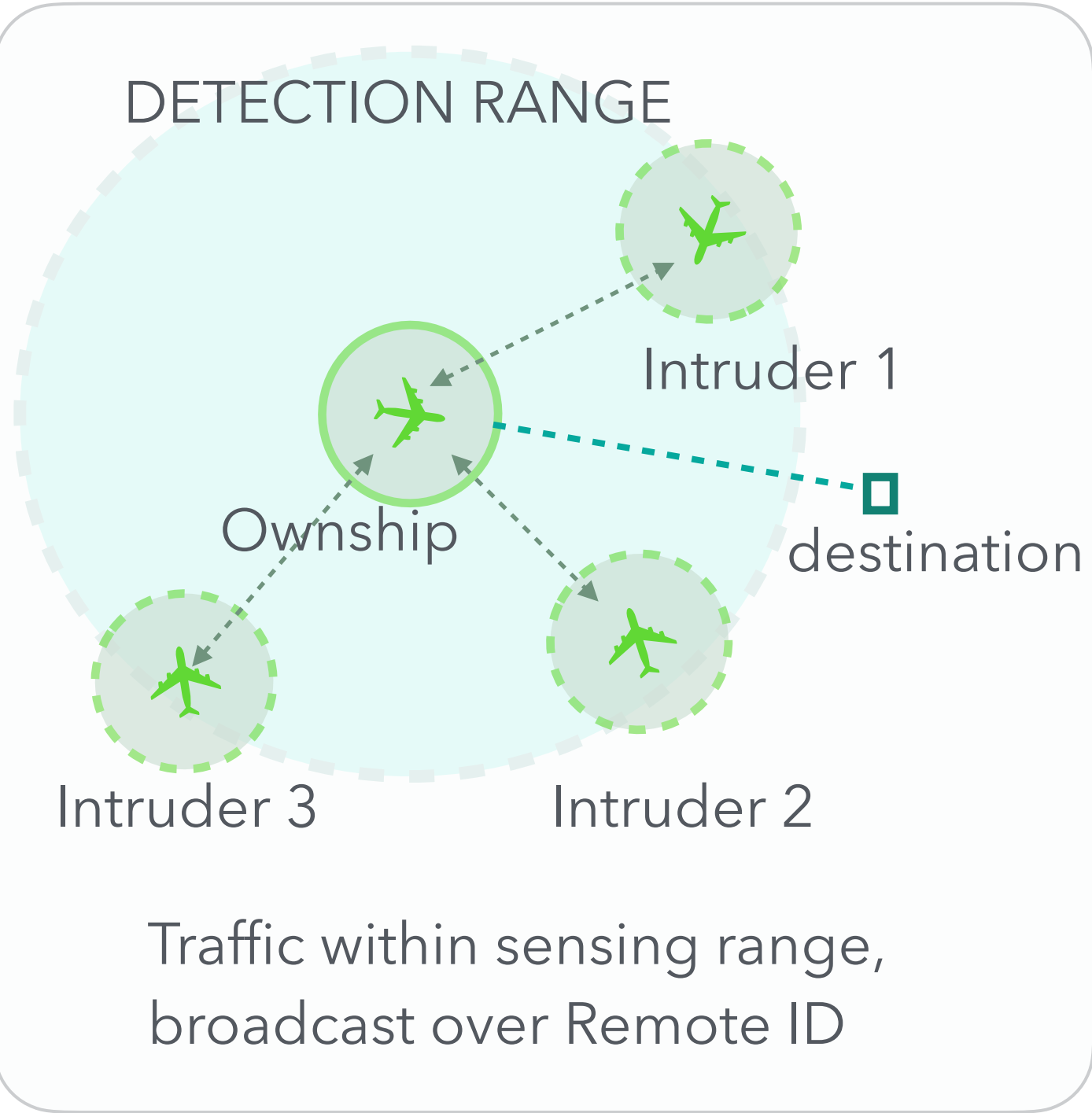


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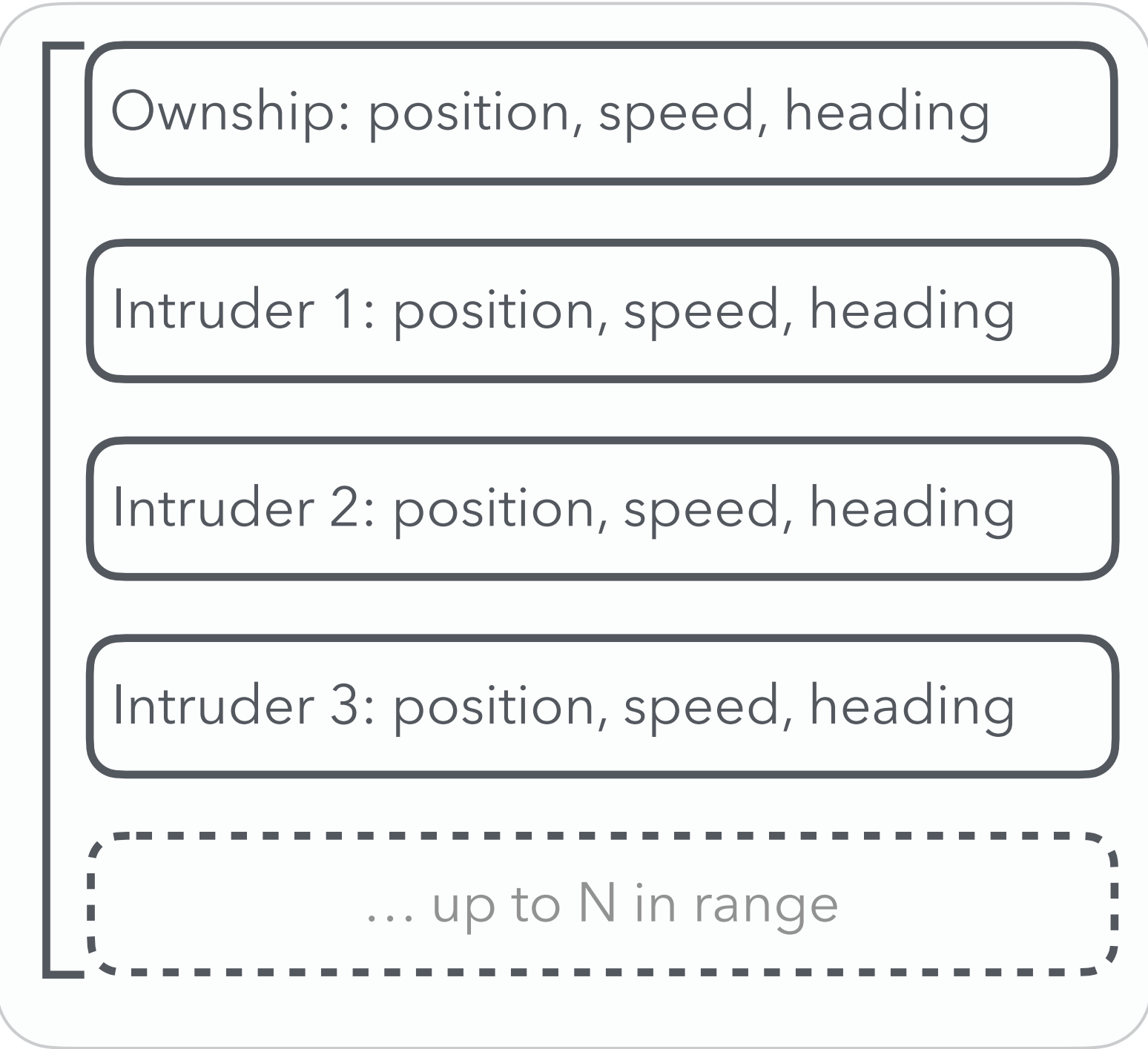


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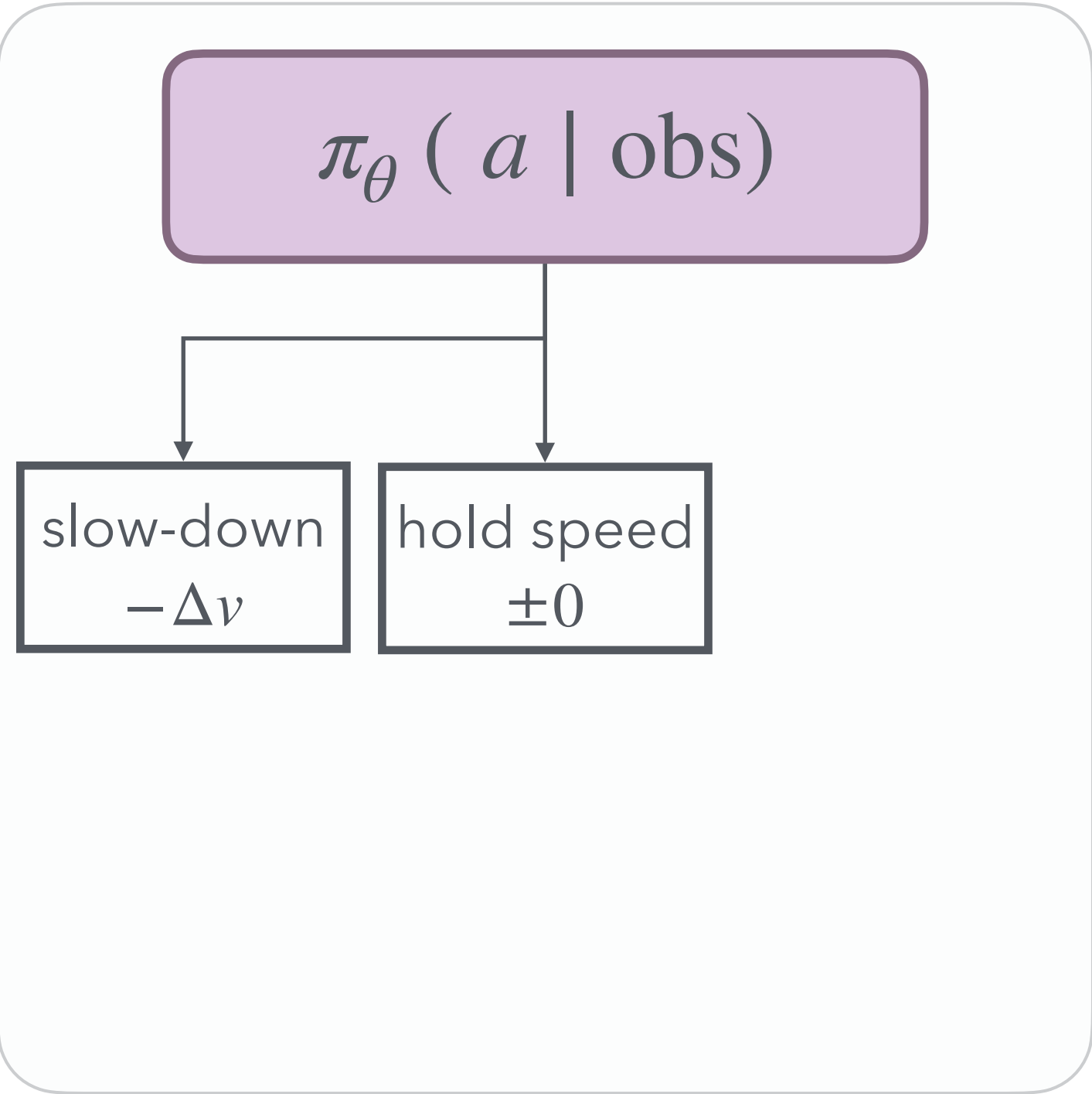
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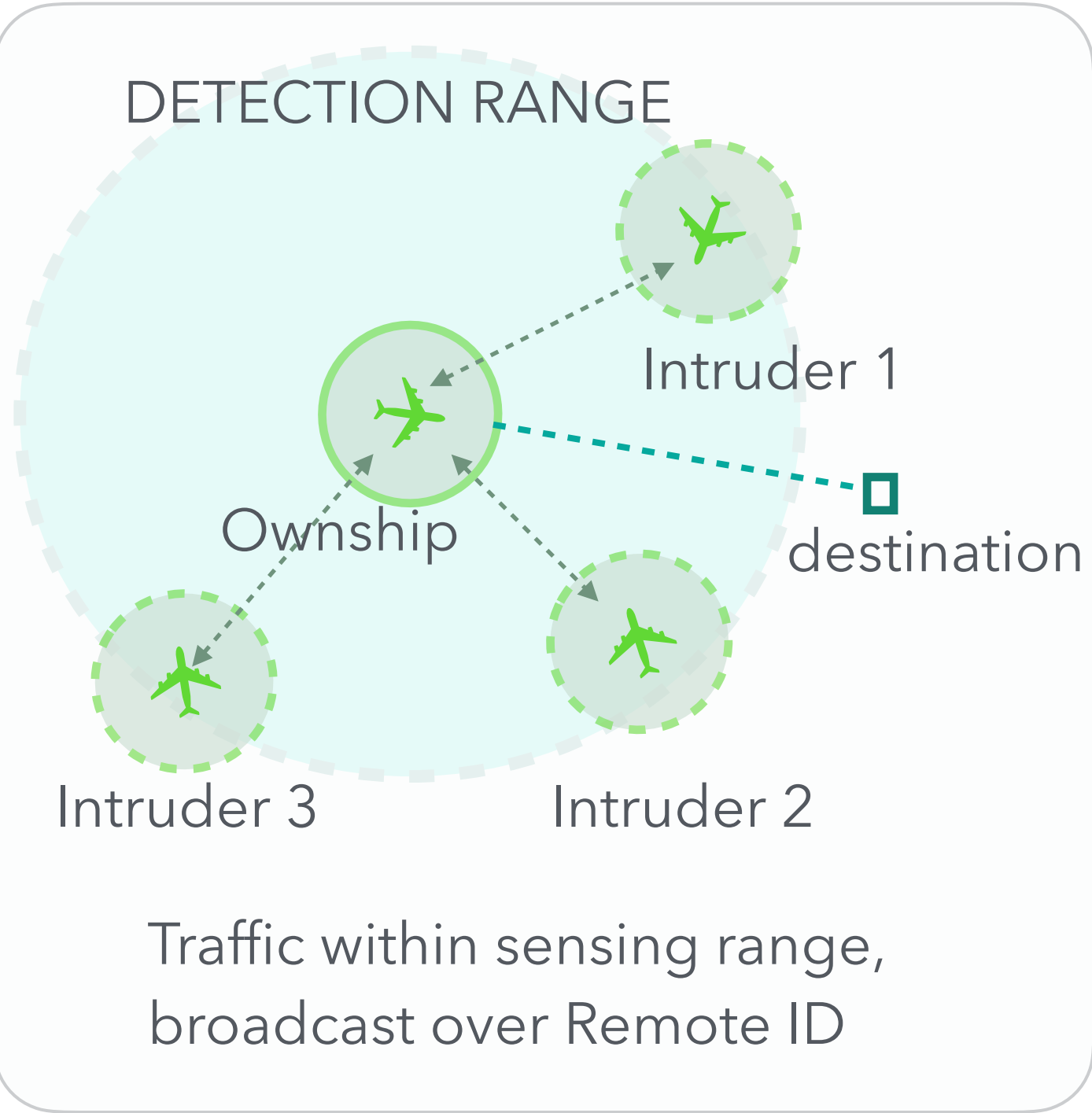


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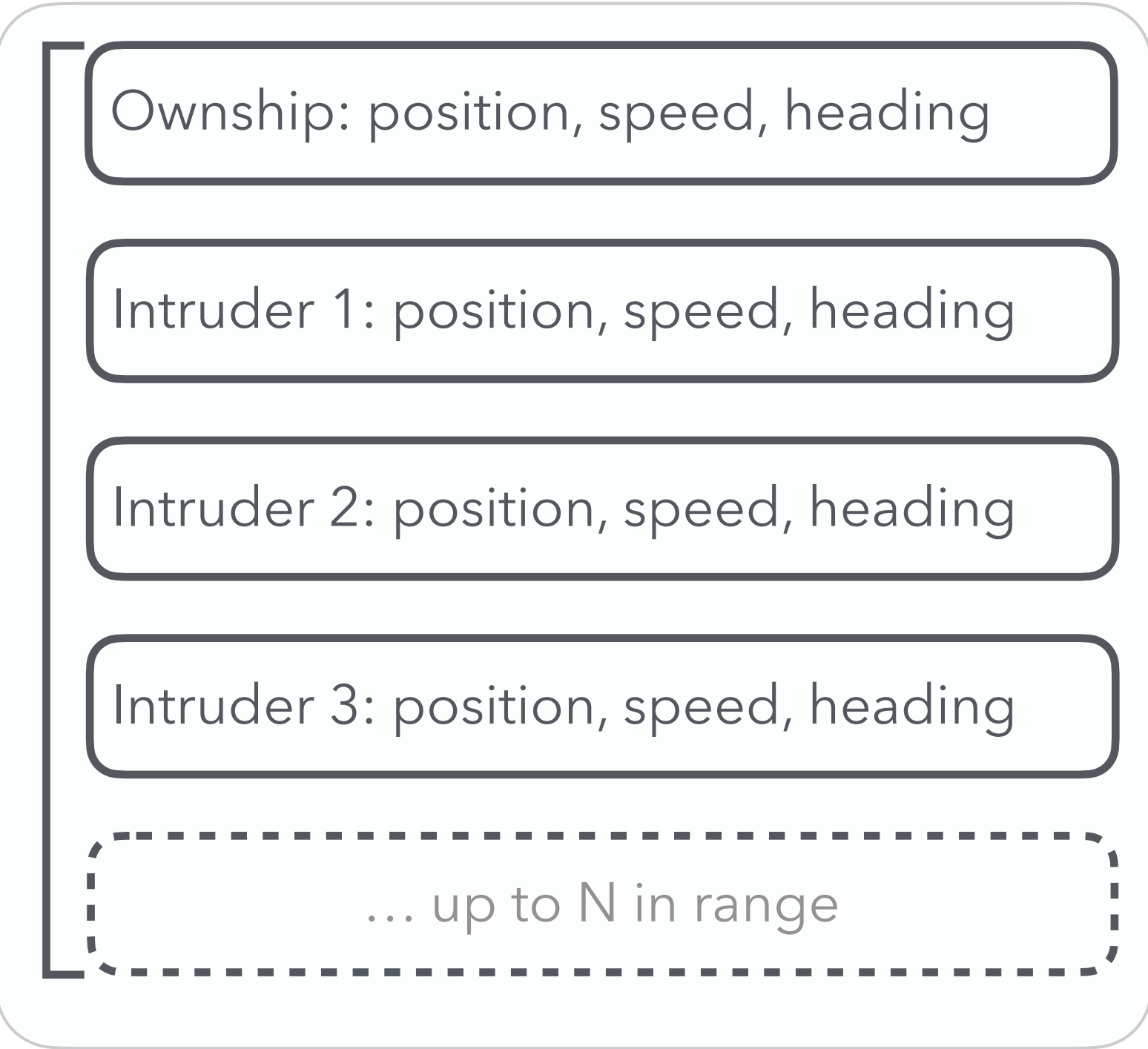


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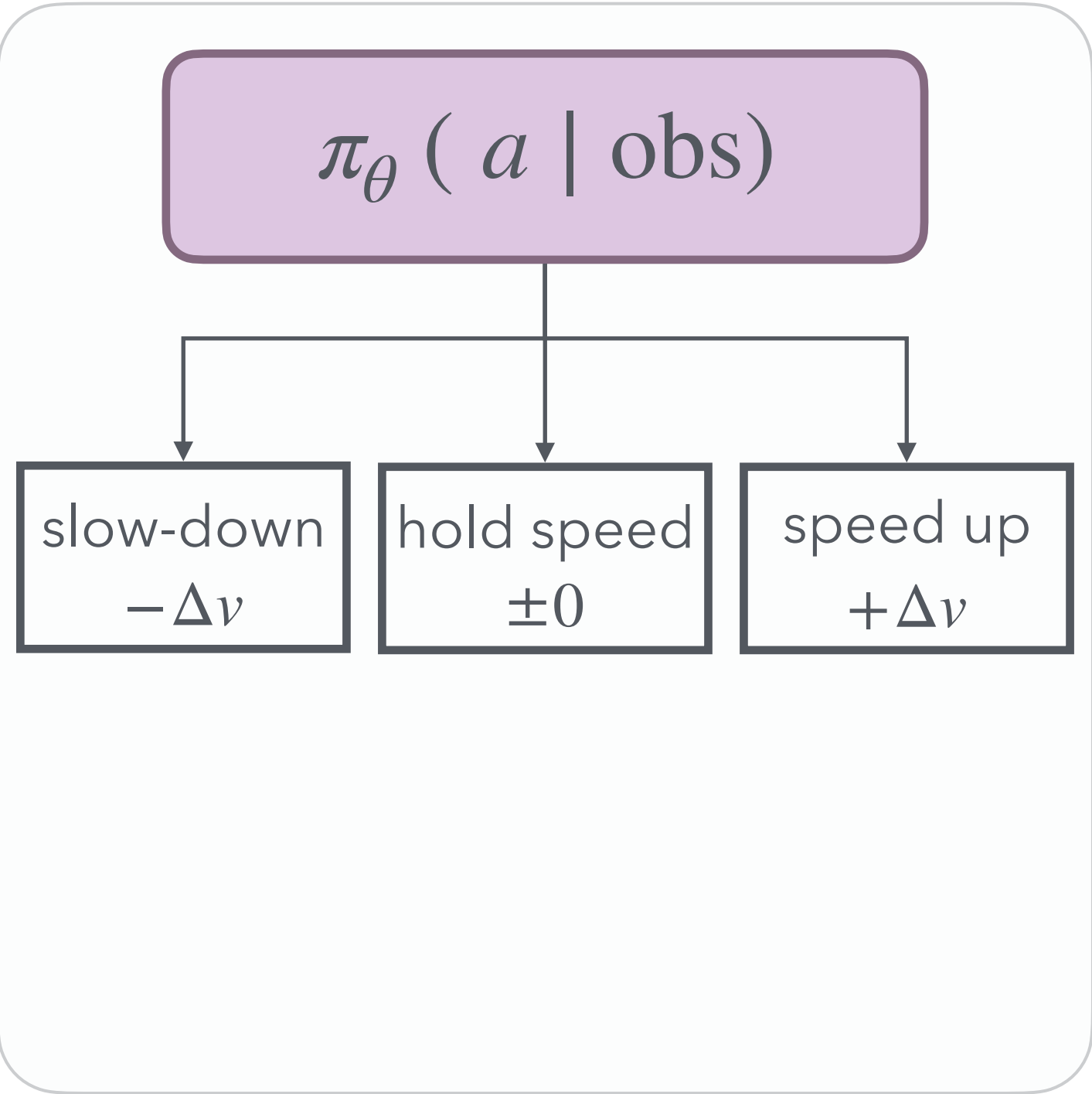
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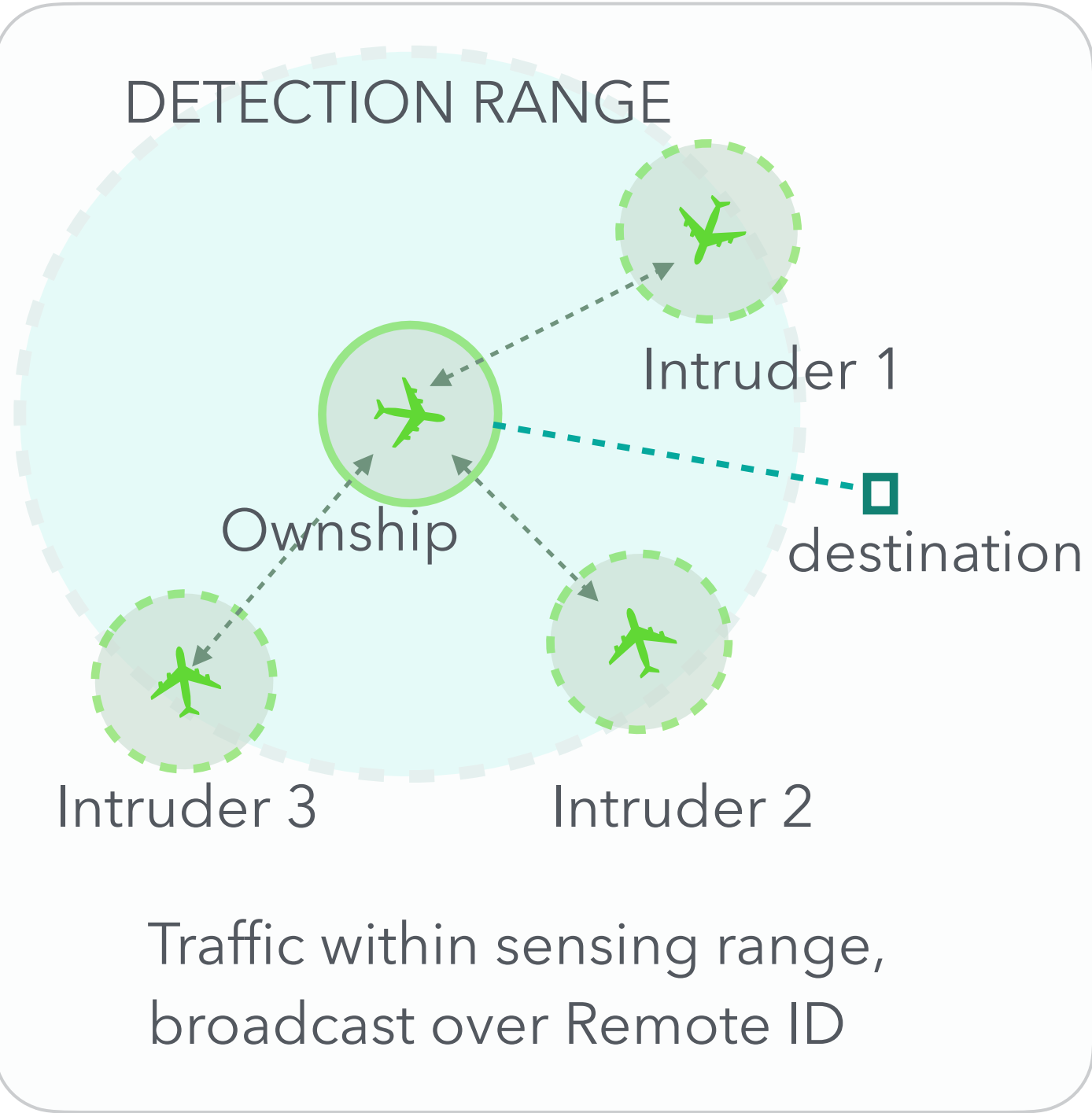


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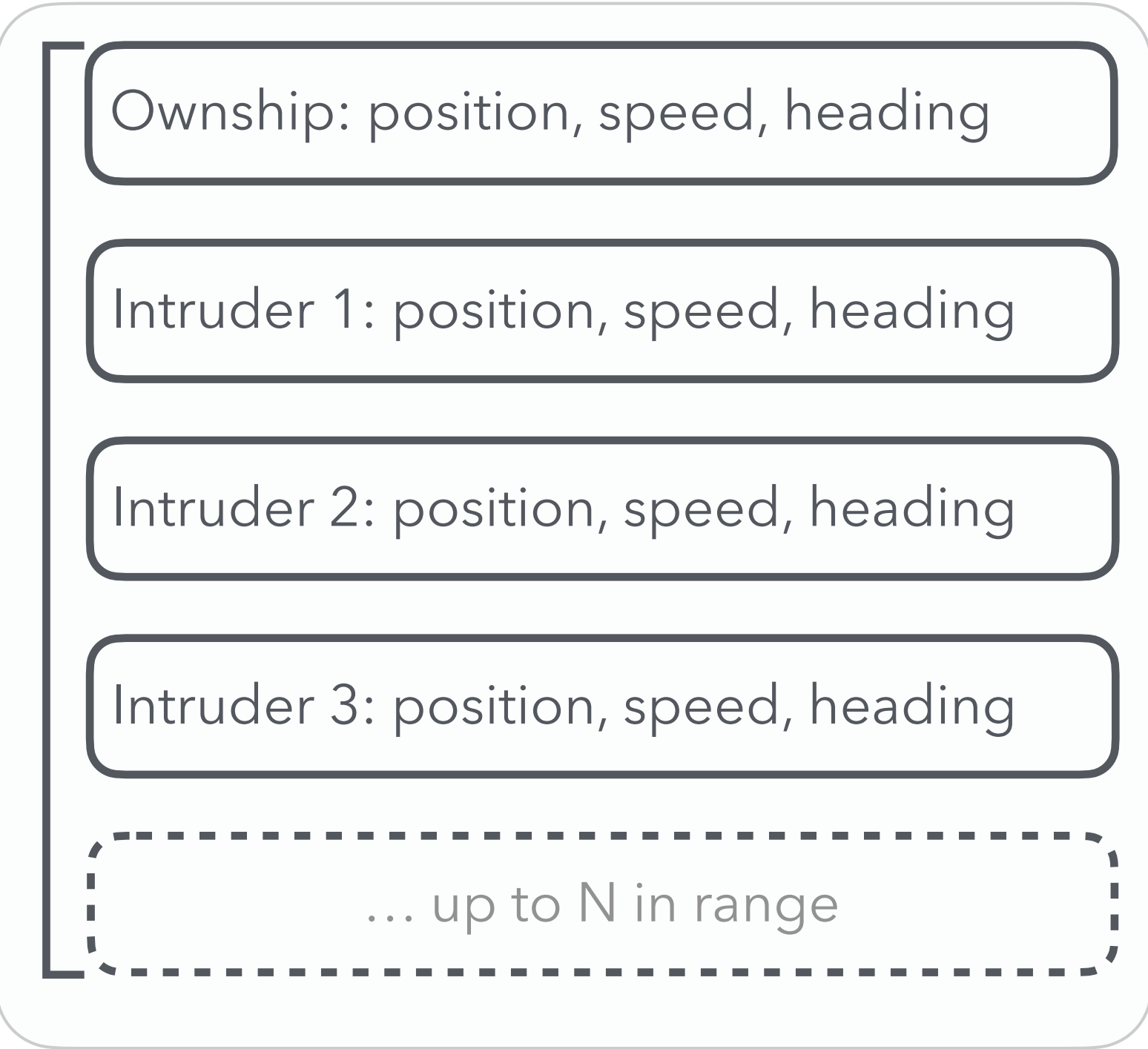


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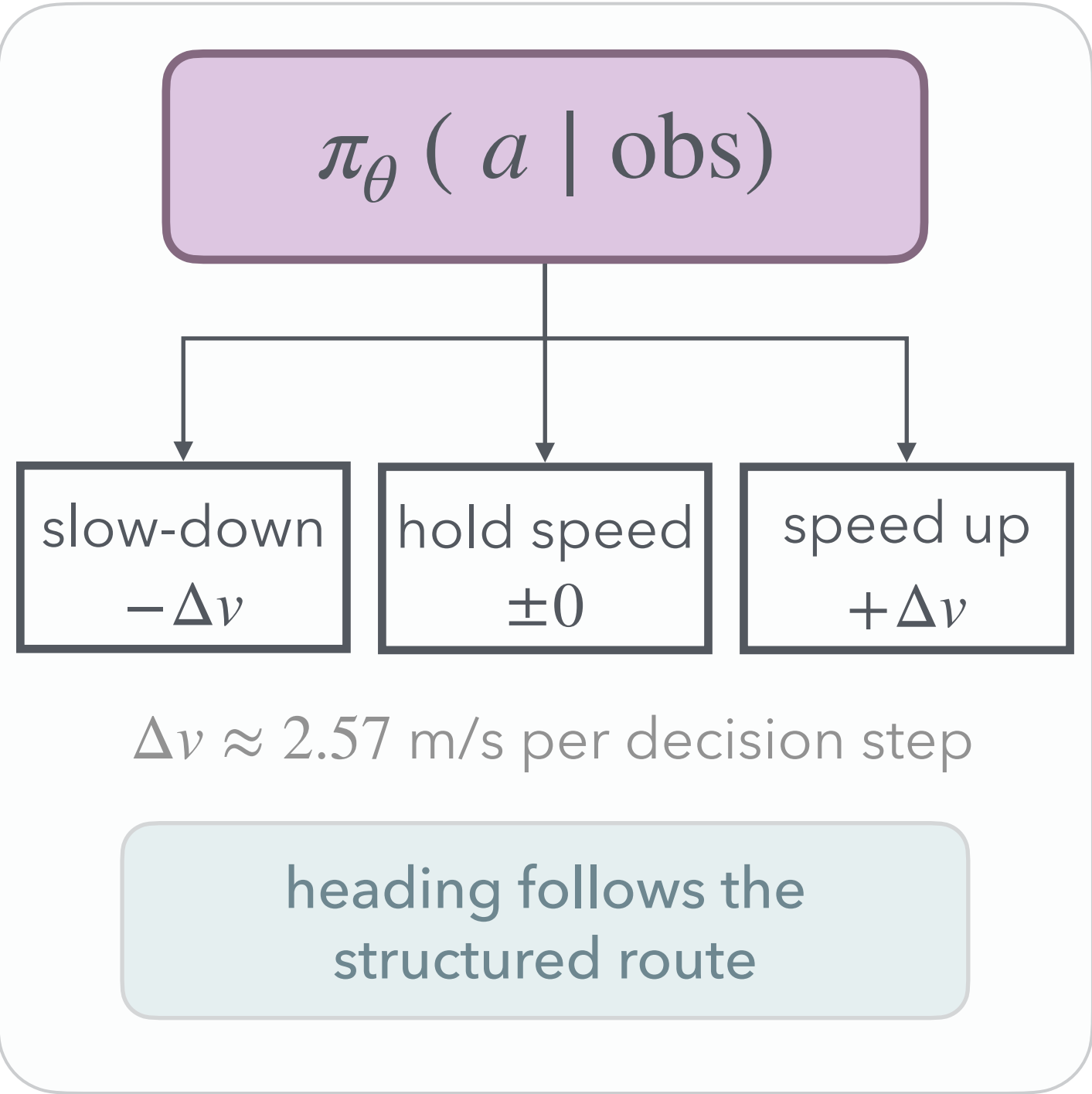
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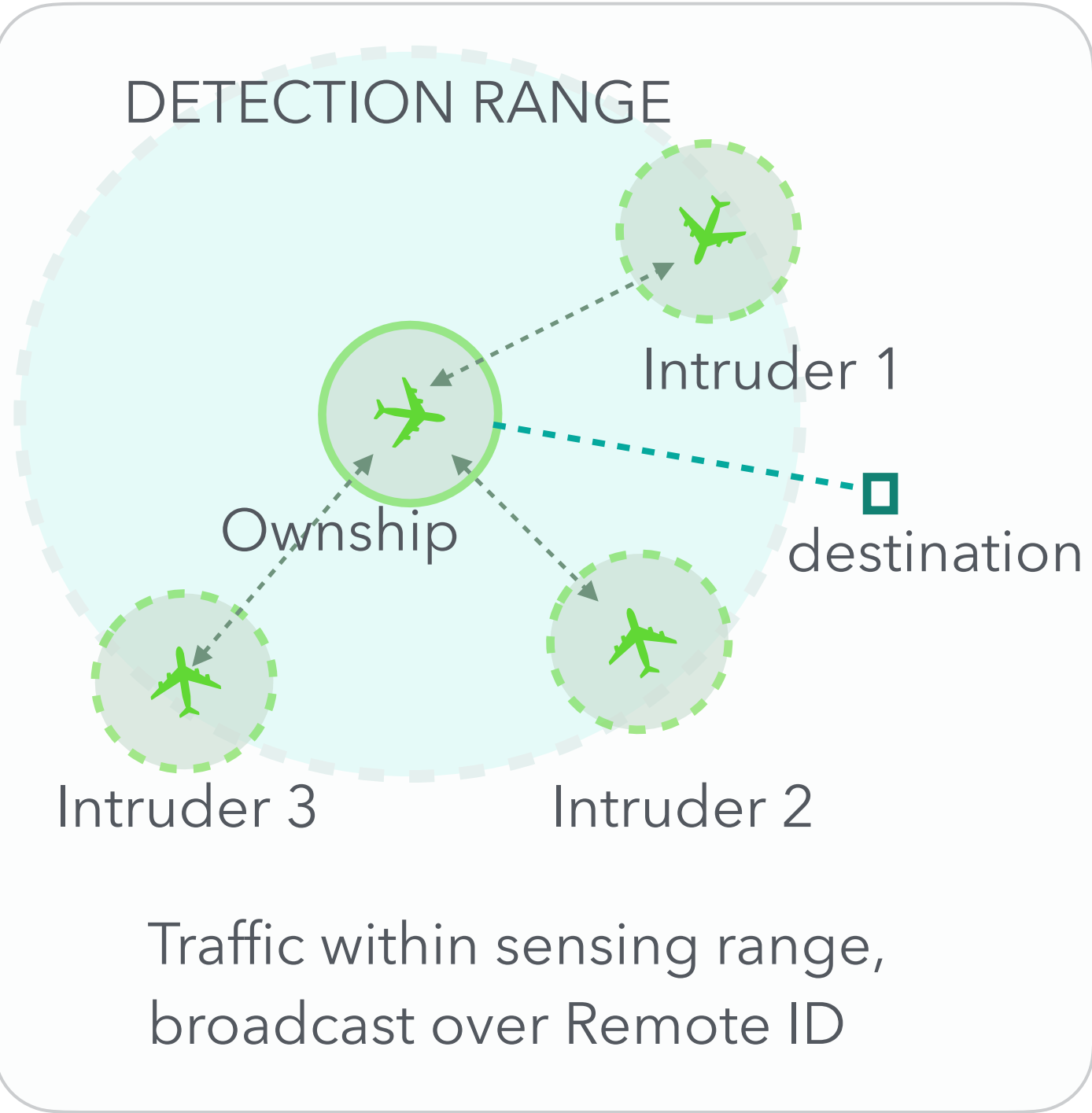


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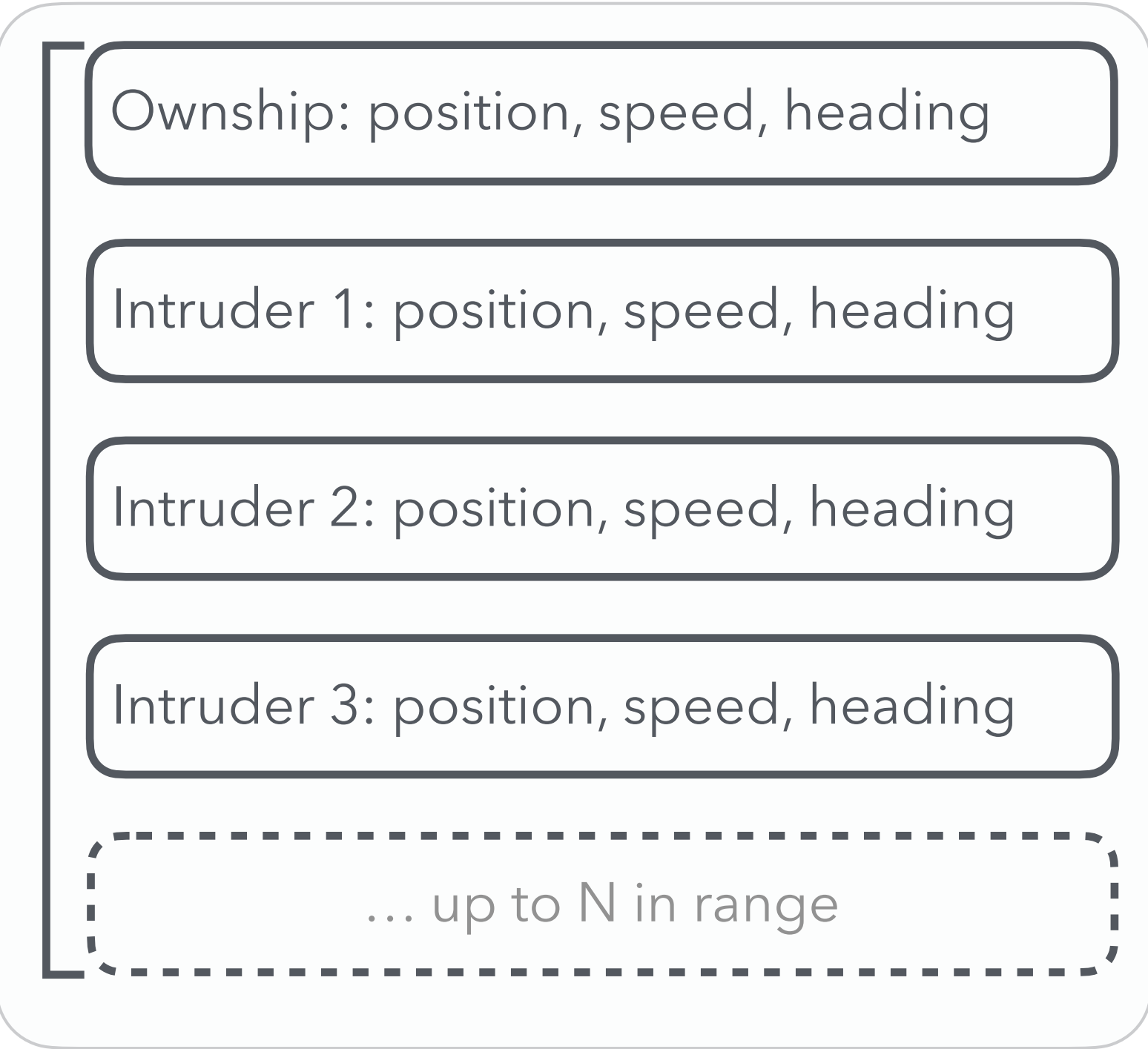


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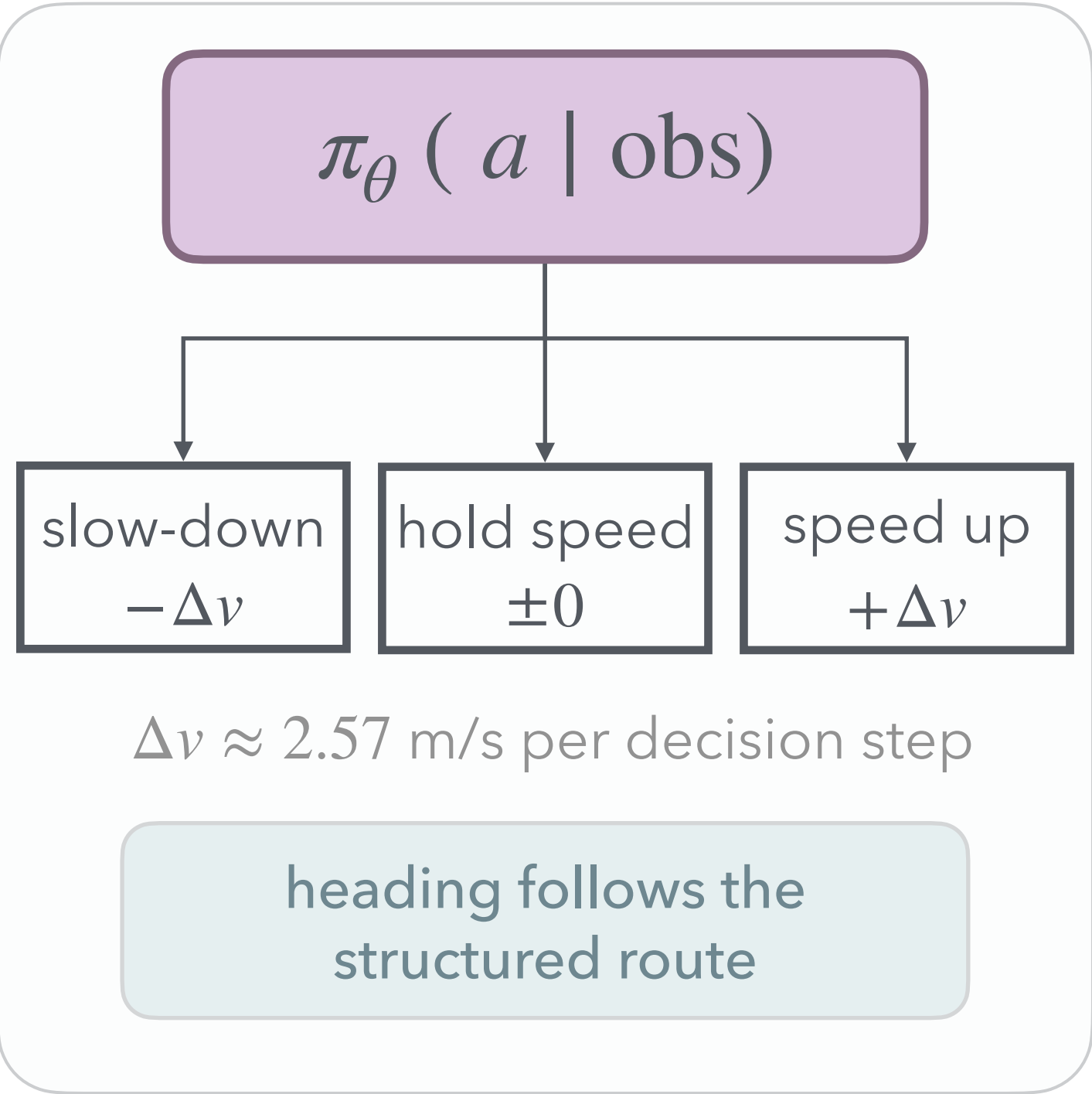
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A speed change by one UAS alters what its neighbors observe.

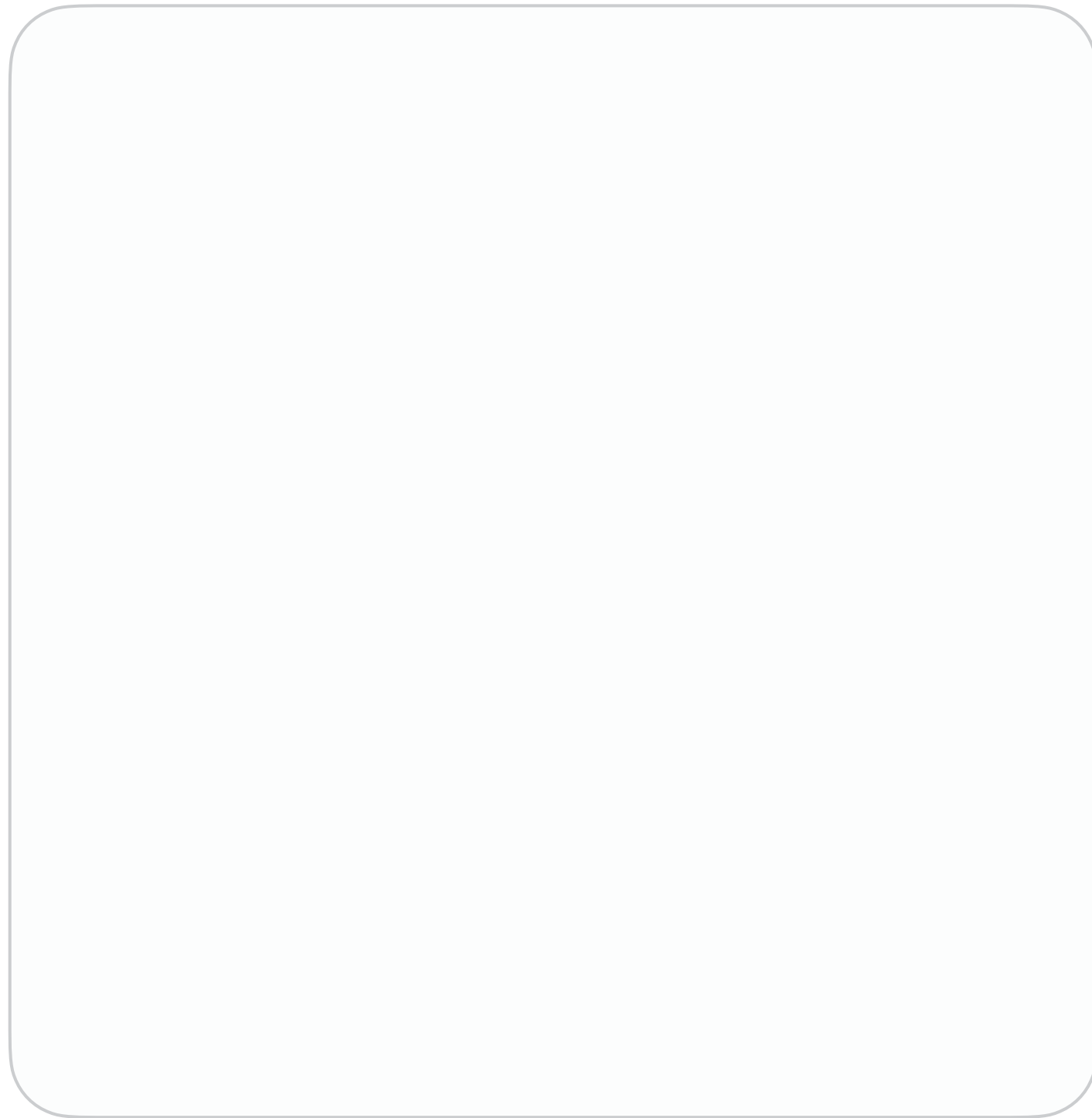
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Urban environments disrupt navigation integrity

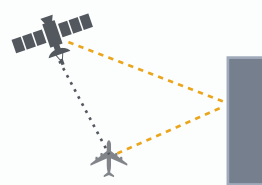
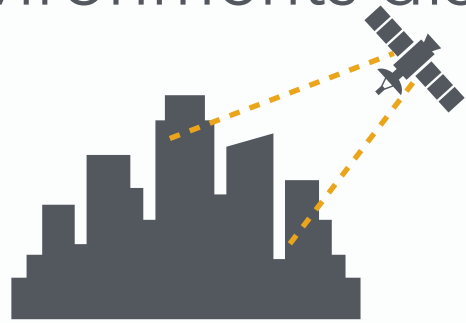


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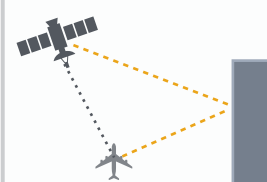
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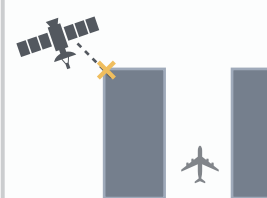
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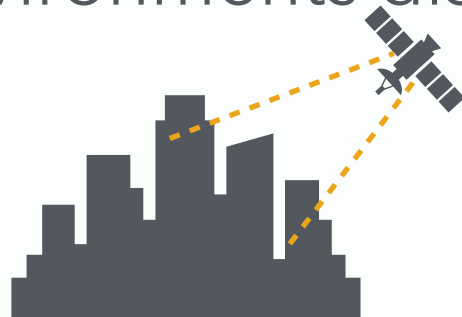
Blockage

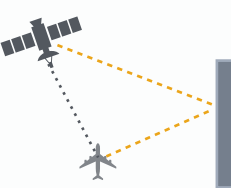
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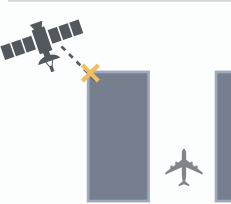
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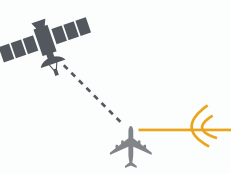




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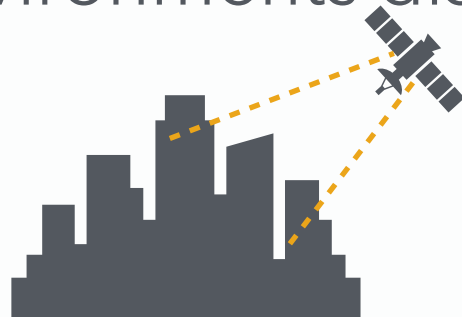


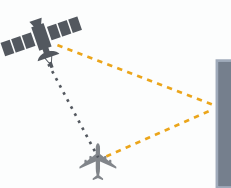
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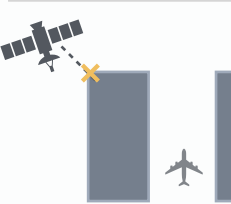
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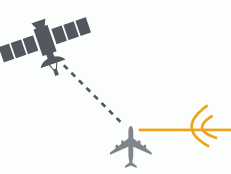




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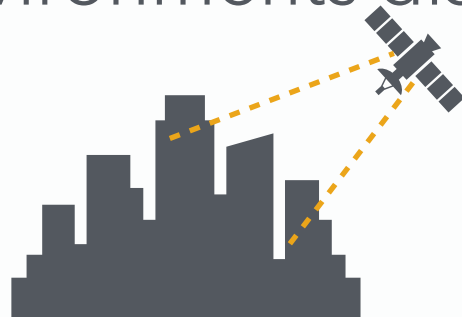
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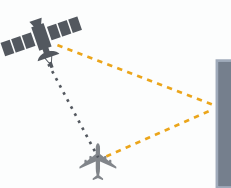


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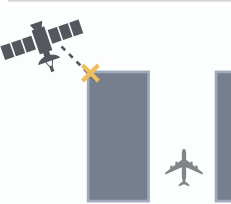
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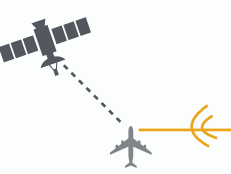




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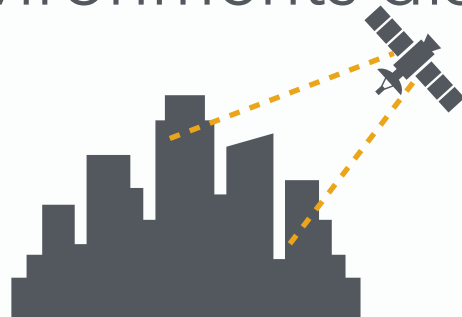
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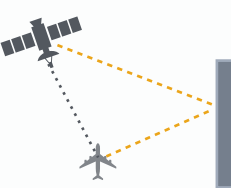
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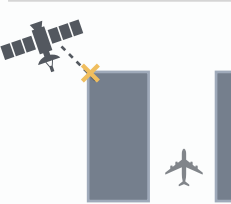
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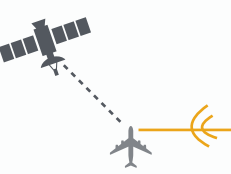




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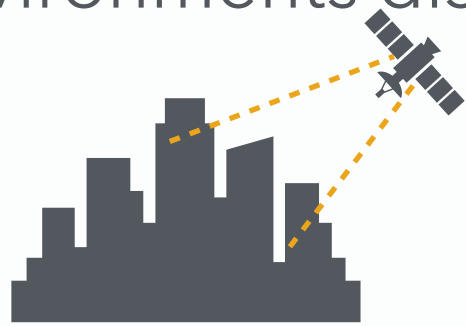


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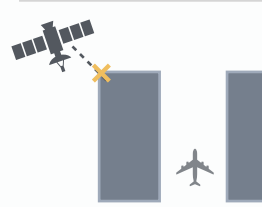
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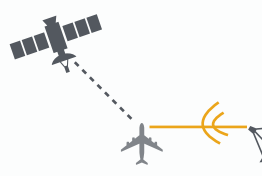
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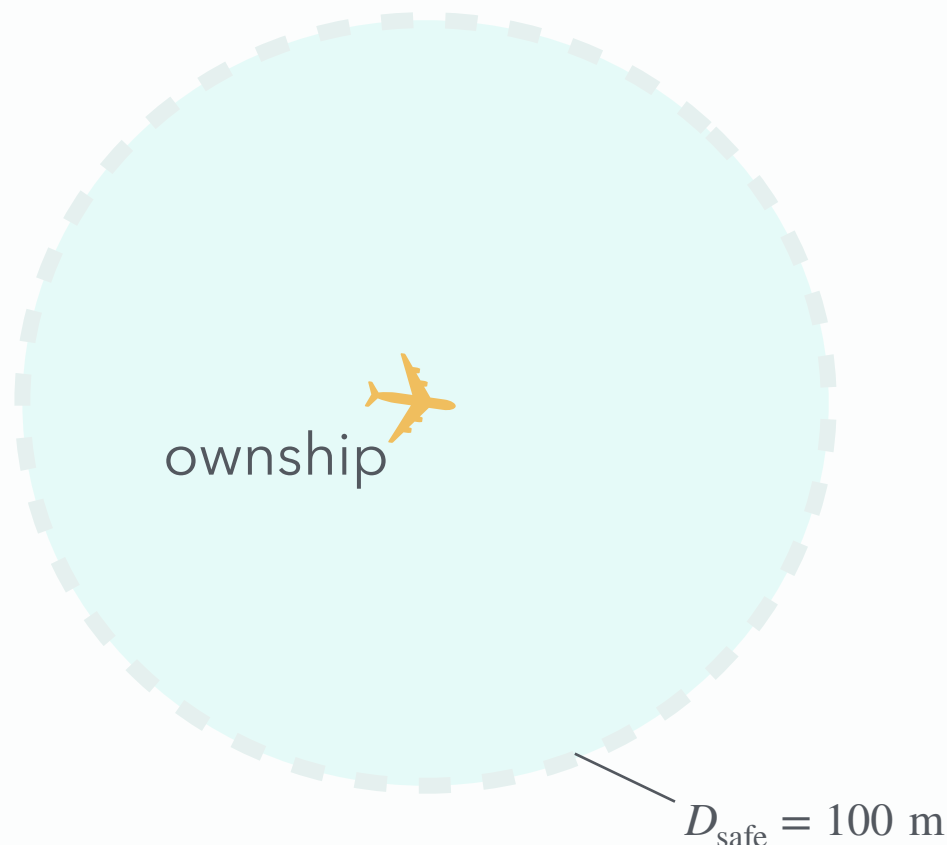


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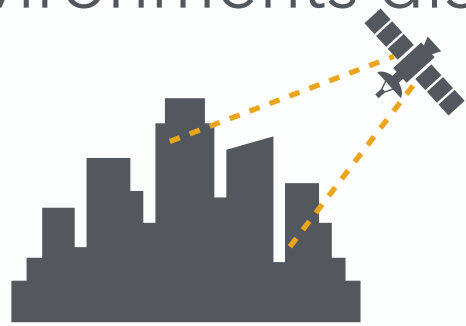


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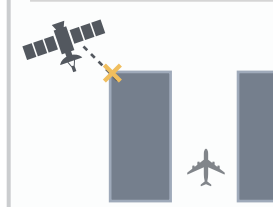
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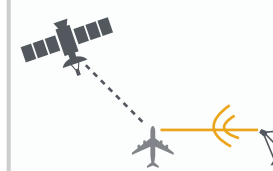
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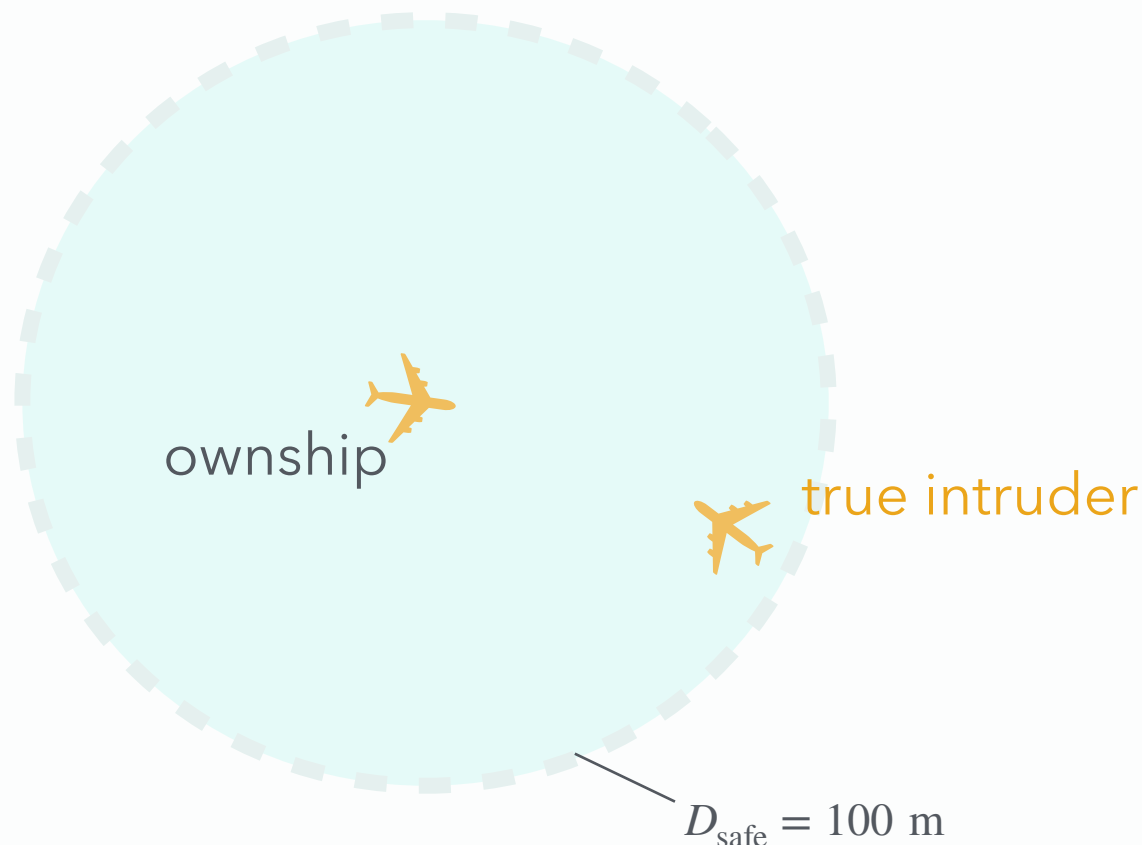


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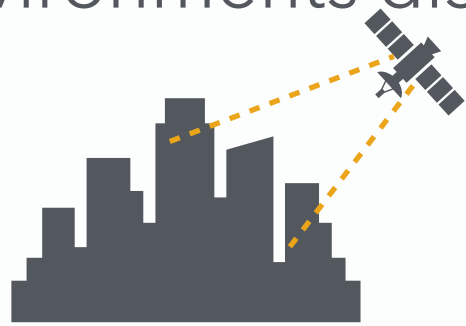


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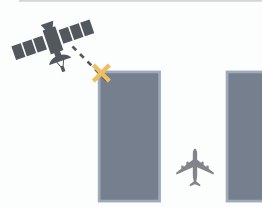
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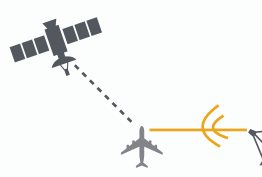
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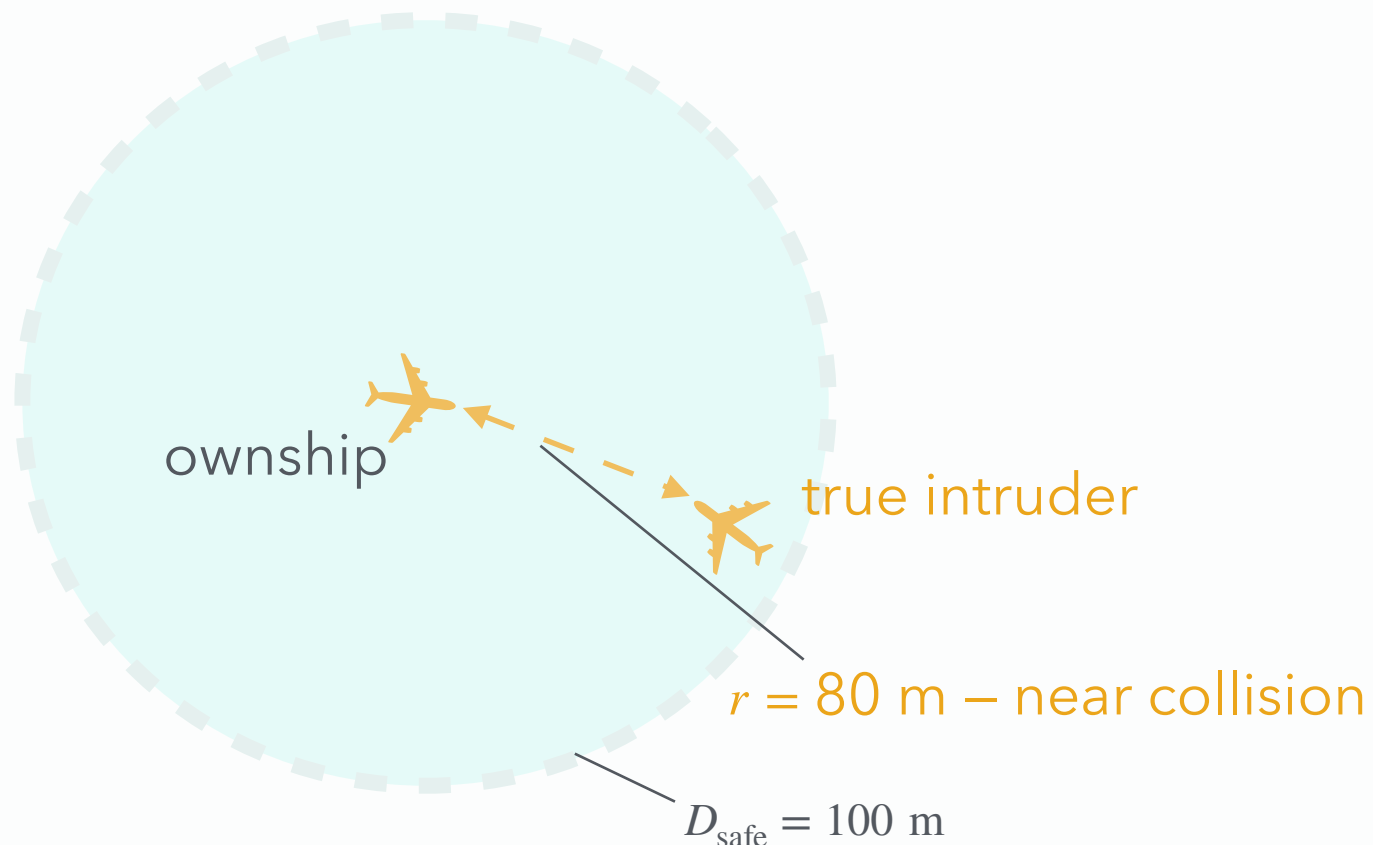


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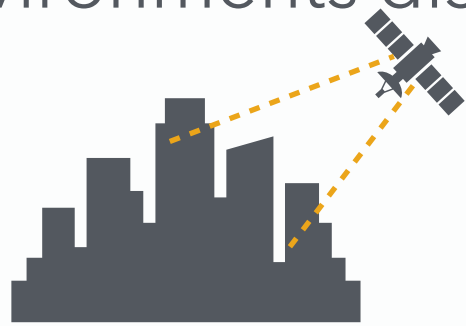


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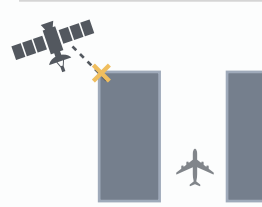
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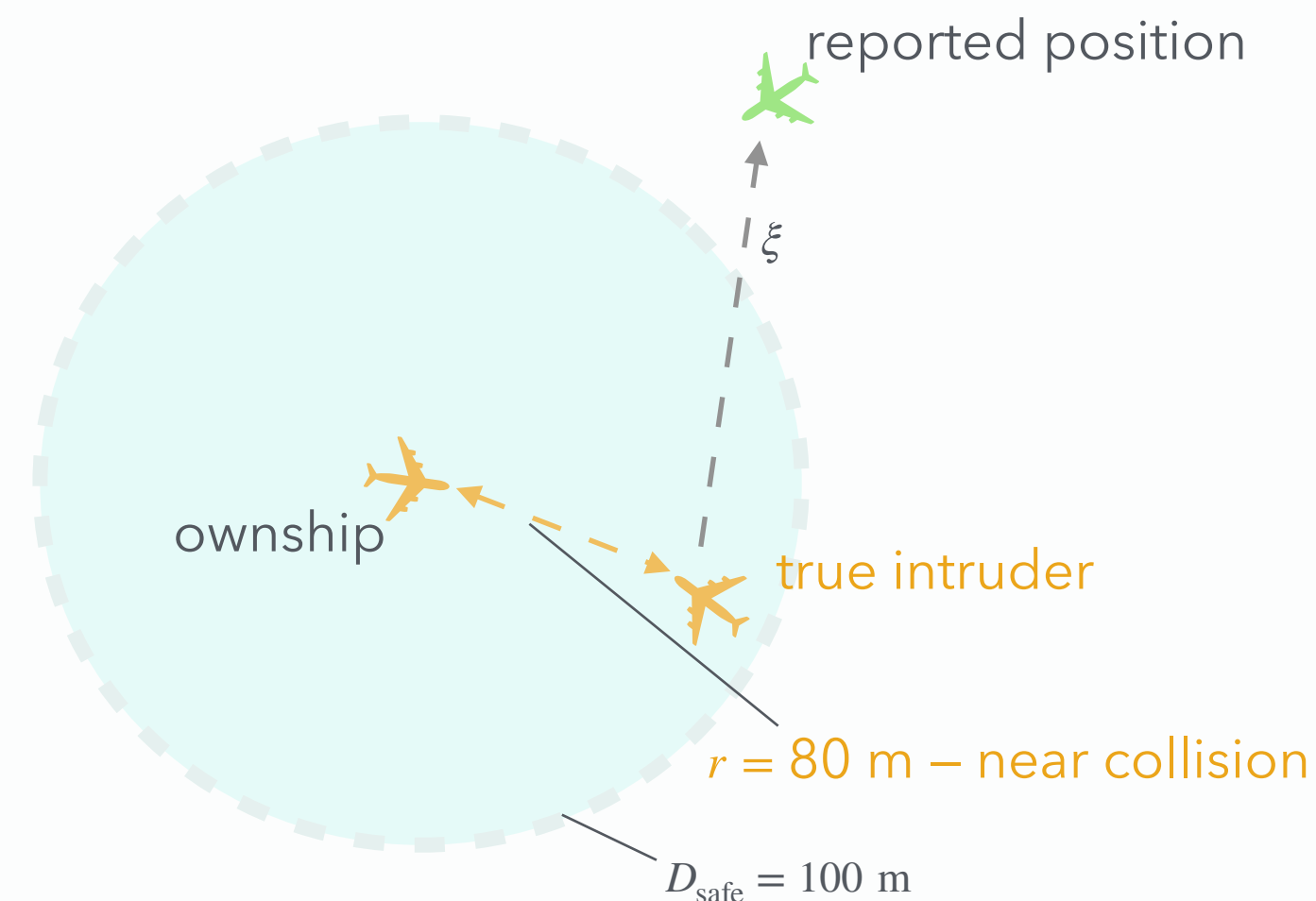


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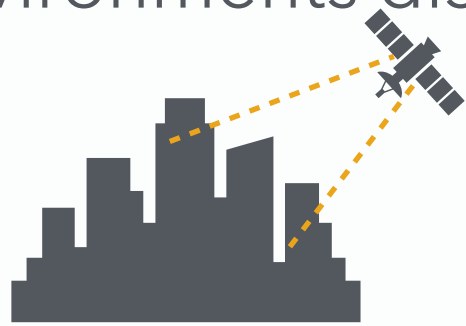


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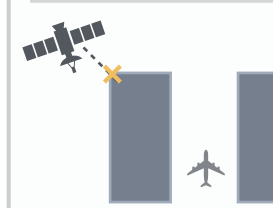
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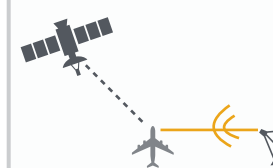
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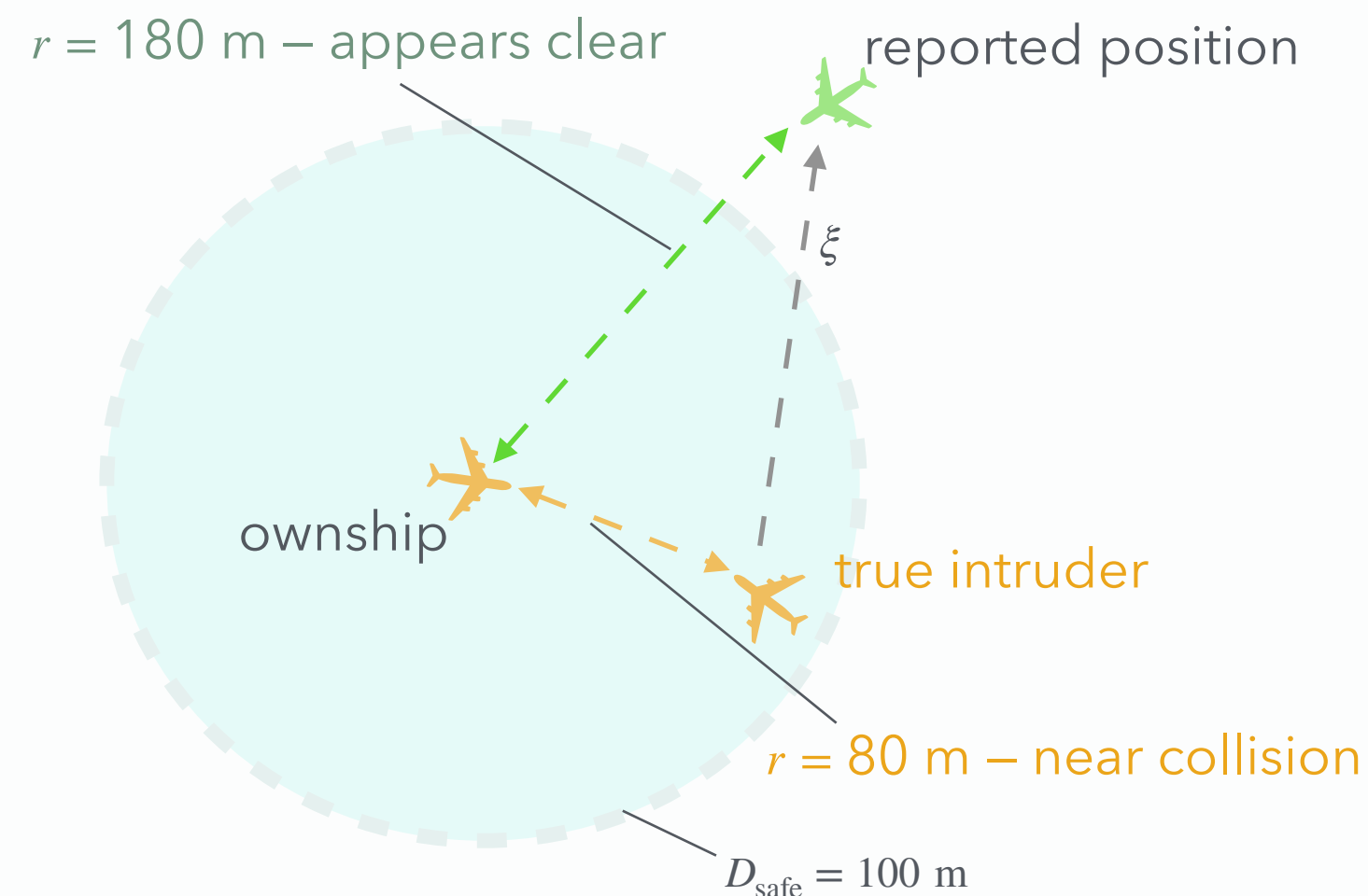


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1. WHY URBAN GNSS DEGRADES

Urban environments disrupt navigation integrity

Multipath
Reflections from building faces bias position estimation

Blockage
Urban canyons create gaps and unstable fixes

Spoofing / jamming
Delayed signals, false or replayed signals, indistinguishable from the truth

2. CONSEQUENCE

A closing conflict can be reported as clear traffic

$r = 180\text{ m}$ – appears clear

reported position

ξ

ownship

true intruder

$r = 80\text{ m}$ – near collision

$D_{\text{safe}} = 100\text{ m}$

3. DEGRADATION MODEL

02 THE PROBLEM

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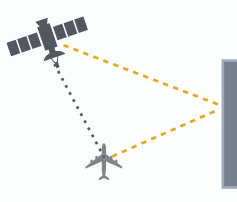
3. DEGRADATION MODEL

A bounded state degradation model

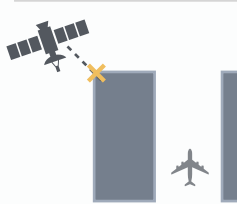
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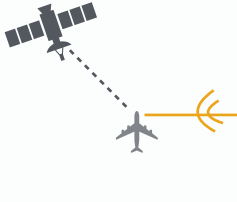
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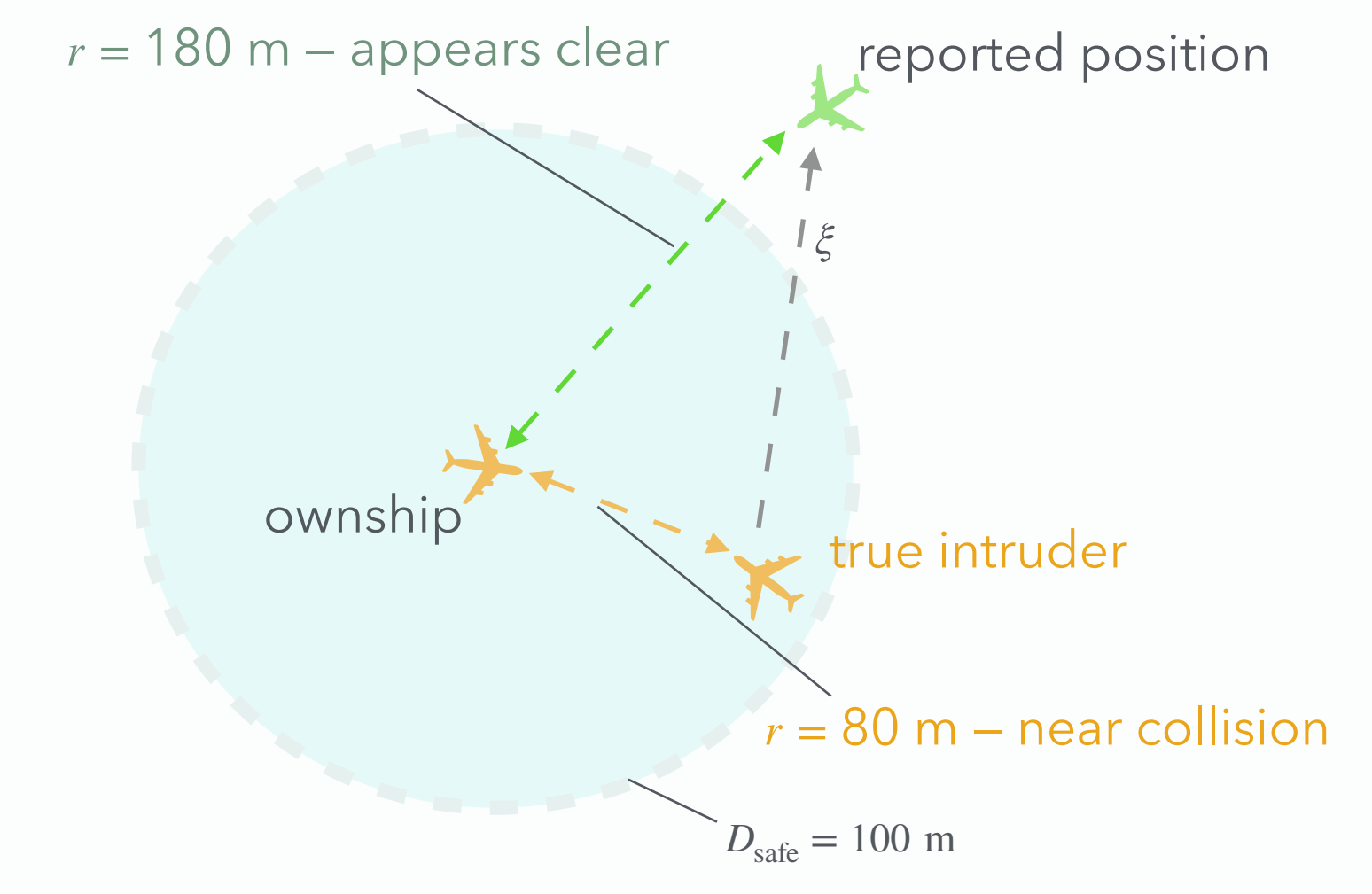
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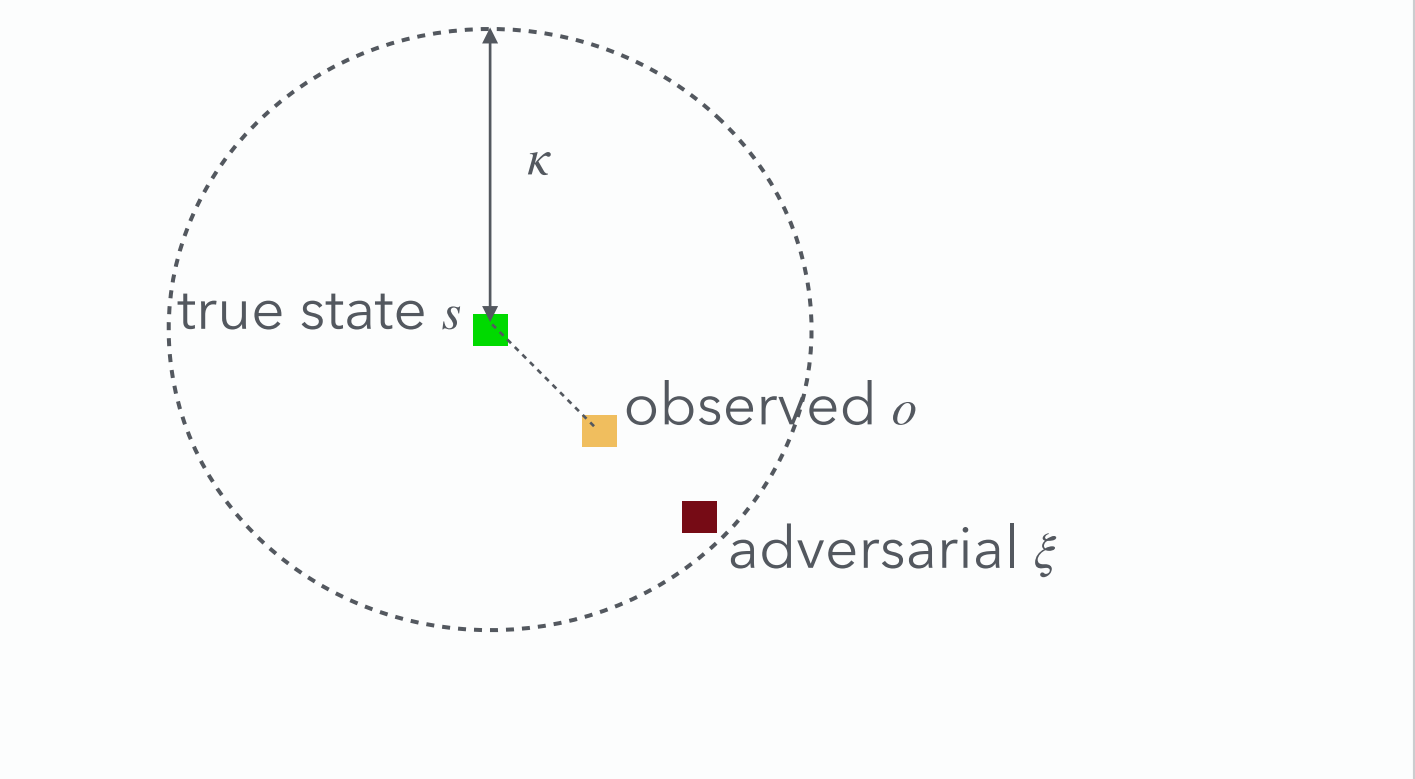
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true state s

observed o

adversarial ξ

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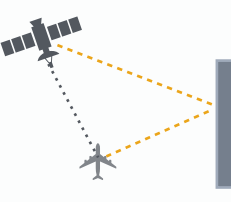
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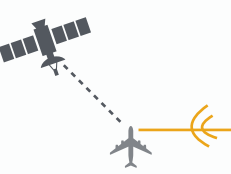
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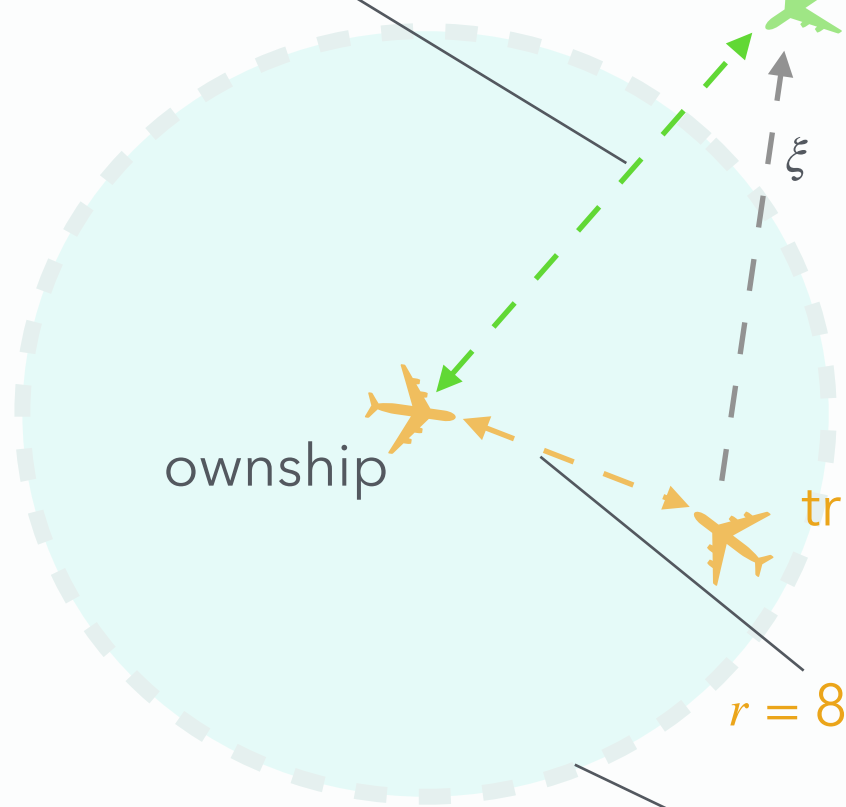
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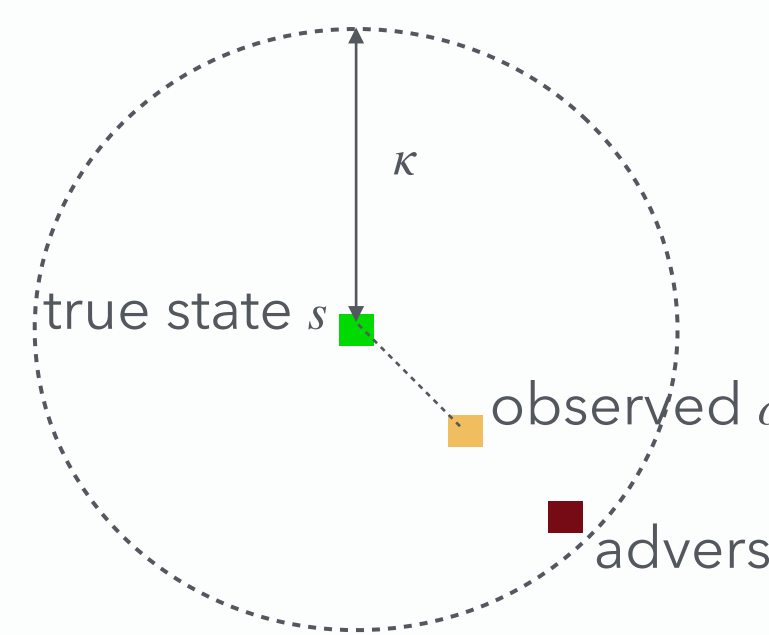
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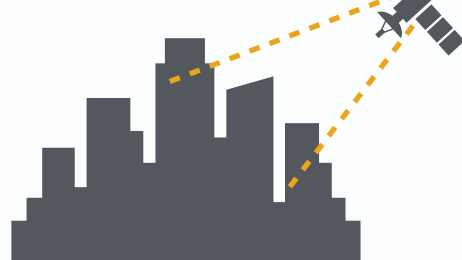
$o = (1 - R)s + R\xi$, where $\|\xi - s\|_{\infty} \leq \kappa$

Perturbation is bounded componentwise

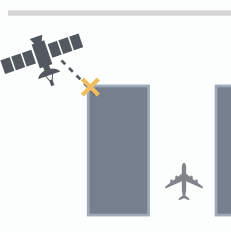
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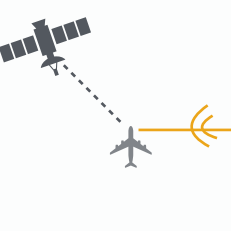
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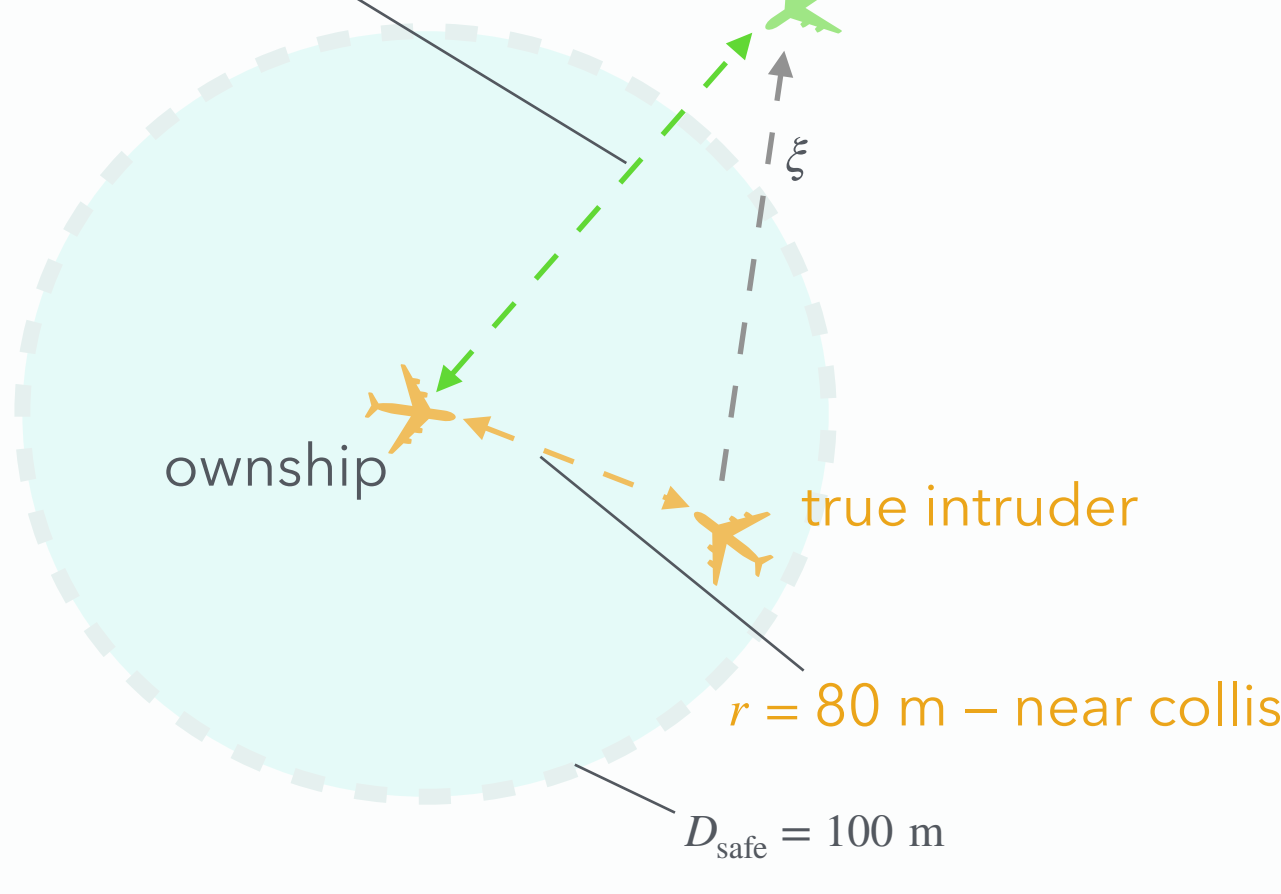
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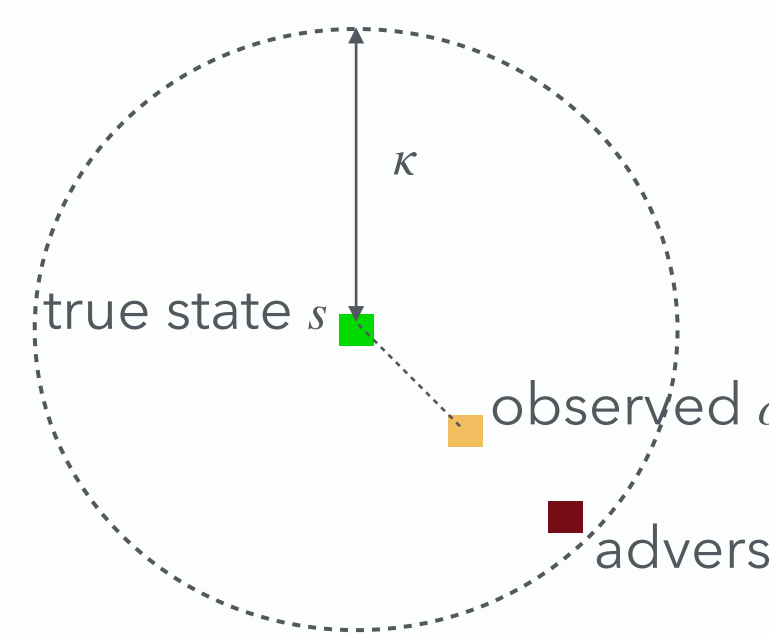
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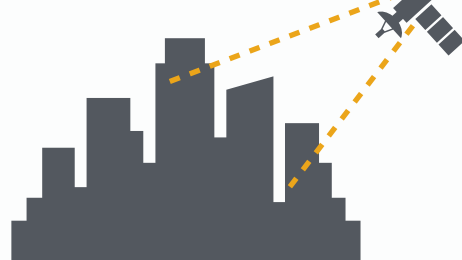
$R = 0 \cdot \text{nominal}$ $\xrightarrow{\text{orange arrow}} R \uparrow \cdot \text{degraded}$

02 THE PROBLEM

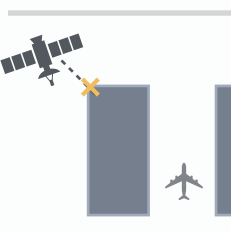
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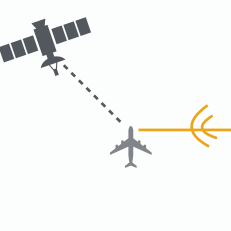
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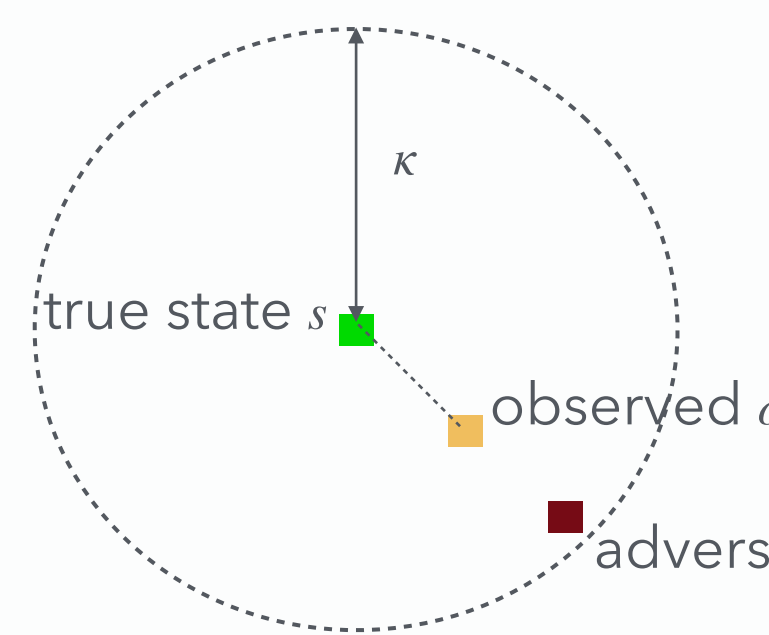
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Perturbation is bounded componentwise

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The separation policy then acts on observation o , while safety is measured on true state s .

02 THE PROBLEM

Robustness can be built in – or handled at runtime

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How should a runtime filter attach to a learned policy?

Before the policy sees the state – or after it proposes an action?

03 APPROACH

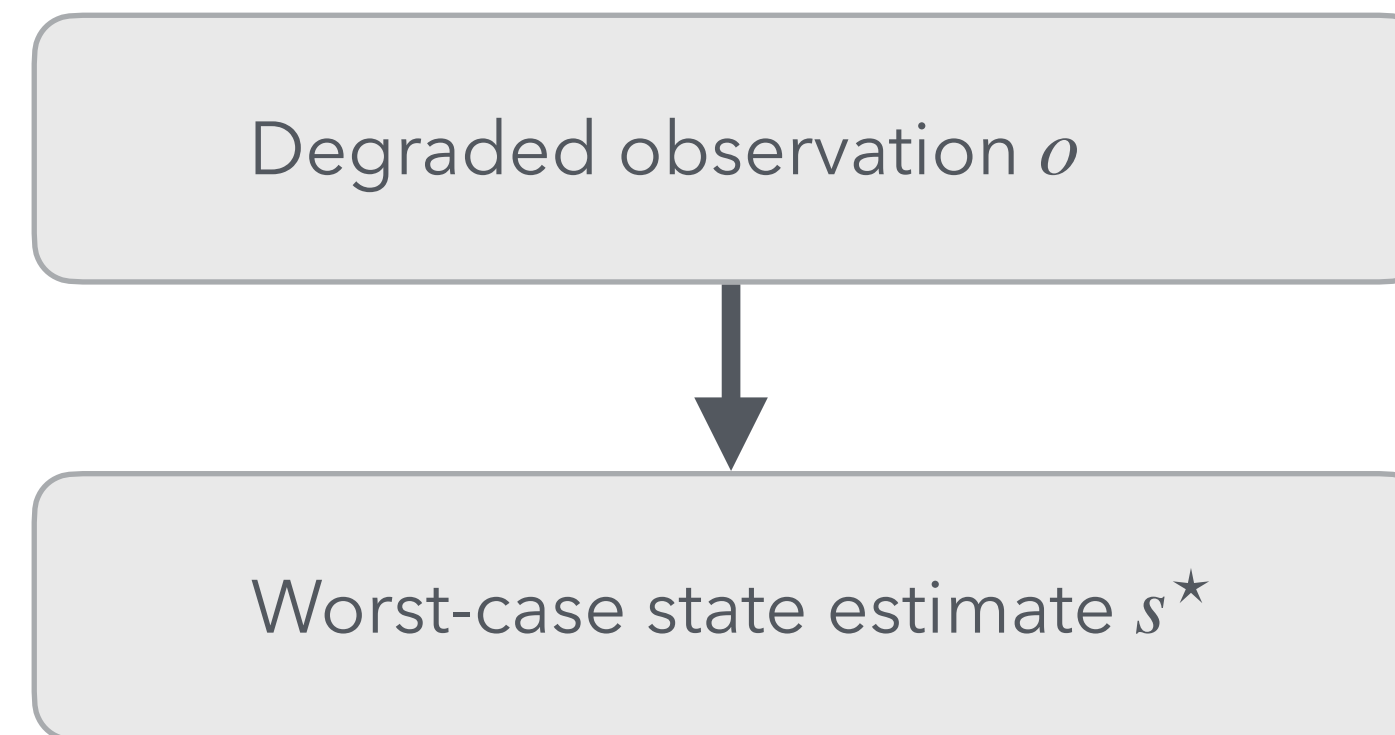
Two ways to add a runtime safety filter

03 APPROACH

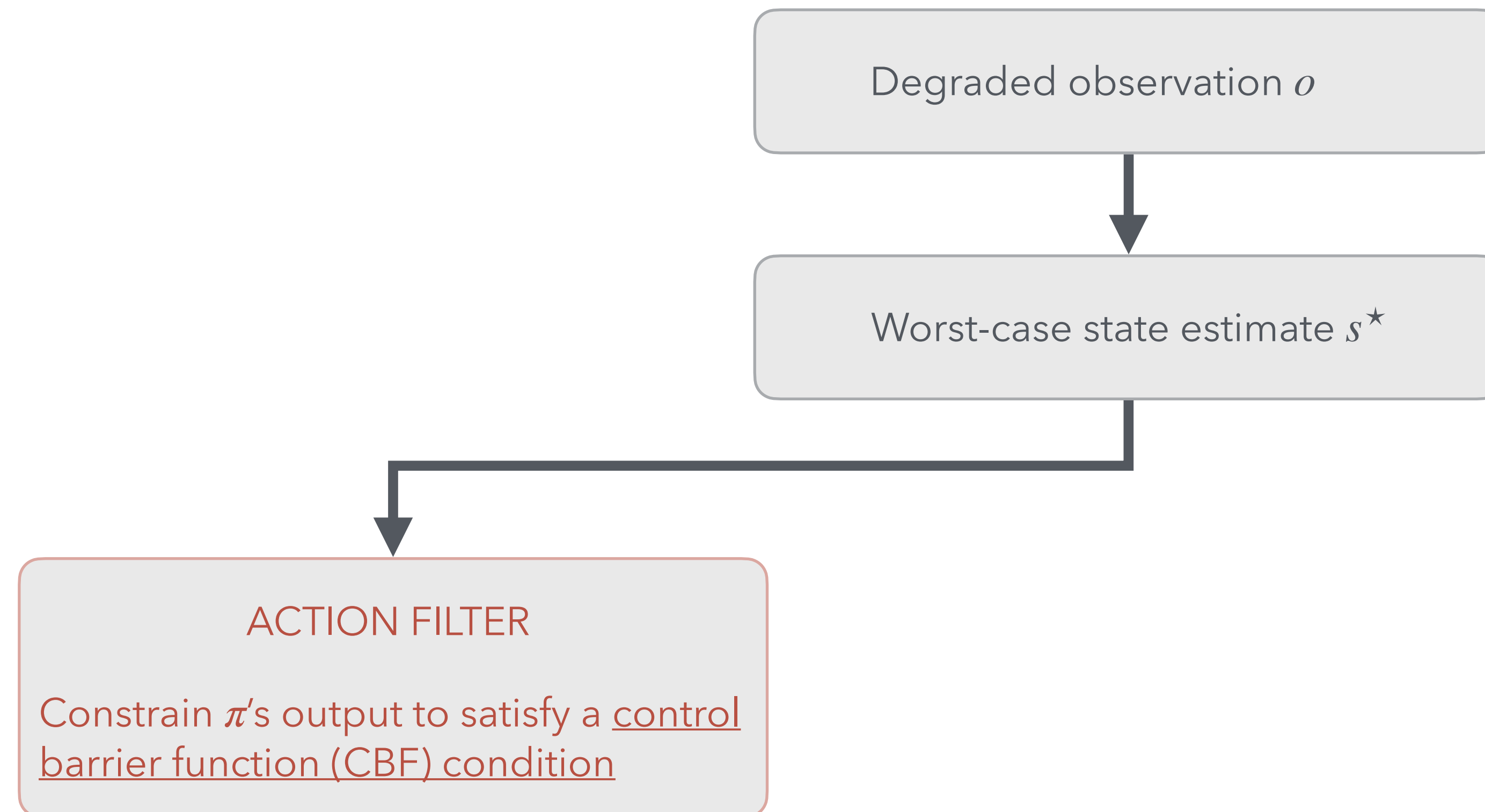
Two ways to add a runtime safety filter

Degraded observation o

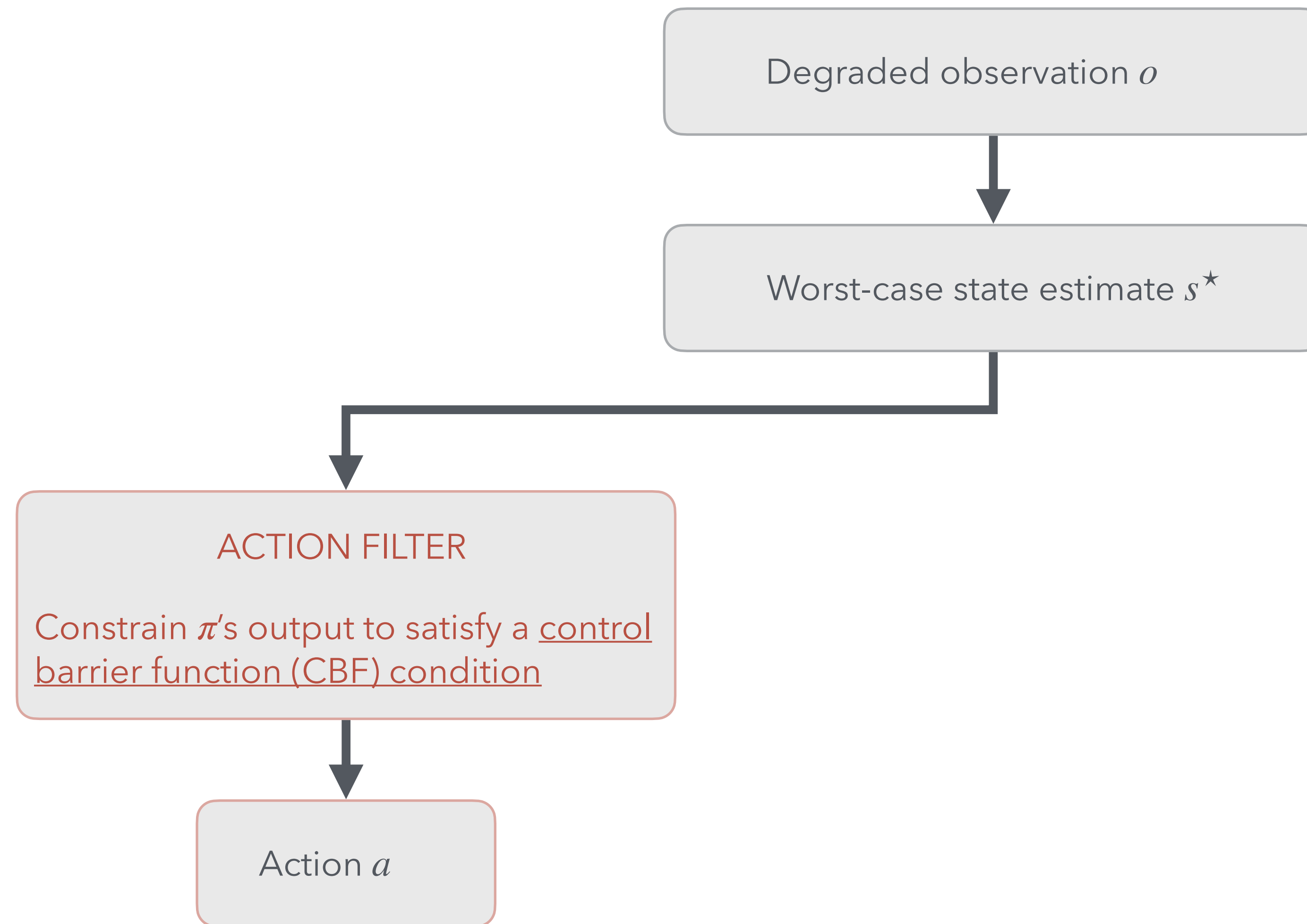
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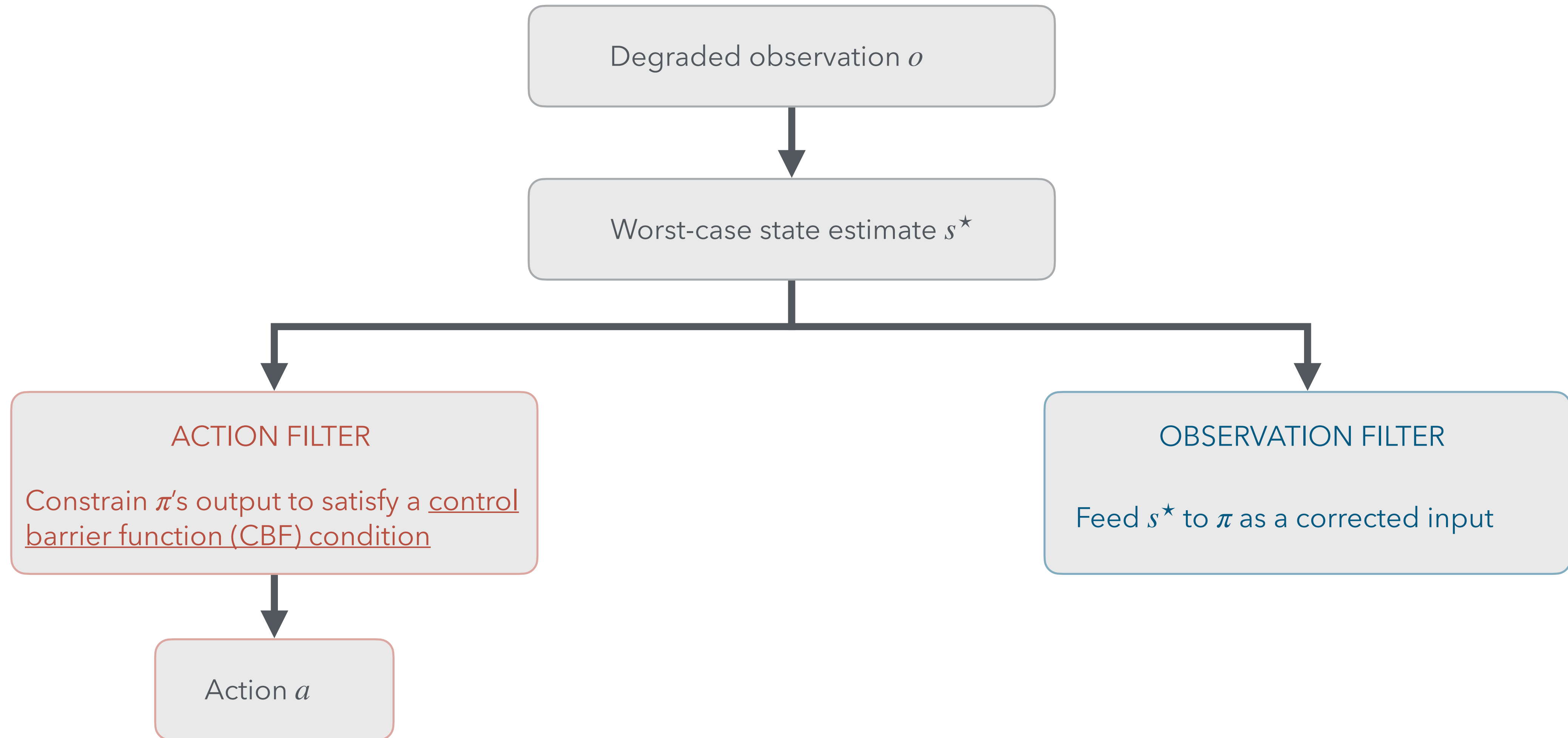
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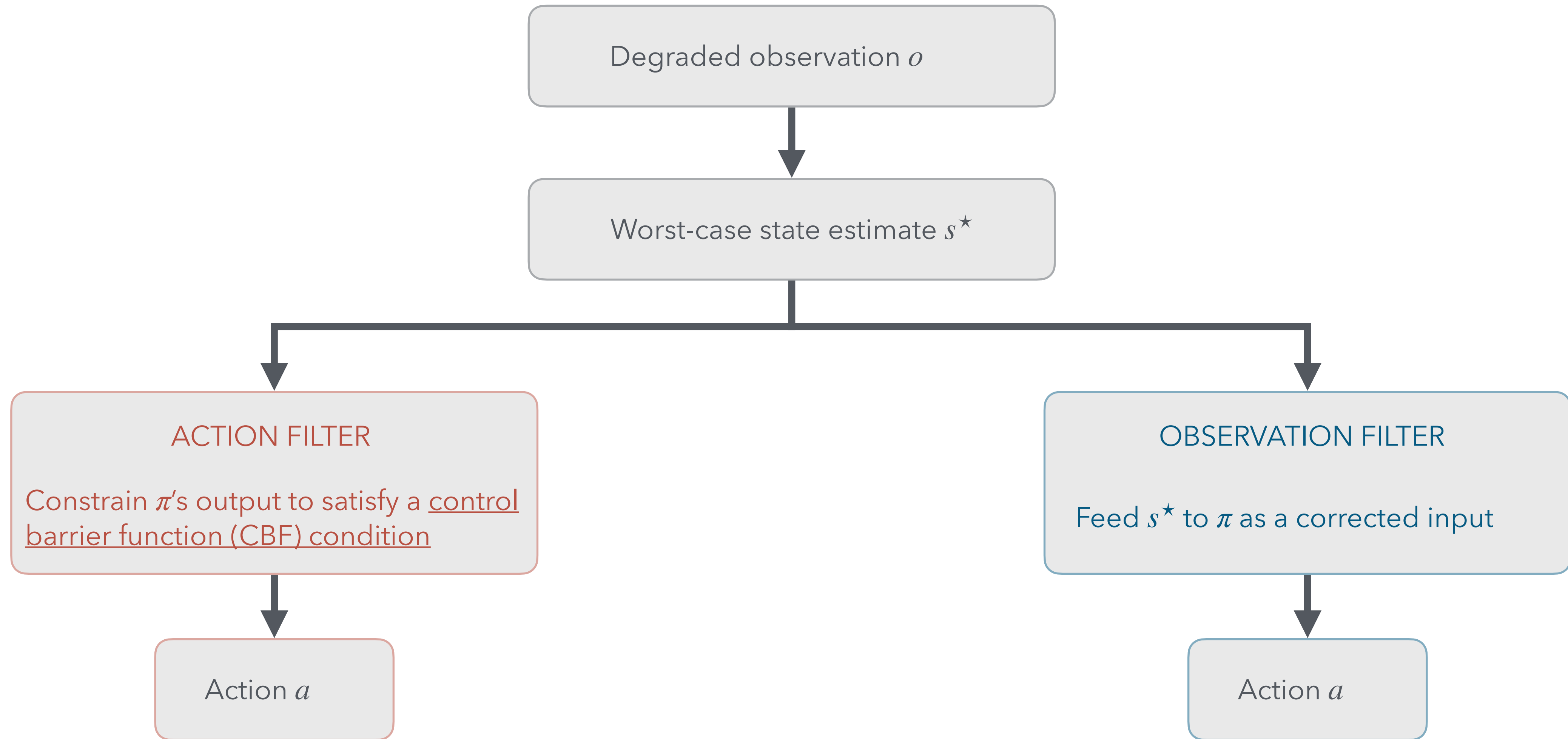
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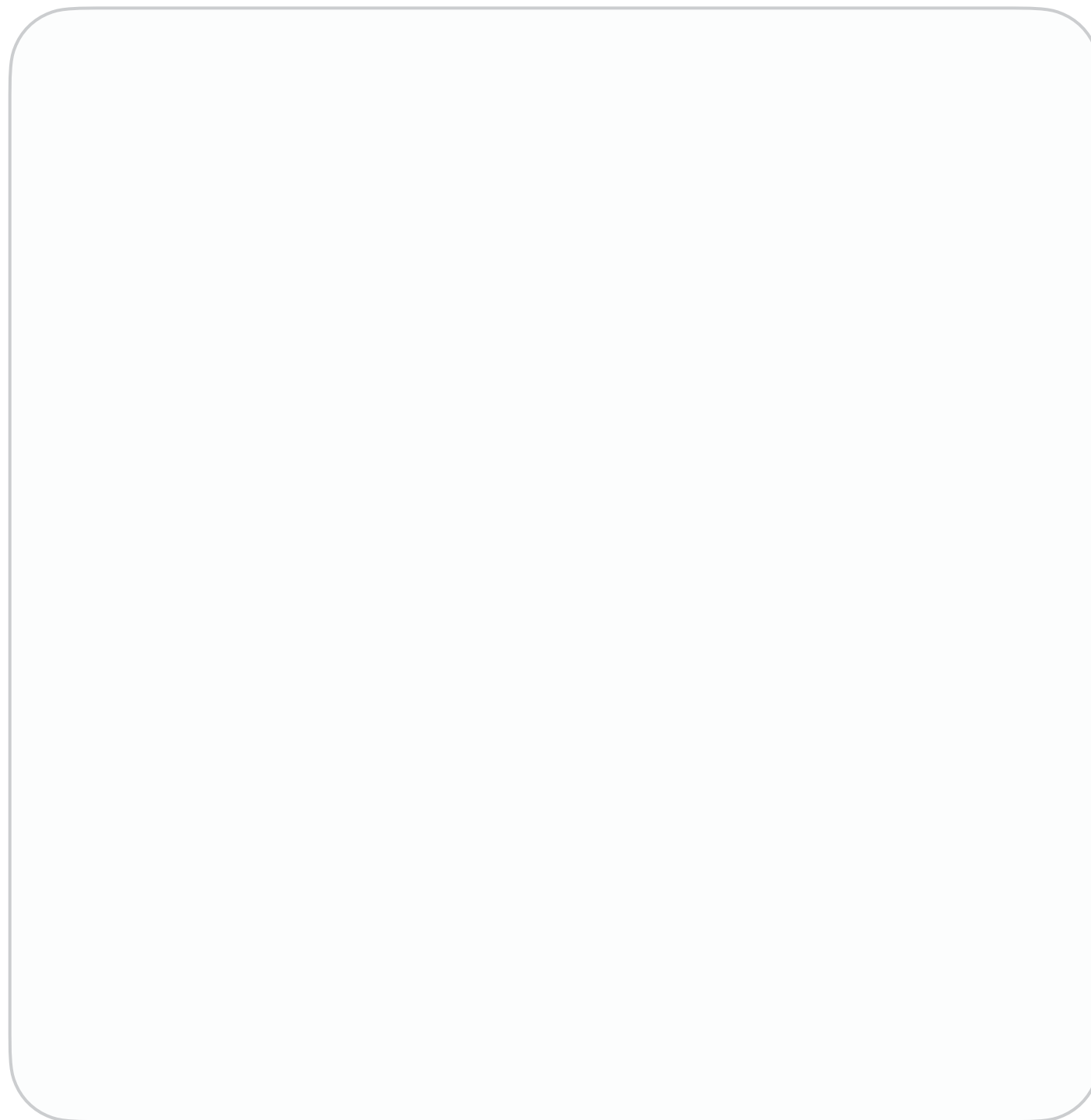


Both filters start from the same worst-case state estimation

03 APPROACH

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1. SAFETY MARGIN



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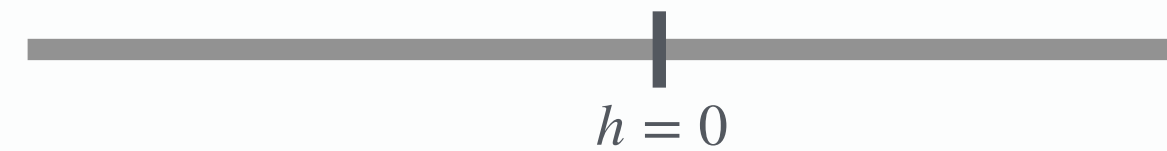
1. SAFETY MARGIN

Barrier function as safety margin

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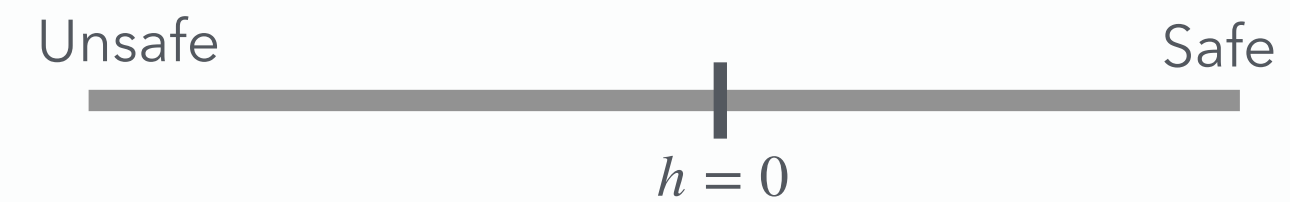


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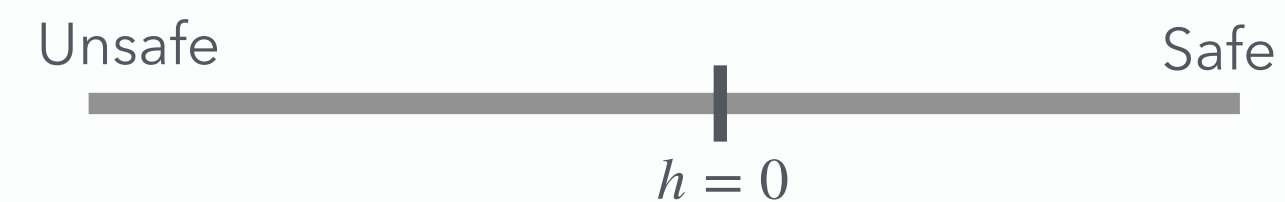
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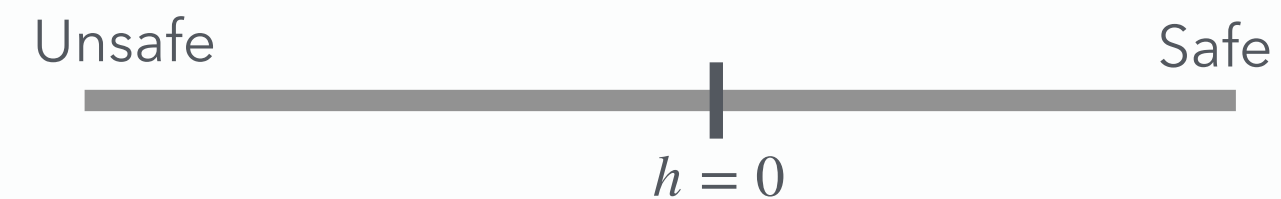
$$h(s) = (\|r\|^2 - D_{\text{safe}}^2) + \alpha \cdot r^T v_{\text{rel}}$$

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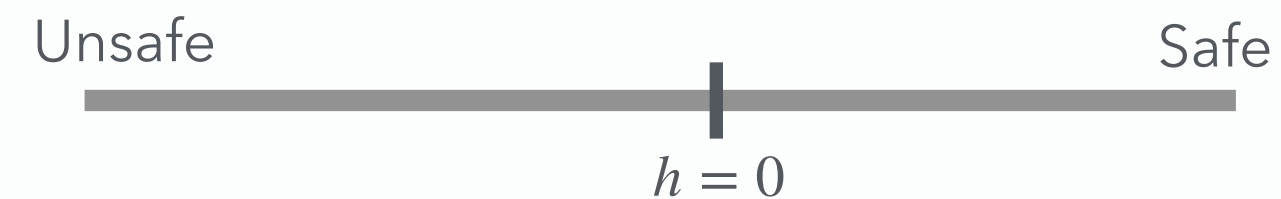
How much room there is between two UASs

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How much room there is between two UASs

$$\alpha \cdot r^T v_{\text{rel}}$$

Whether two UASs are closing in on each other
 α sets how far ahead the margin looks

03 APPROACH

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1. SAFETY MARGIN

Barrier function as safety margin

Unsafe

Unsafe

Safe

$h = 0$

 Safe

$$h(s) = (\|r\|^2 - D_{\text{safe}}^2) + \alpha \cdot r^T v_{\text{rel}}$$

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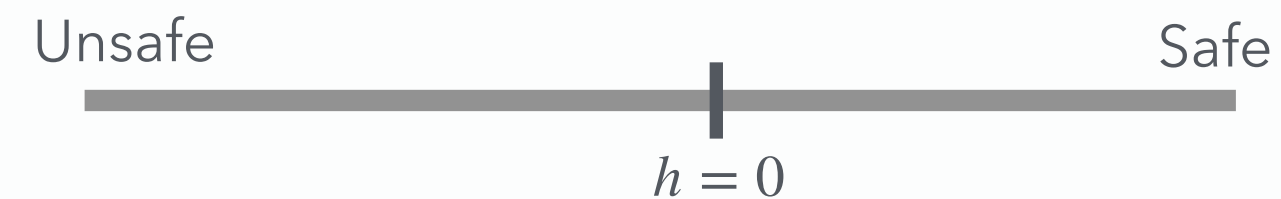
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Current observation

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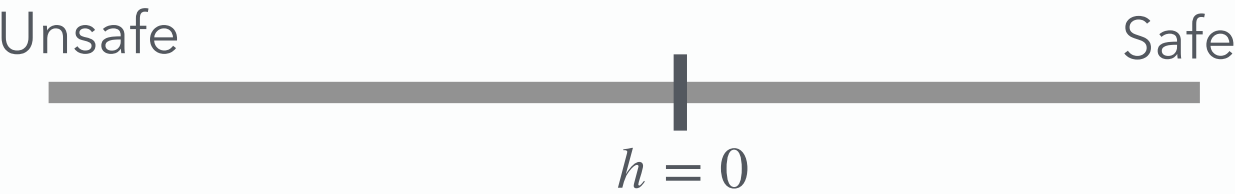
ownship

180 m – appears clear

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Barrier function as safety margin



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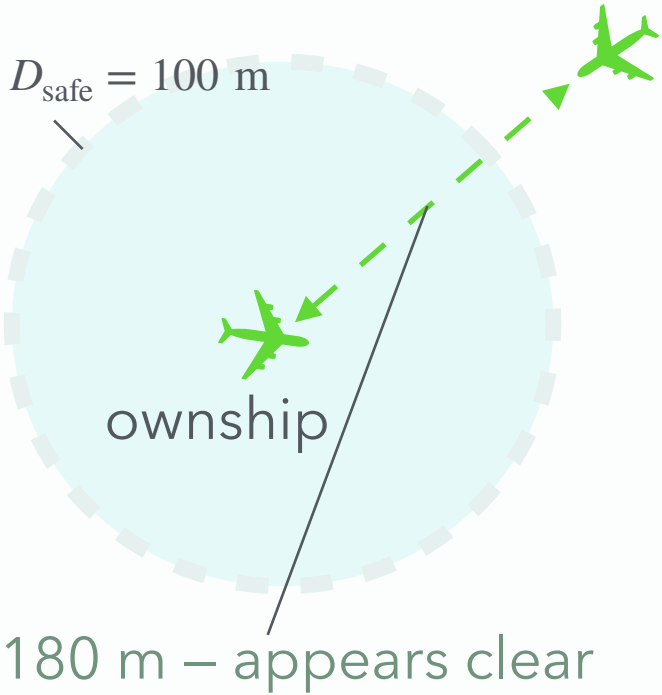
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Current observation



$$s^* = \arg \min_{s \in \mathcal{U}(o, R_{\text{max}})} h(s)$$

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Current observation Worst-case view

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ownship

96 m – WORST CASE

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3. IN CLOSED FORM

A closed-form displacement

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3. IN CLOSED FORM

A closed-form displacement

$\mathcal{U}(o, R) = \{s : \|s - o\|_{\infty} \leq R\kappa\}, \quad \delta \triangleq R\kappa$

observed o

true state s

$R\kappa$

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Recall $o = (1 - R)s + R\xi$,
where $\|\xi - s\|_{\infty} \leq \kappa$

Both filters start from the same worst-case state estimation

1. SAFETY MARGIN

Barrier function as safety margin

Unsafe Safe

$h = 0$

$$h(s) = (\|r\|^2 - D_{\text{safe}}^2) + \alpha \cdot r^T v_{\text{rel}}$$

$\|r\|^2 - D_{\text{safe}}^2$
How much room there is between two UASs

$\alpha \cdot r^T v_{\text{rel}}$
Whether two UASs are closing in on each other
 α sets how far ahead the margin looks

2. WORST CASE

What looked clear now reads as a conflict

Current observation Worst-case view

$D_{\text{safe}} = 100 \text{ m}$

ownship

180 m – appears clear

ownship

96 m – WORST CASE

$$s^* = \arg \min_{s \in \mathcal{U}(o, R_{\text{max}})} h(s)$$

3. IN CLOSED FORM

A closed-form displacement

$\mathcal{U}(o, R) = \{s : \|s - o\|_{\infty} \leq R\delta\}, \quad \delta \triangleq R\kappa$

observed o

true state s

Recall $o = (1 - R)s + R\xi$,
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$R = 0 \cdot \text{nominal}$ $R \uparrow \cdot \text{degraded}$

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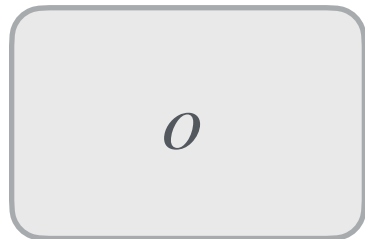
Both filters compute s^* from the same safety margin h . However, only the action filter lets h veto the policy.

03 APPROACH

The filtering approaches differ in what happens next

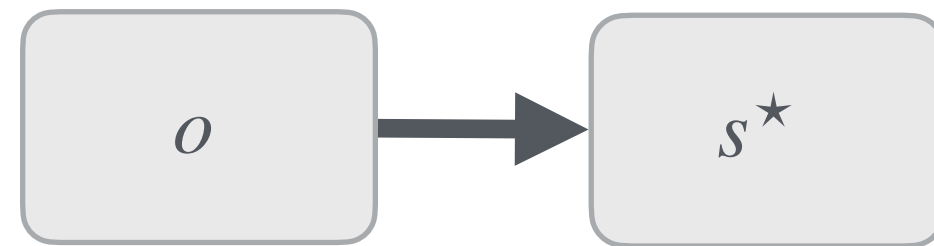
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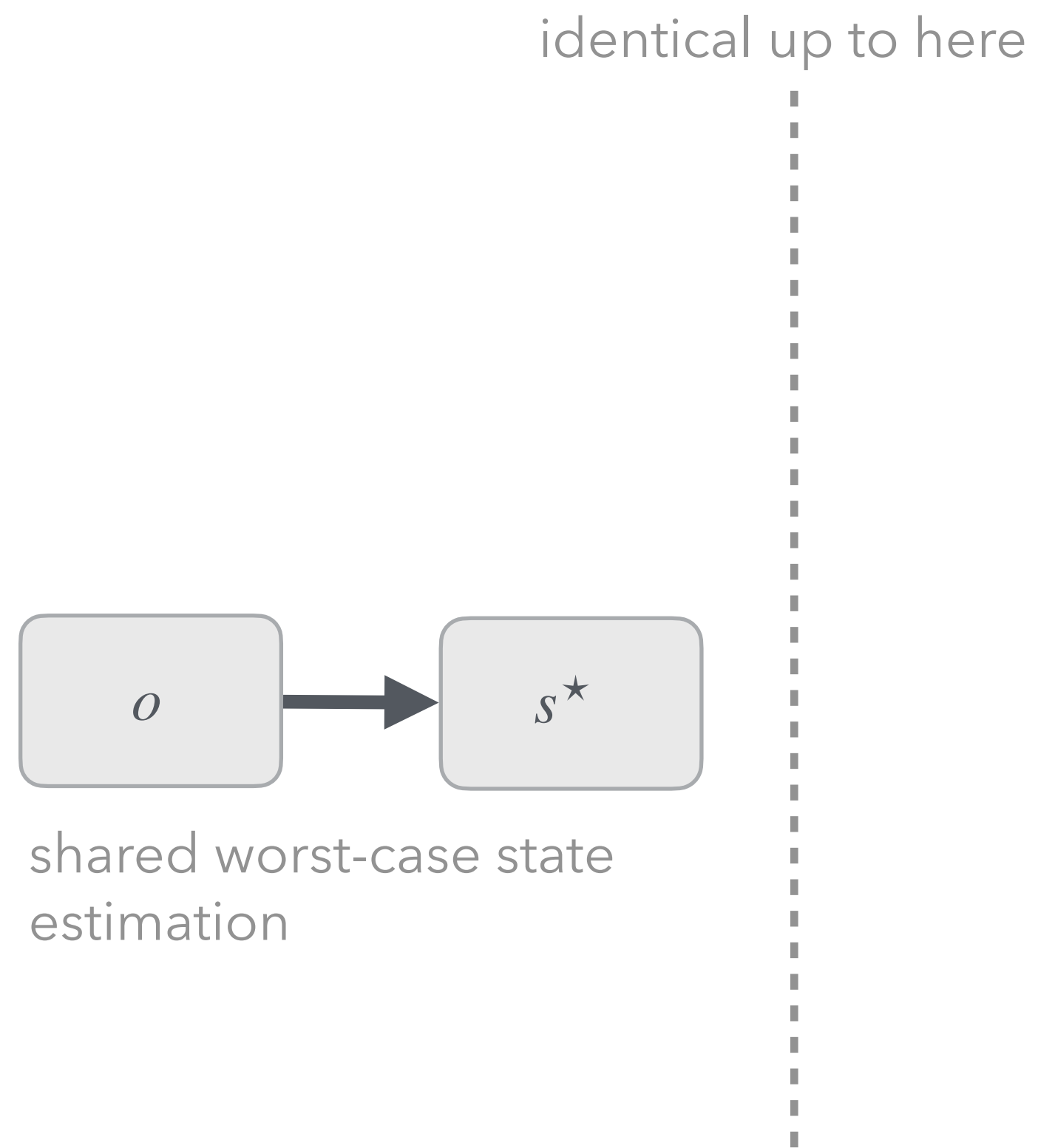
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shared worst-case state
estimation

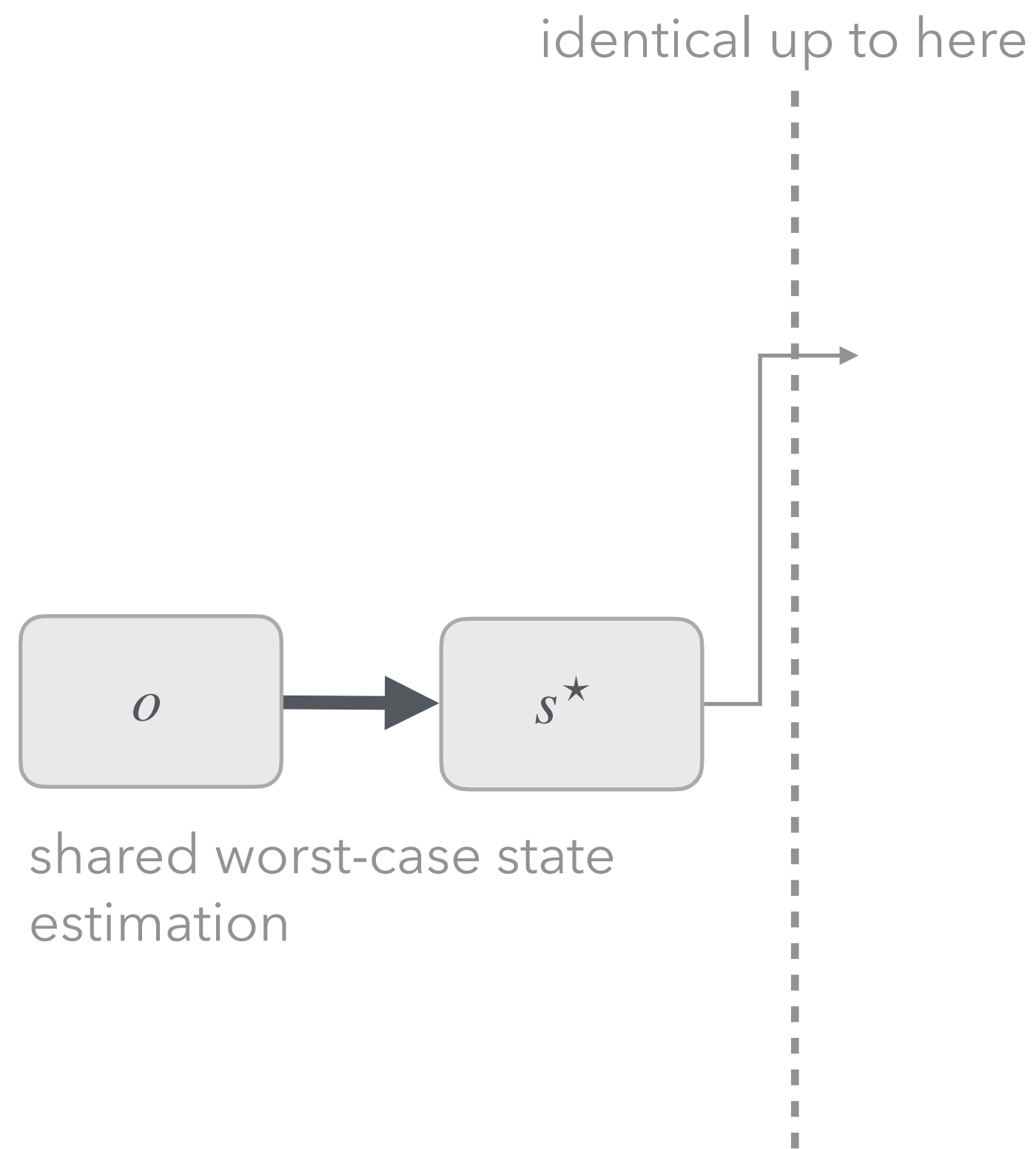
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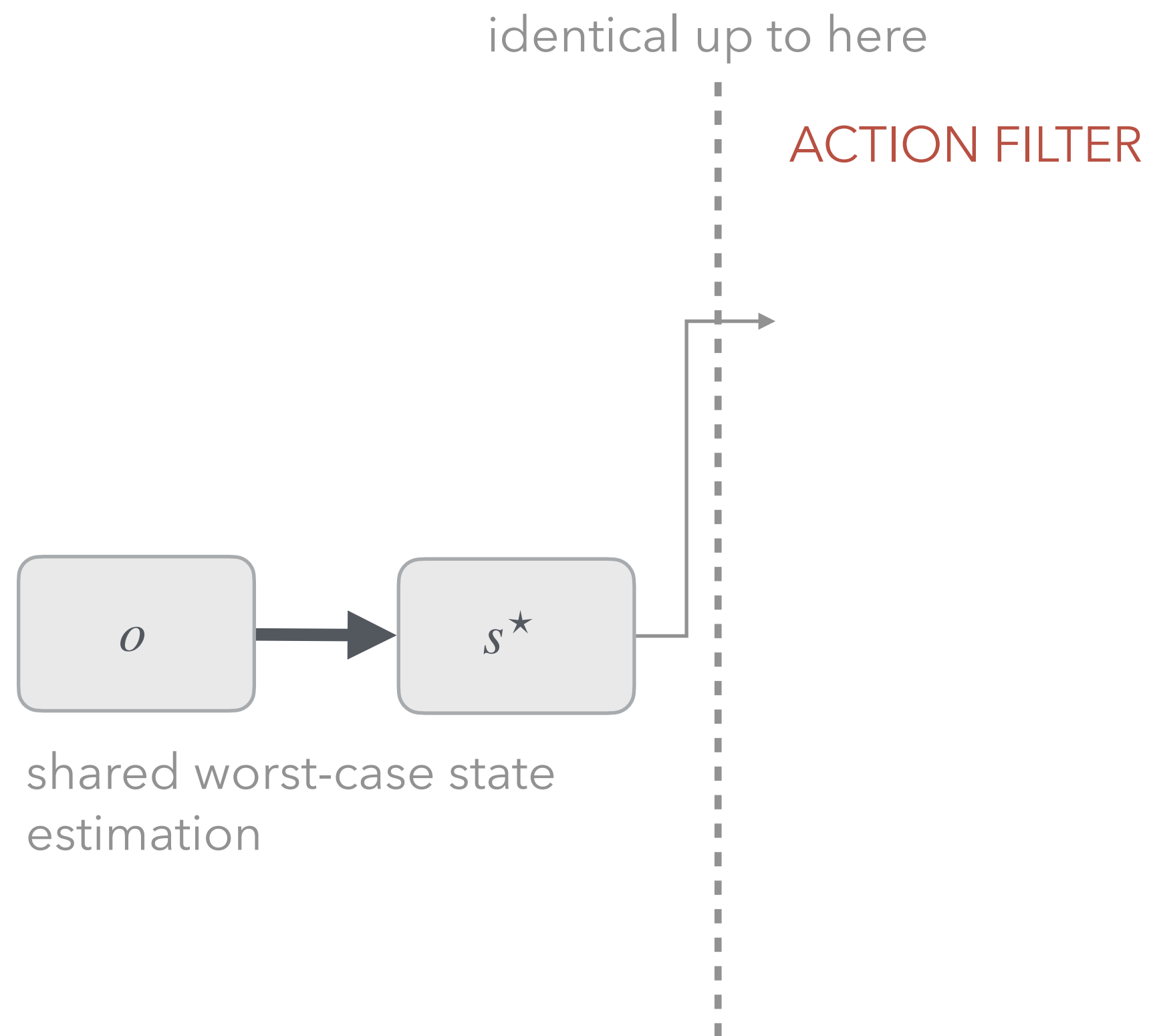
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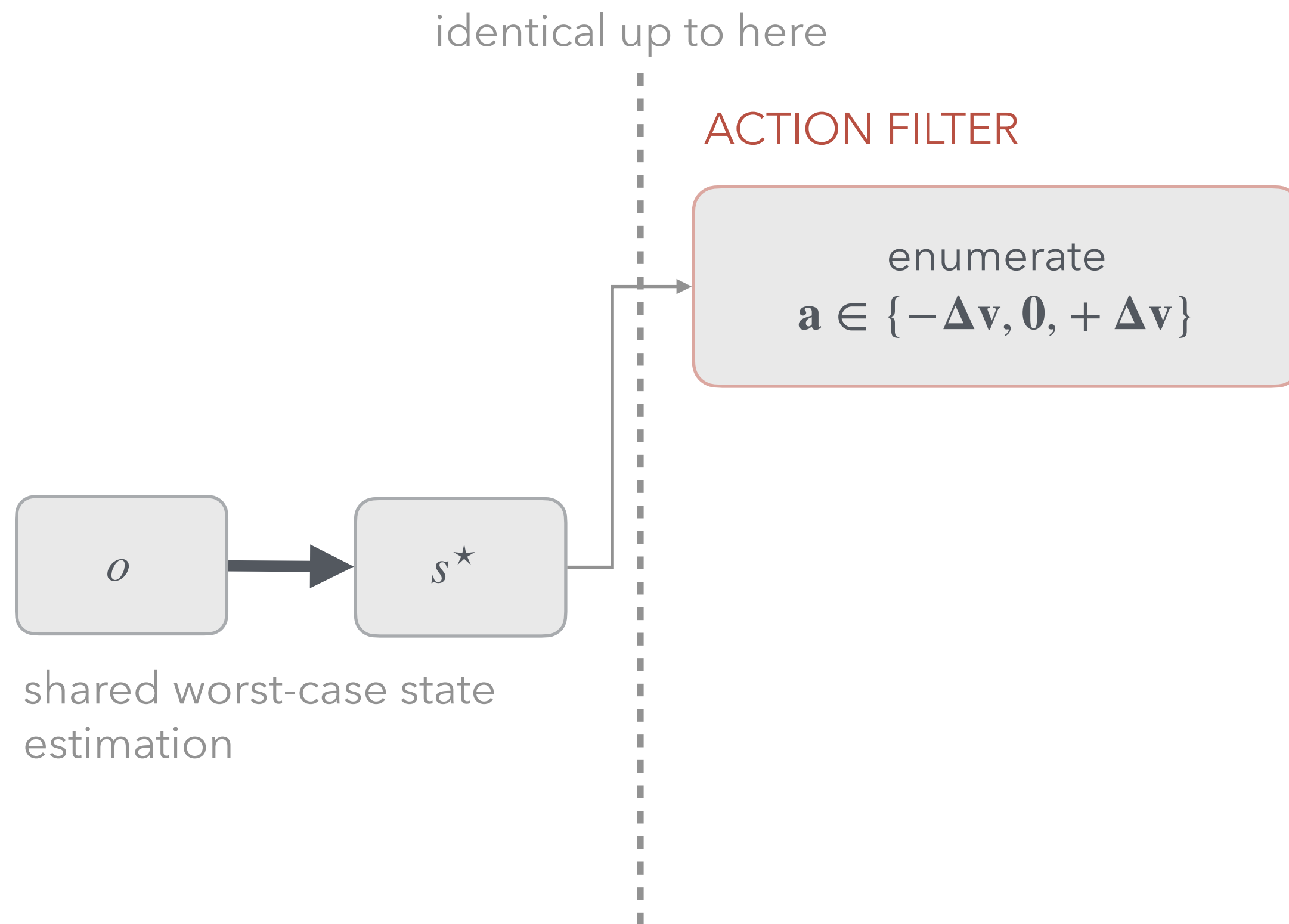
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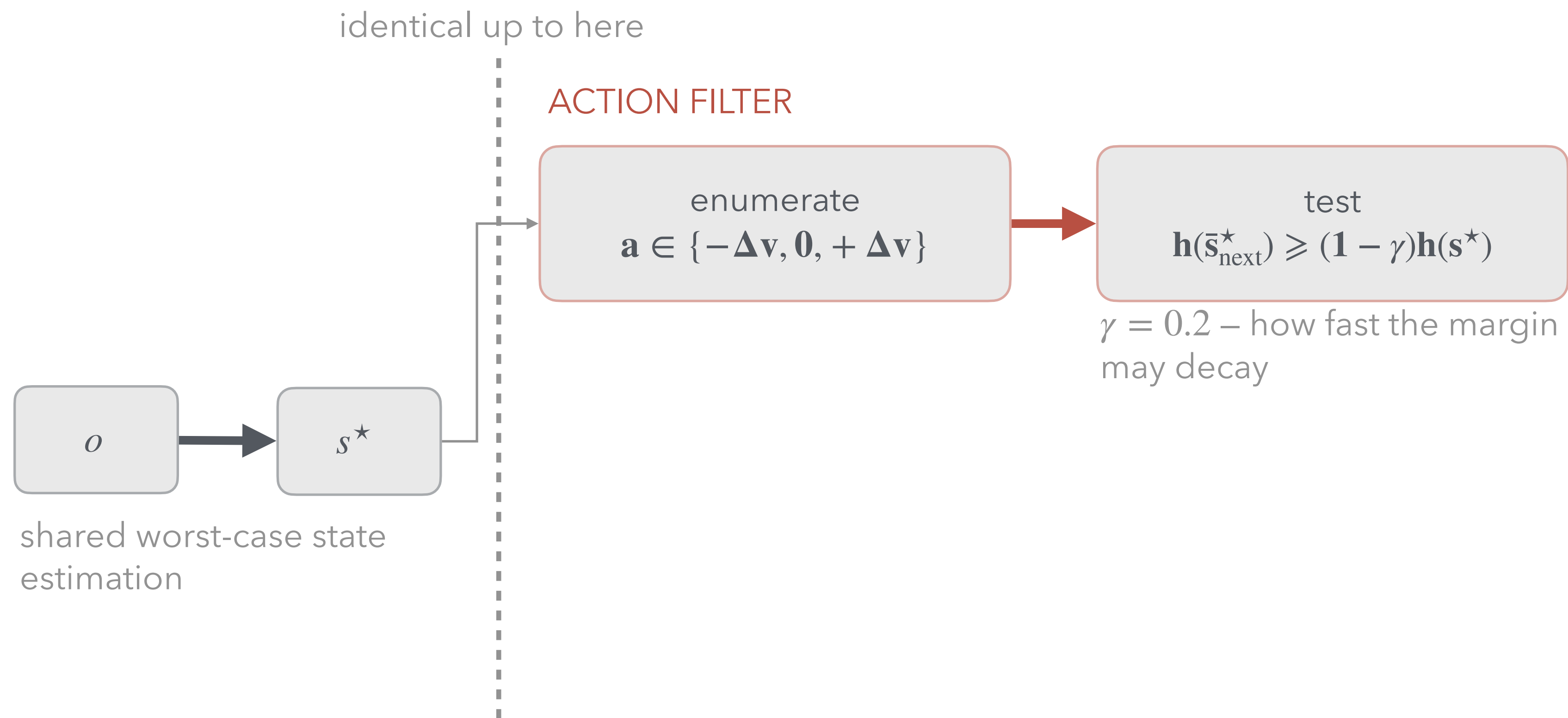
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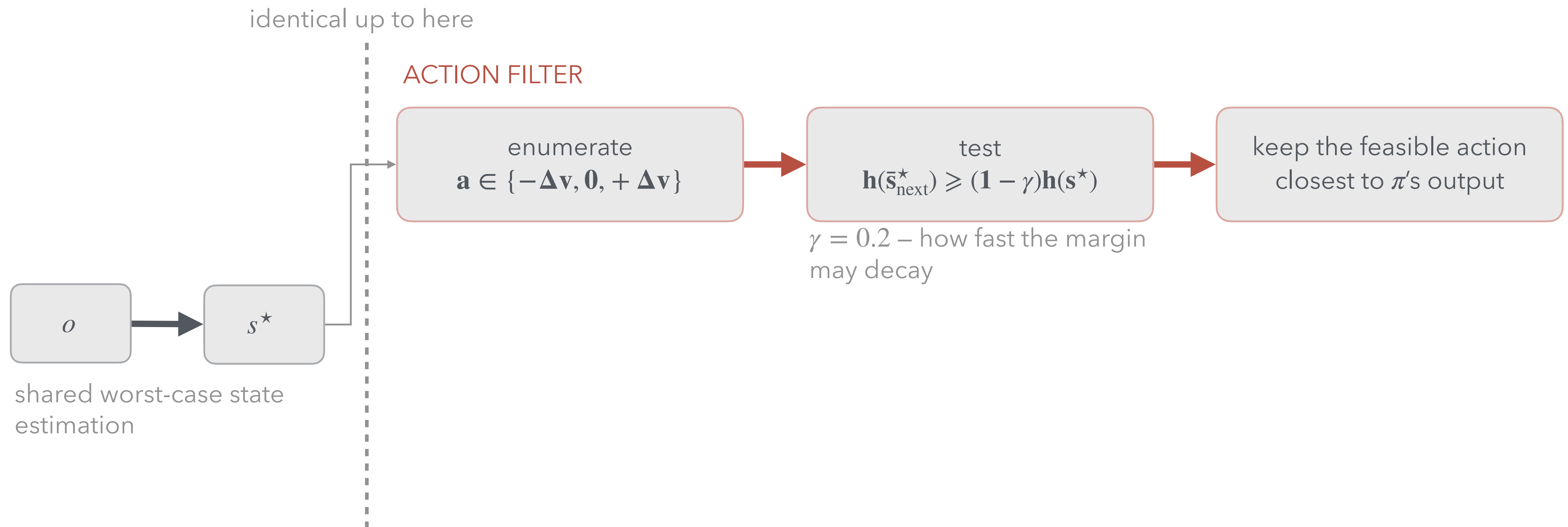


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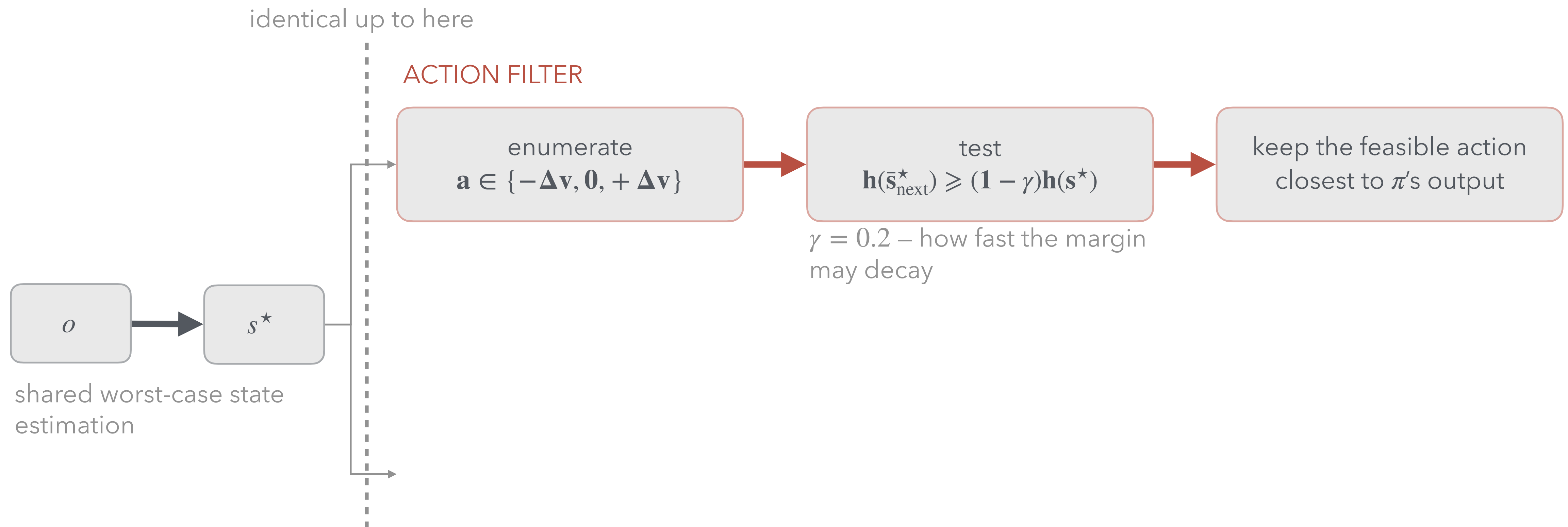
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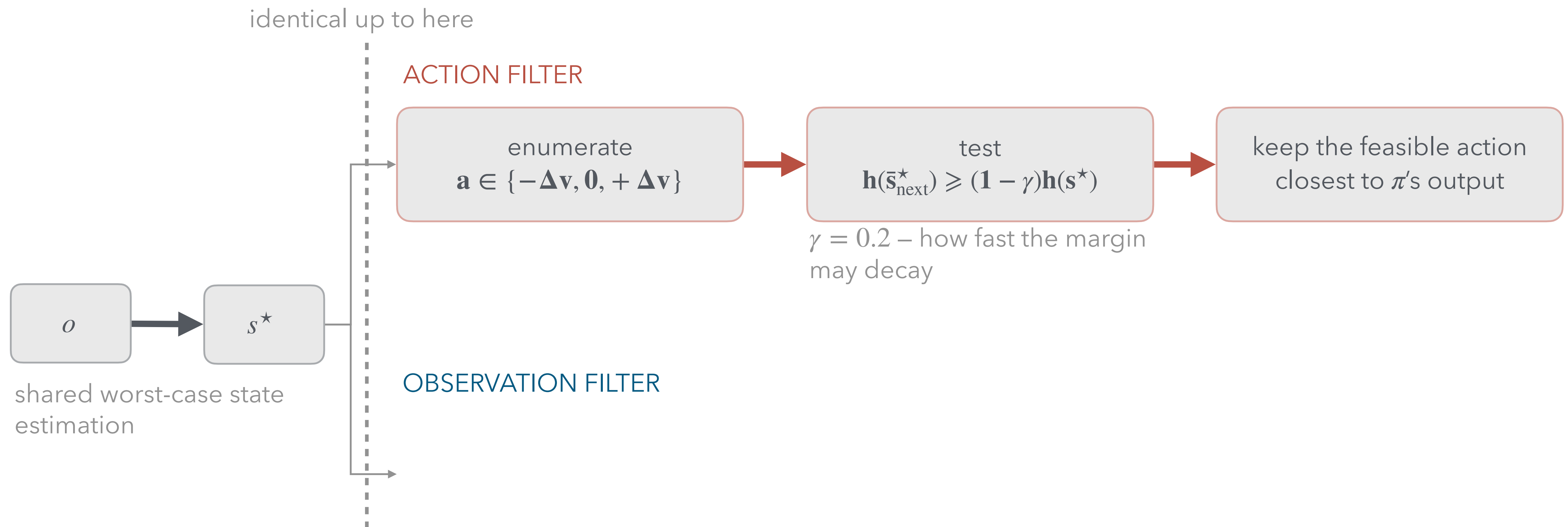


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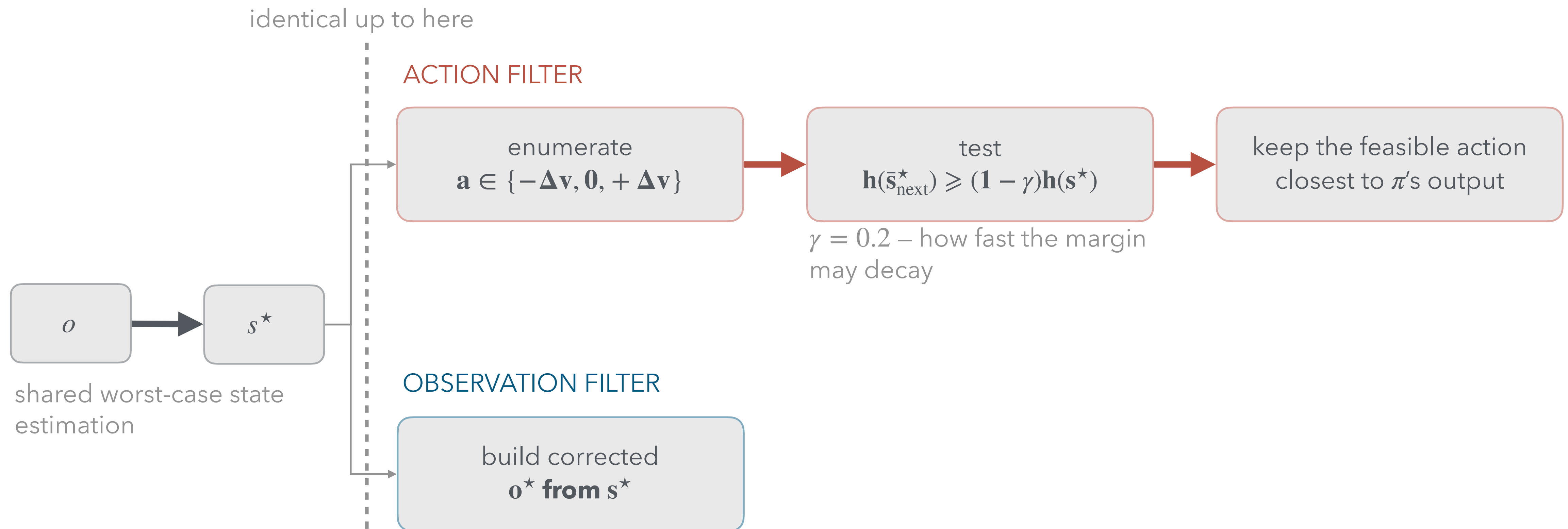
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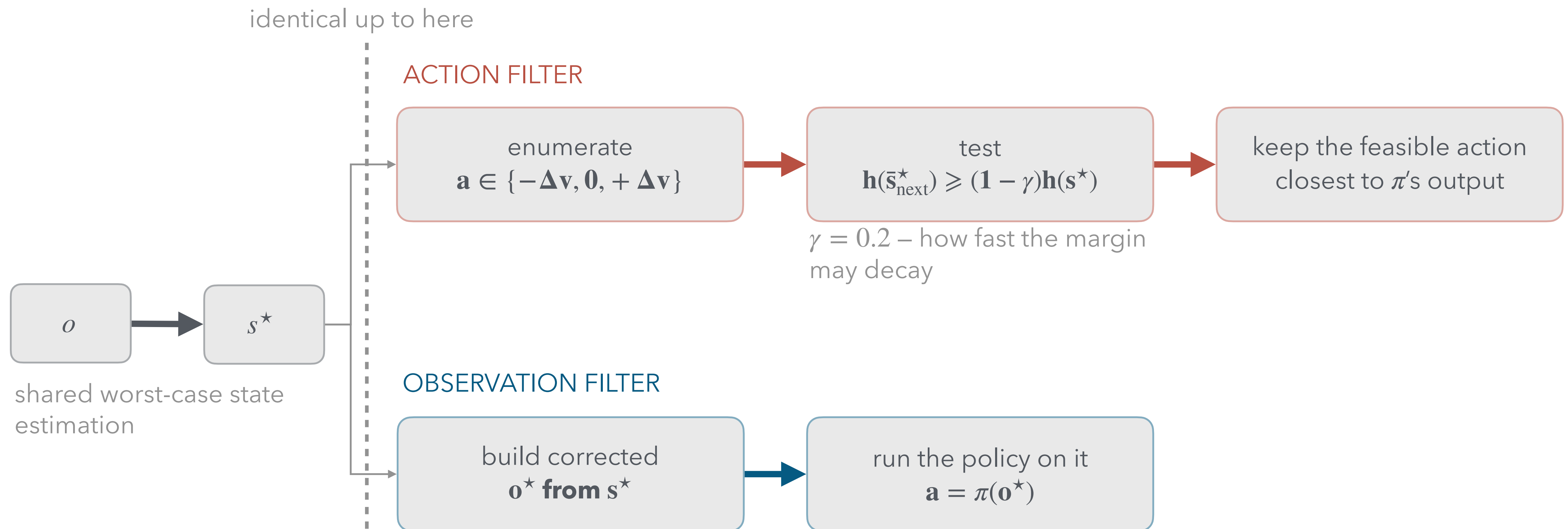
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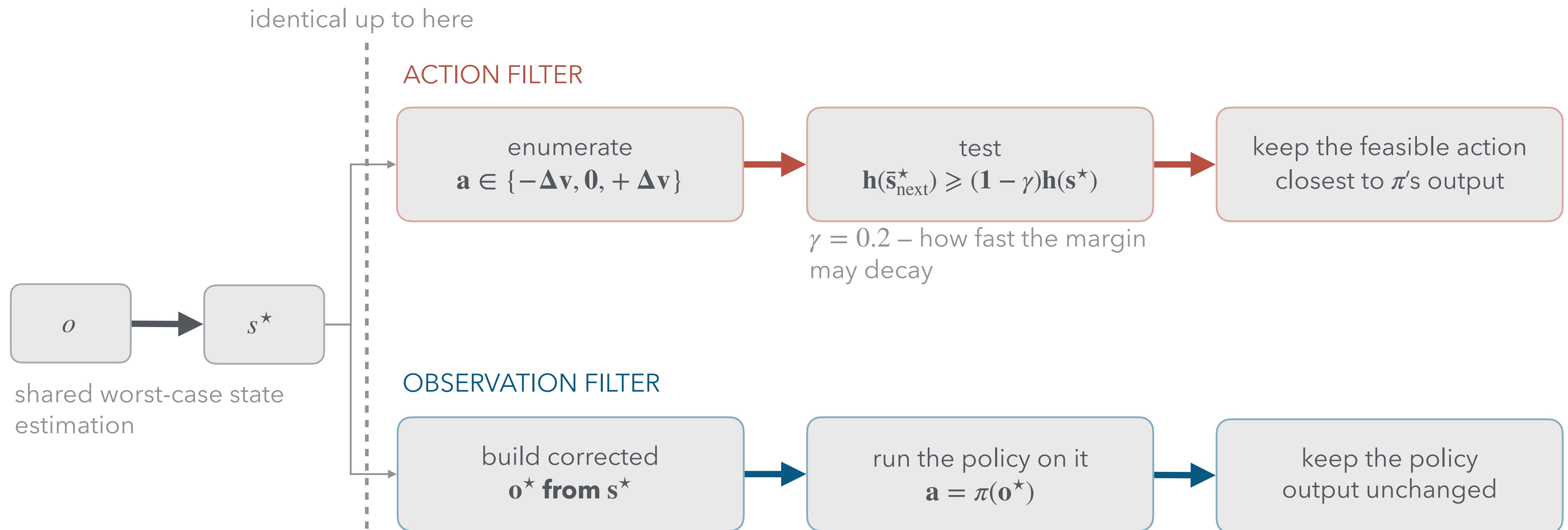
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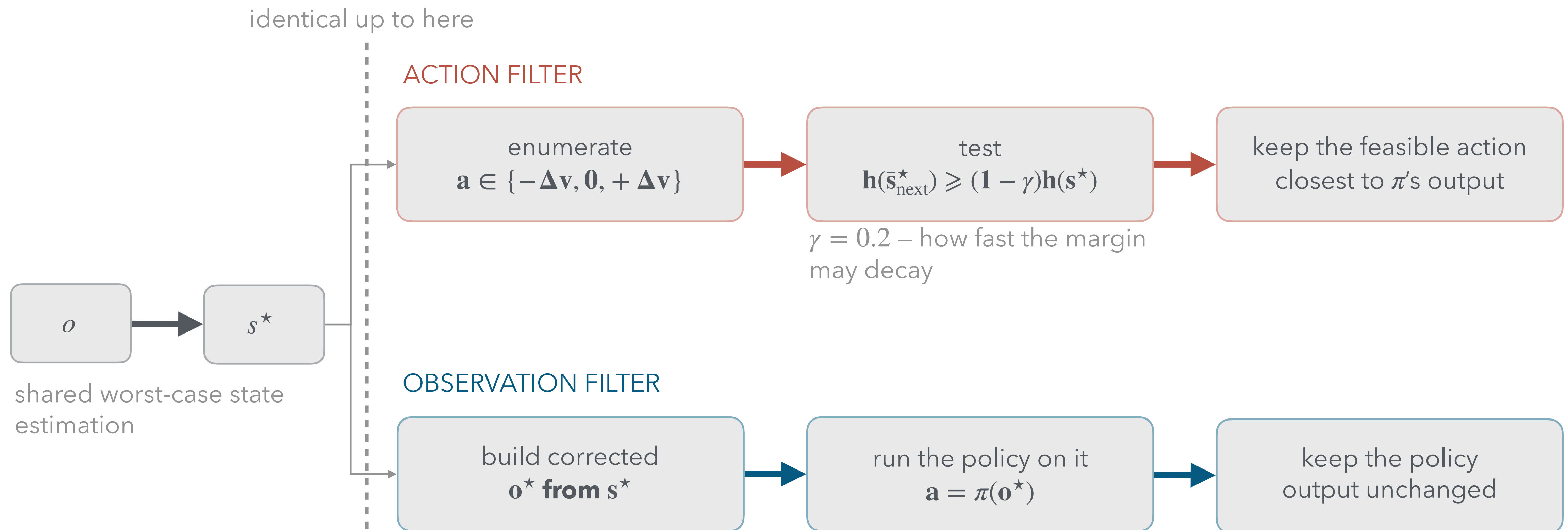
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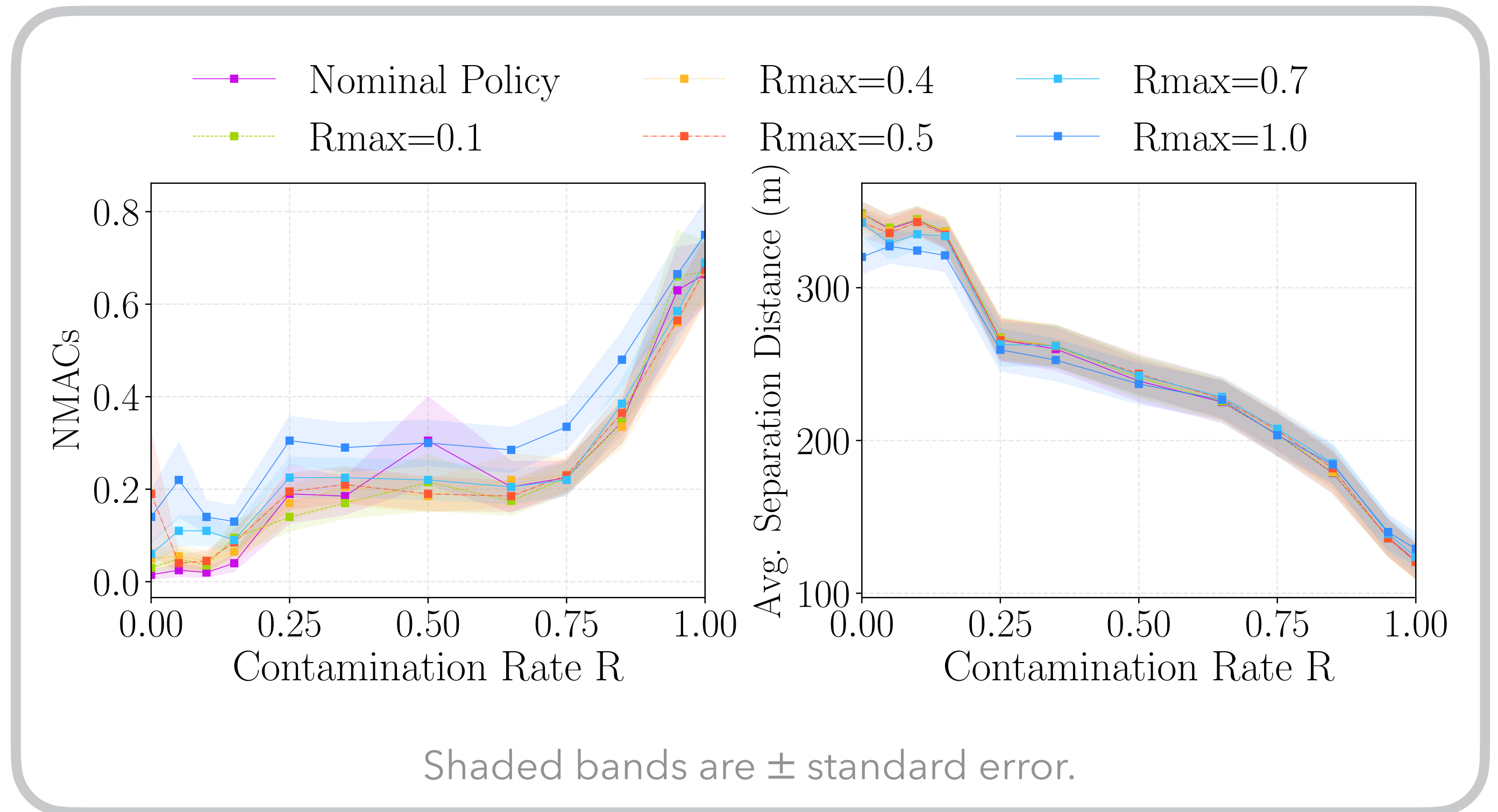


Same estimate, different use. The discrete-time CBF condition applies only to the action filtering.

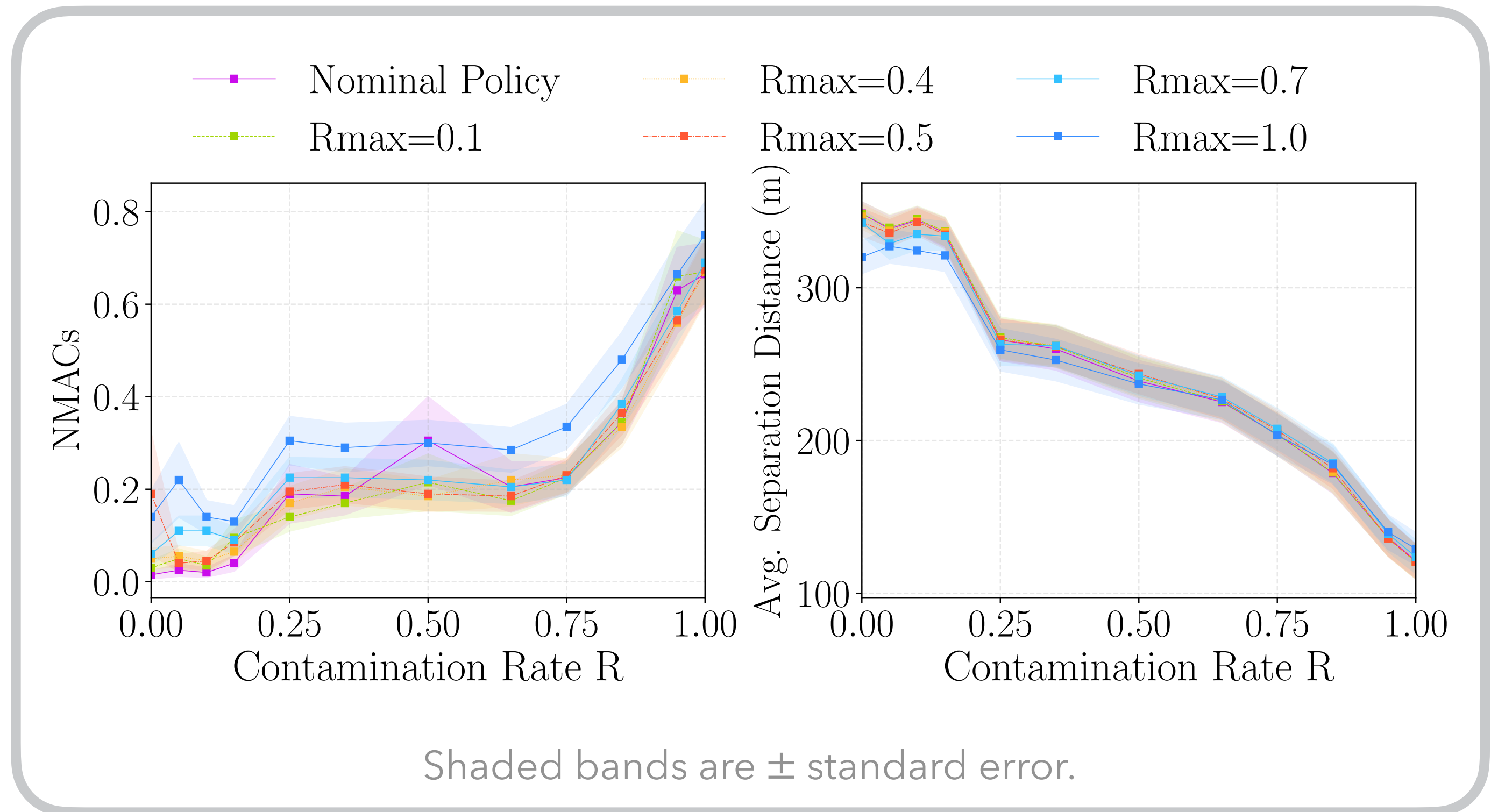
04 RESULTS

Action filtering barely moves the safety needle

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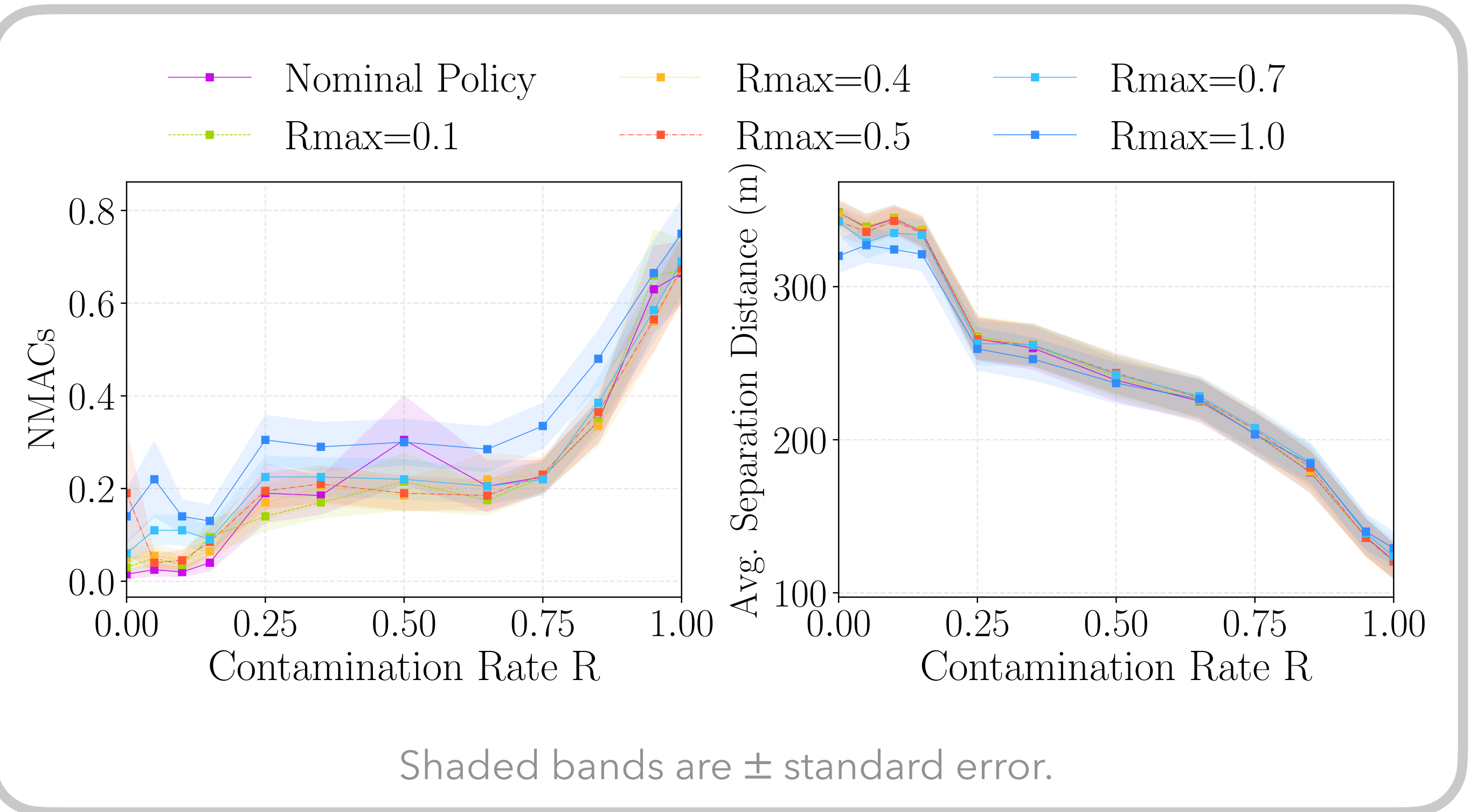


04 RESULTS

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NMAC

Near mid-air collision when two aircraft pass within $D_{\text{safe}} = 100$ m; counted per episode.



04 RESULTS

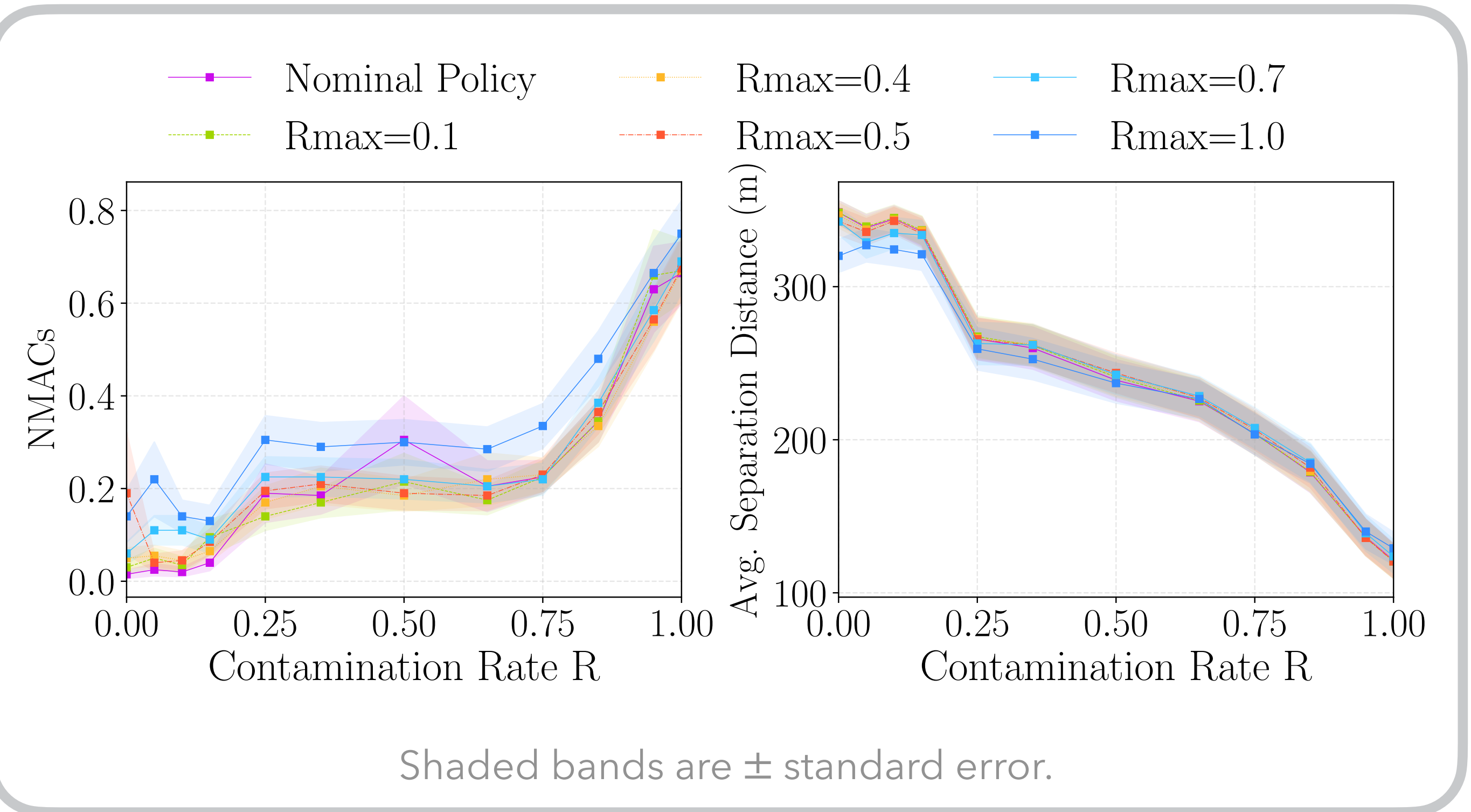
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Contamination rate: how degraded GNSS actually is. 0 is nominal; 1 is fully adversarial.



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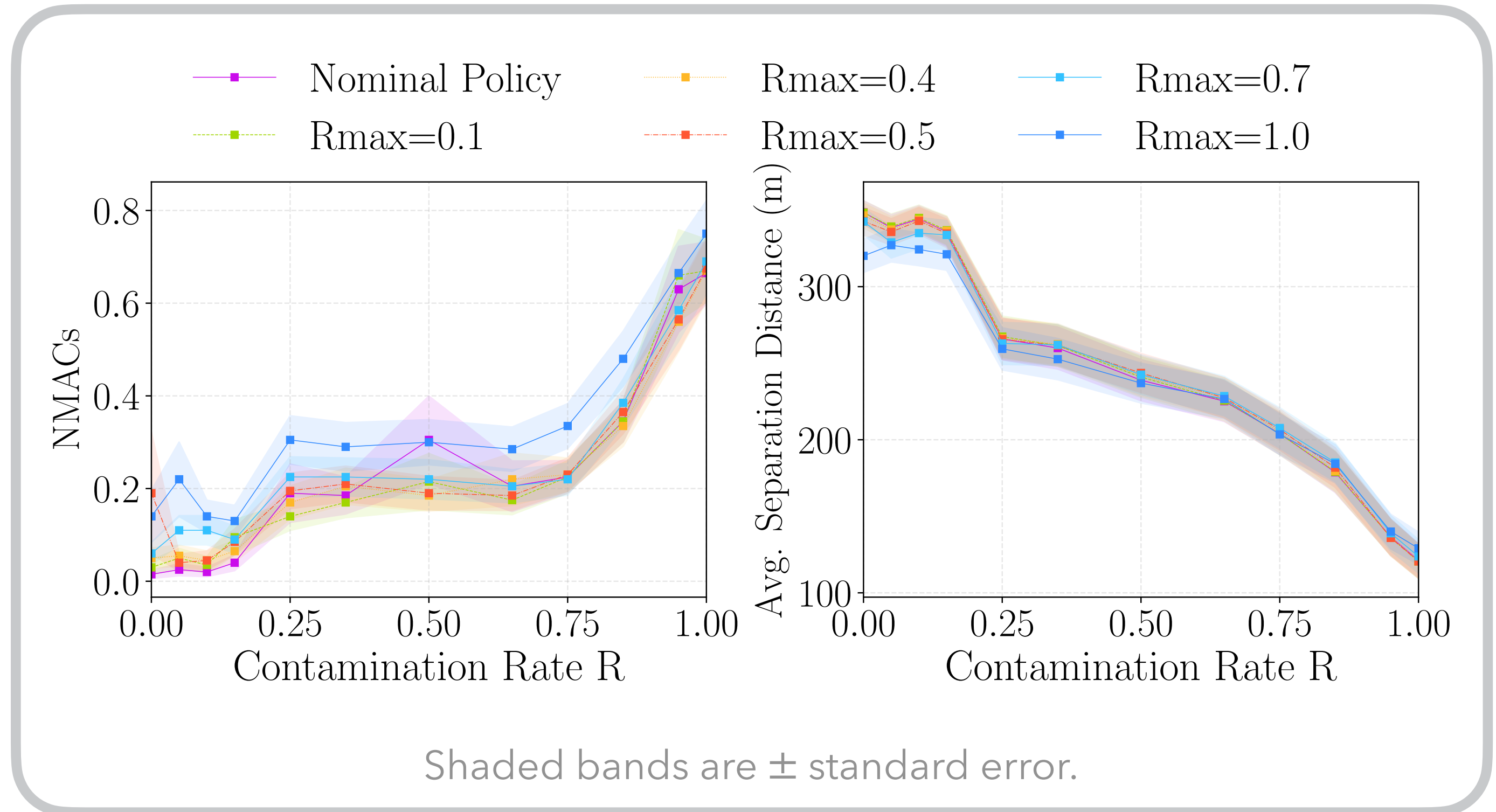
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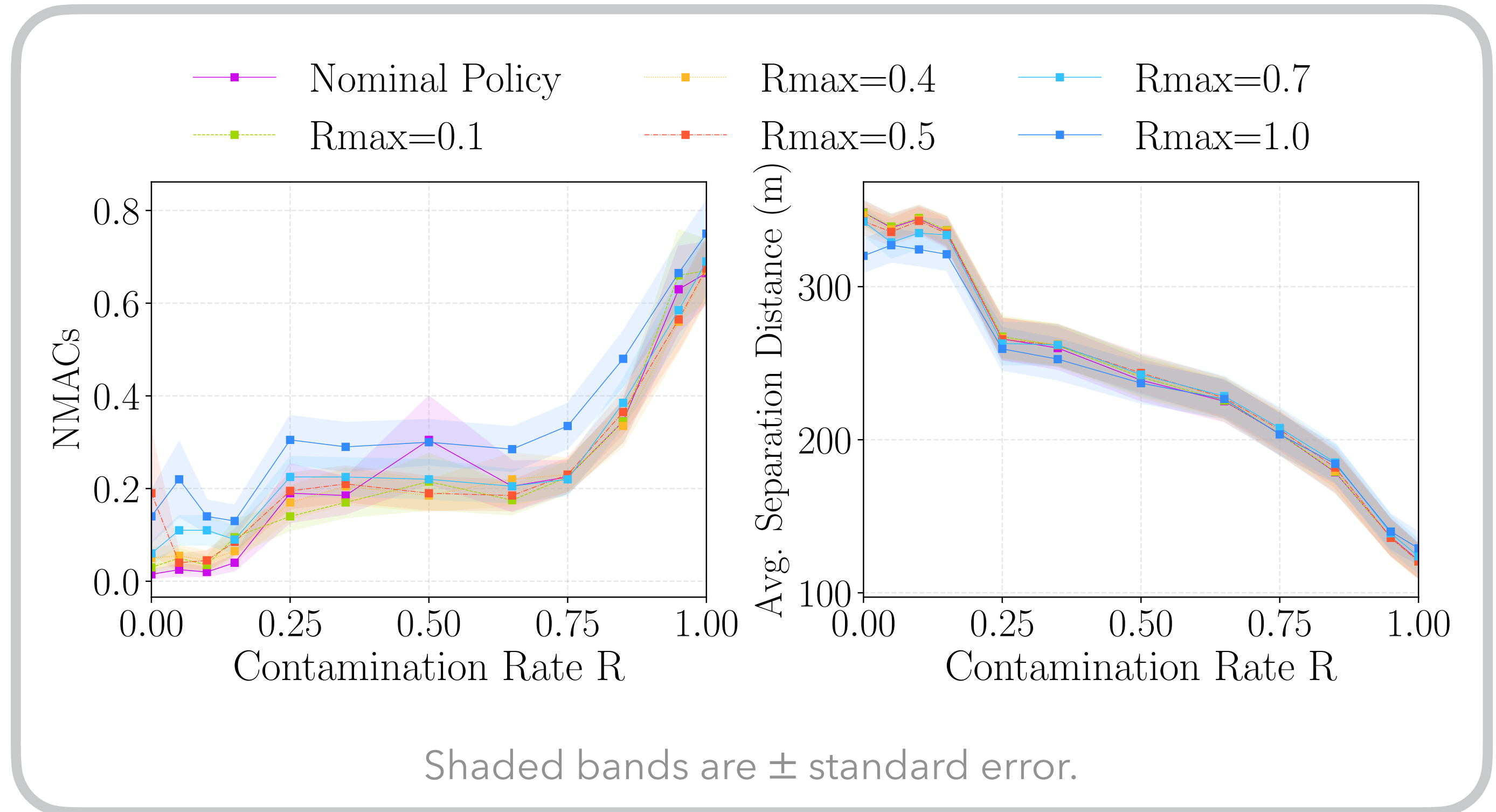
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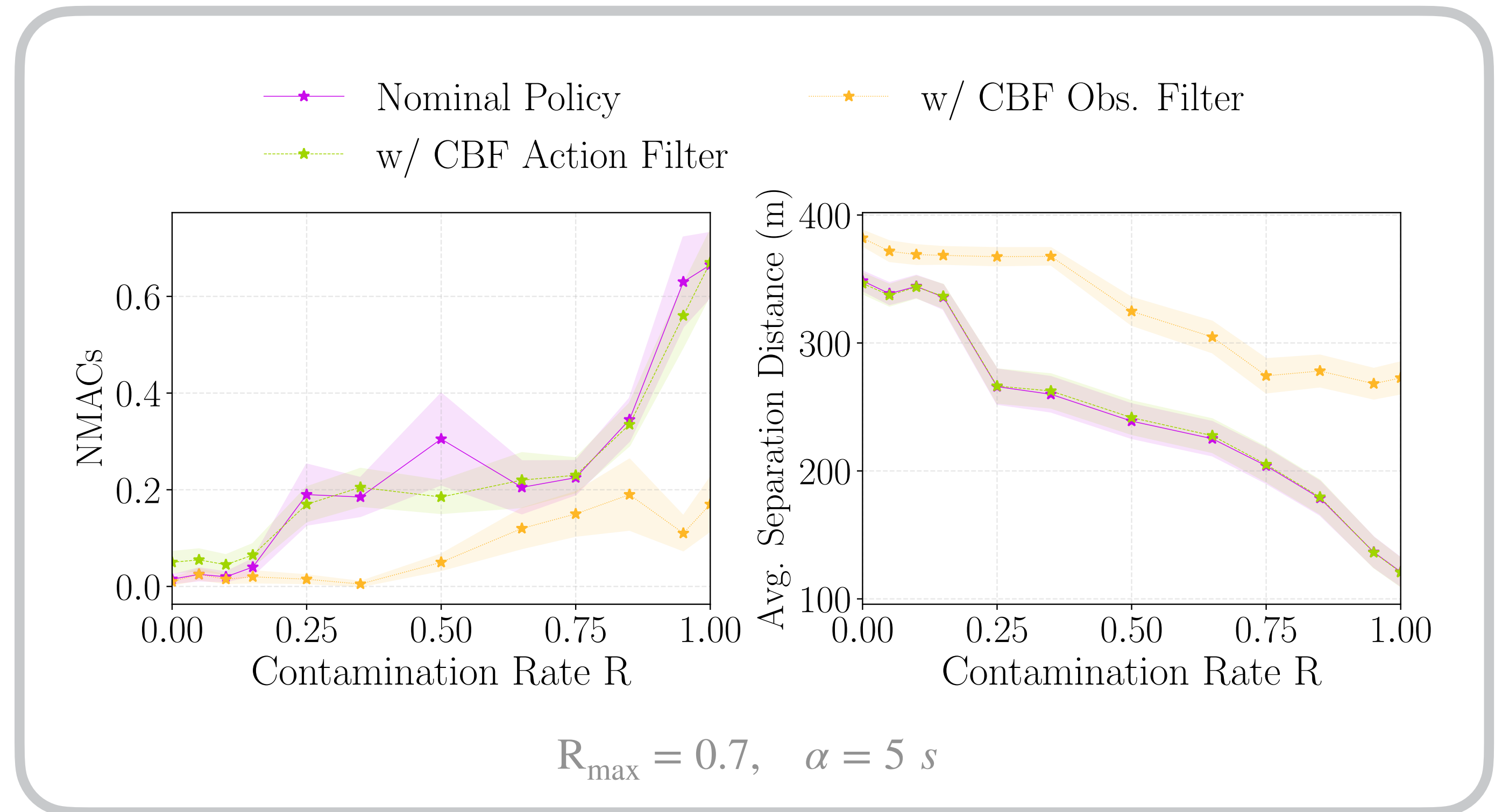
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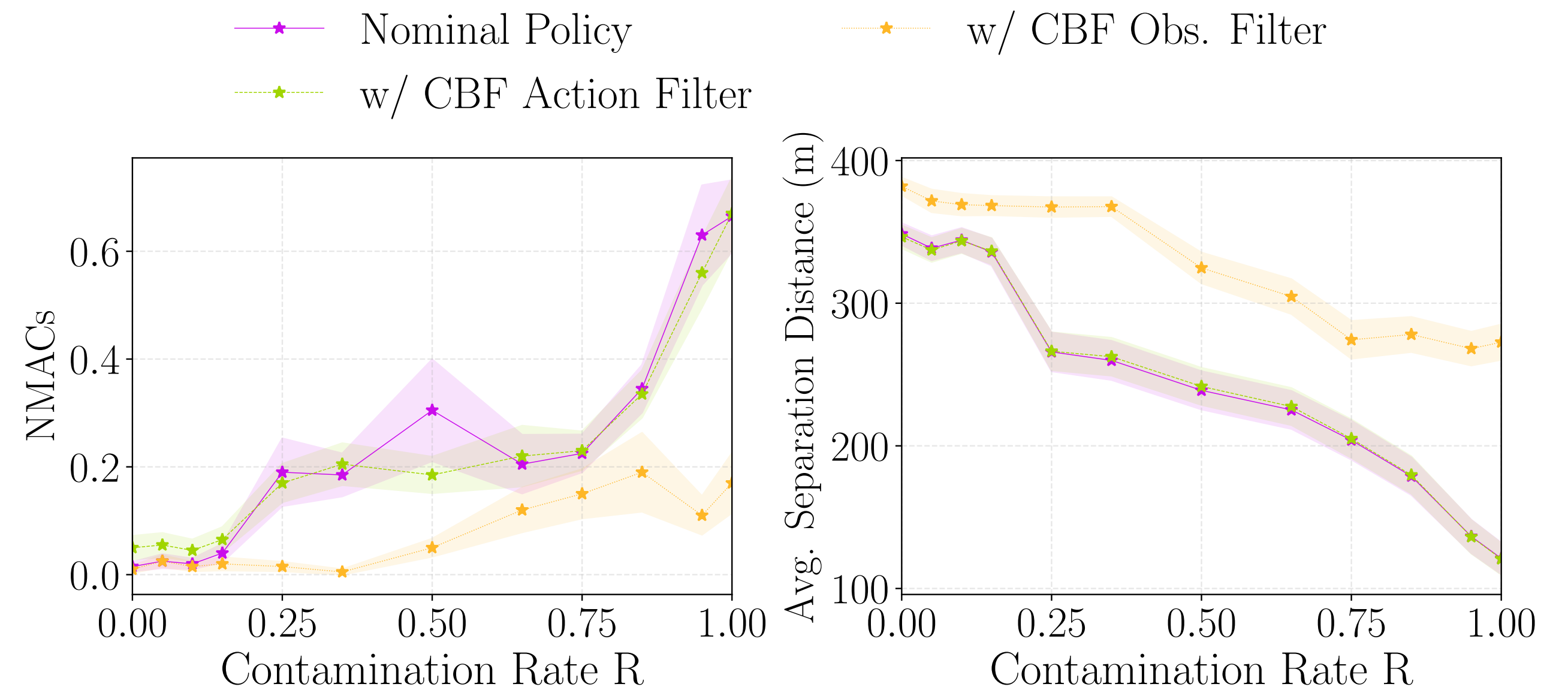
Every setting tracks the nominal policy. Despite changing R_{max} , action filtering does not separate from the unfiltered baseline.

Observation filtering removes nine near collisions in ten

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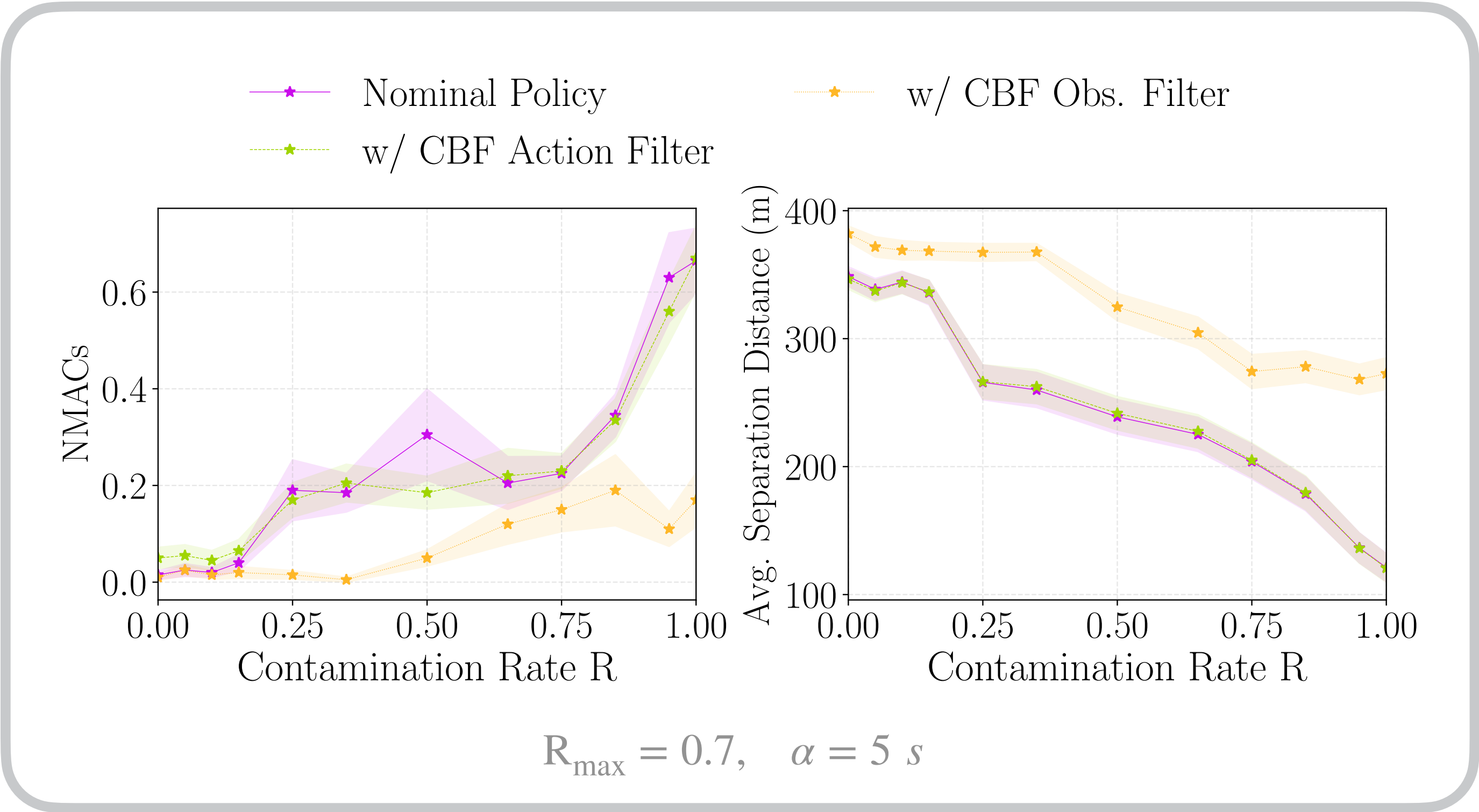


$$R_{\max} = 0.7, \quad \alpha = 5 \text{ s}$$

Observation filtering removes nine near collisions in ten

90%

fewer near mid-air collisions

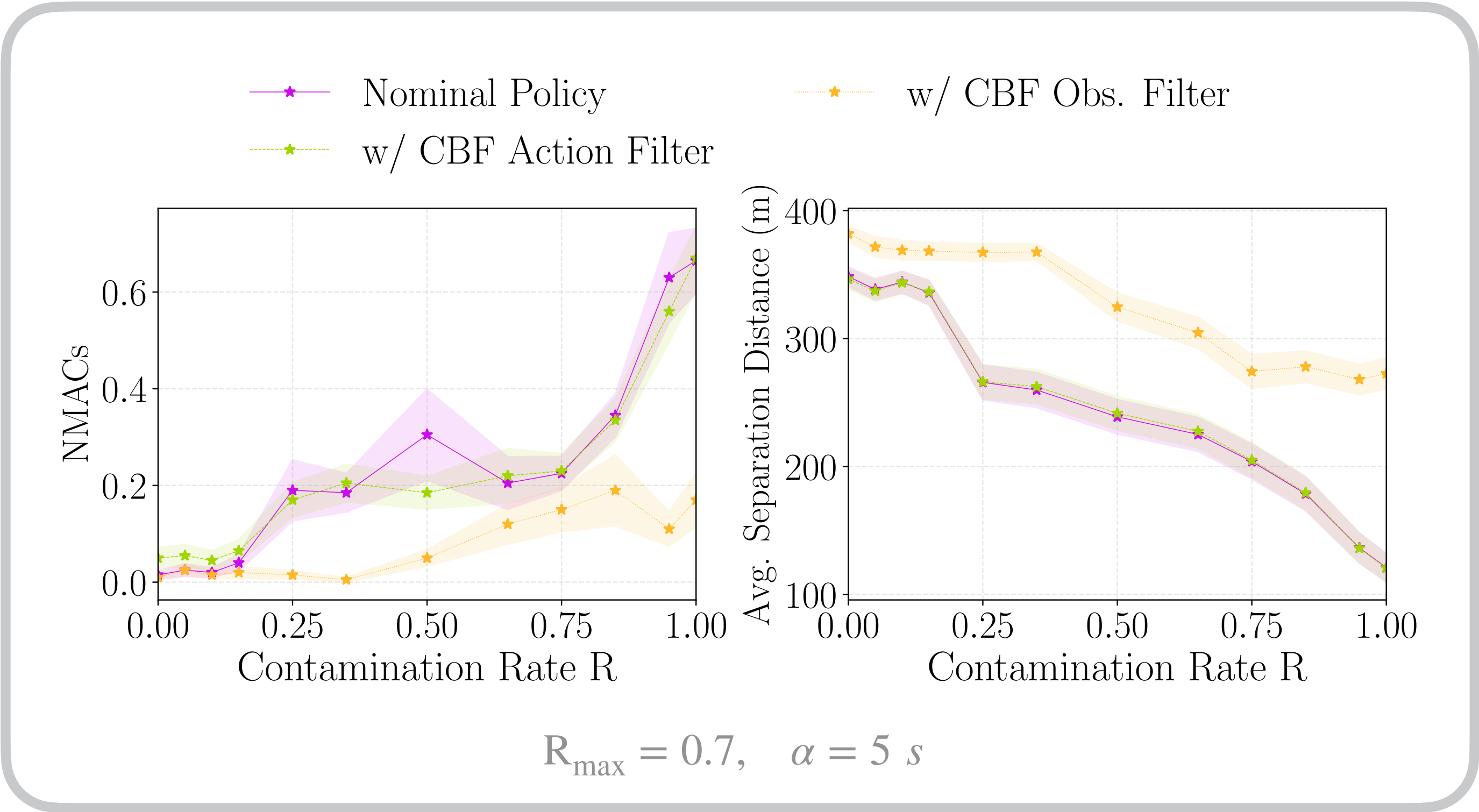


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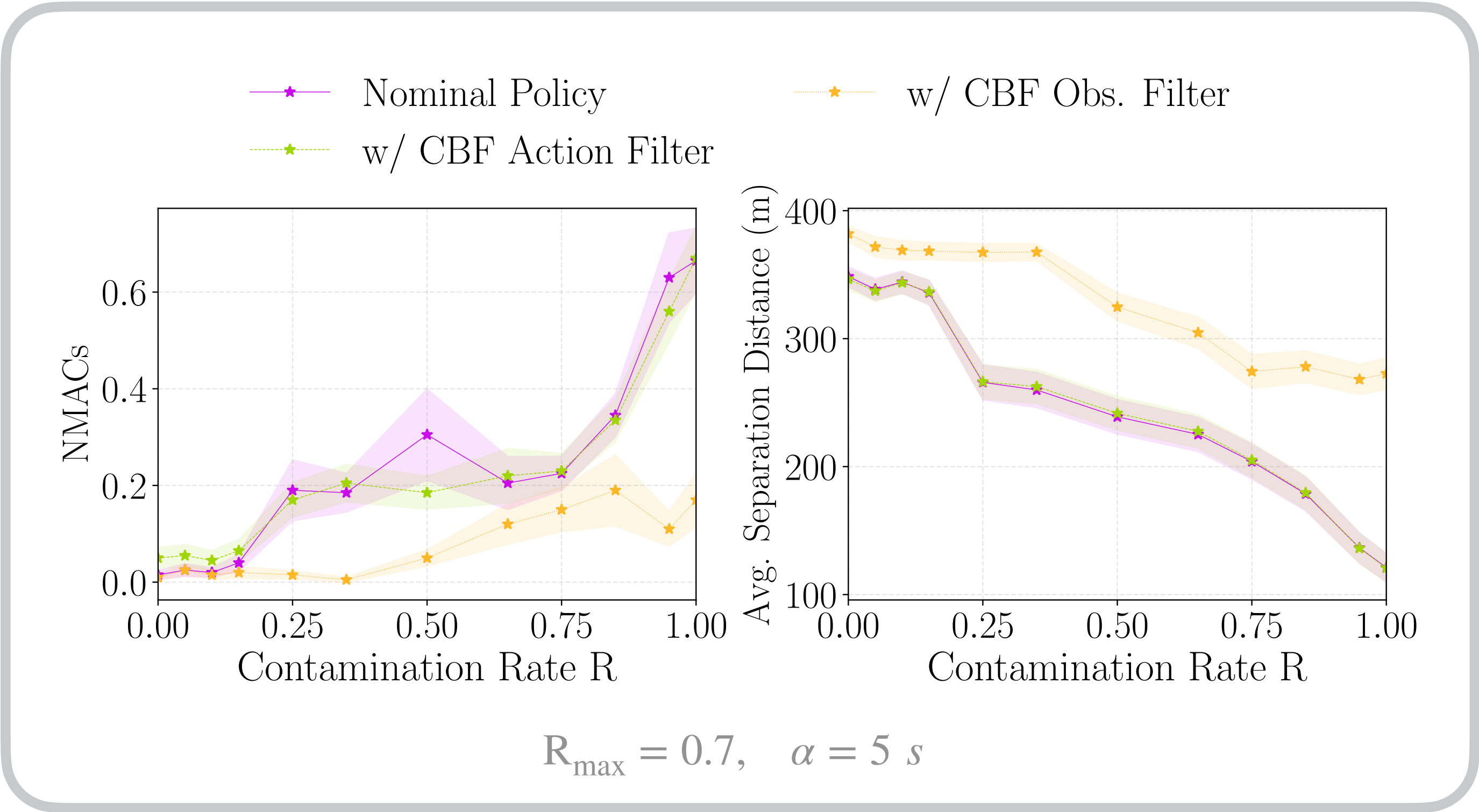
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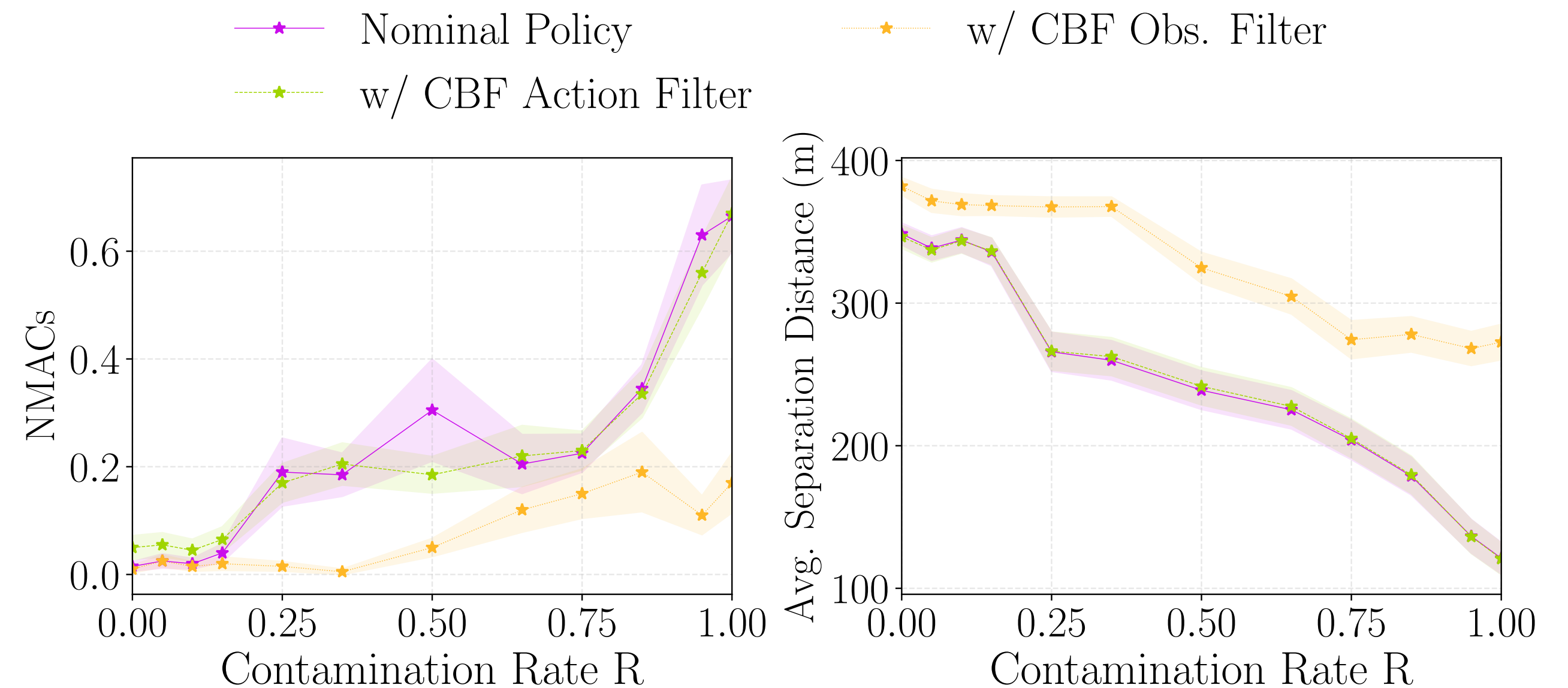
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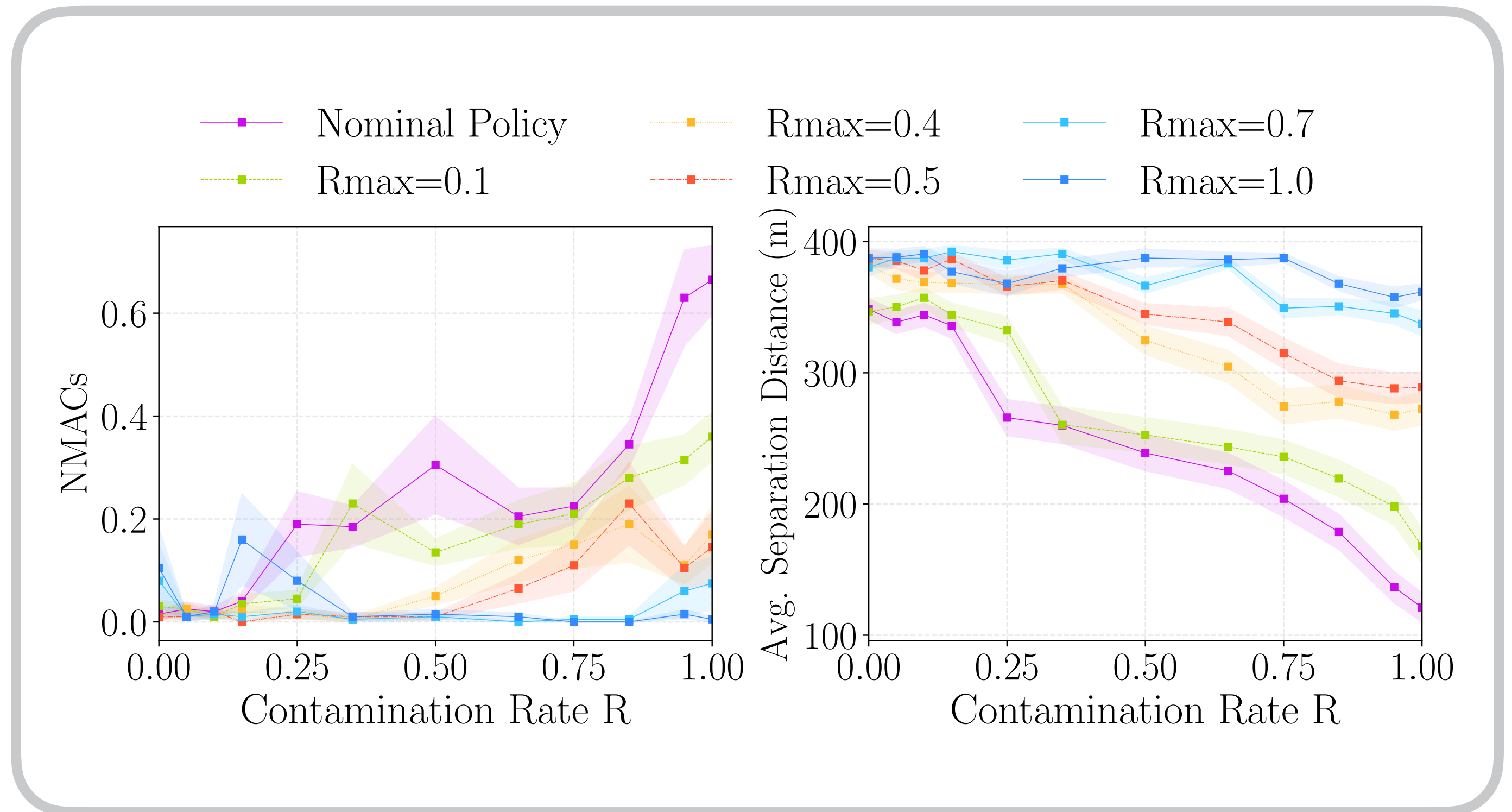
With the same worst-case estimate, the observation filter performs better on its own.

04 RESULTS

The advantage grows with what the filter assumes

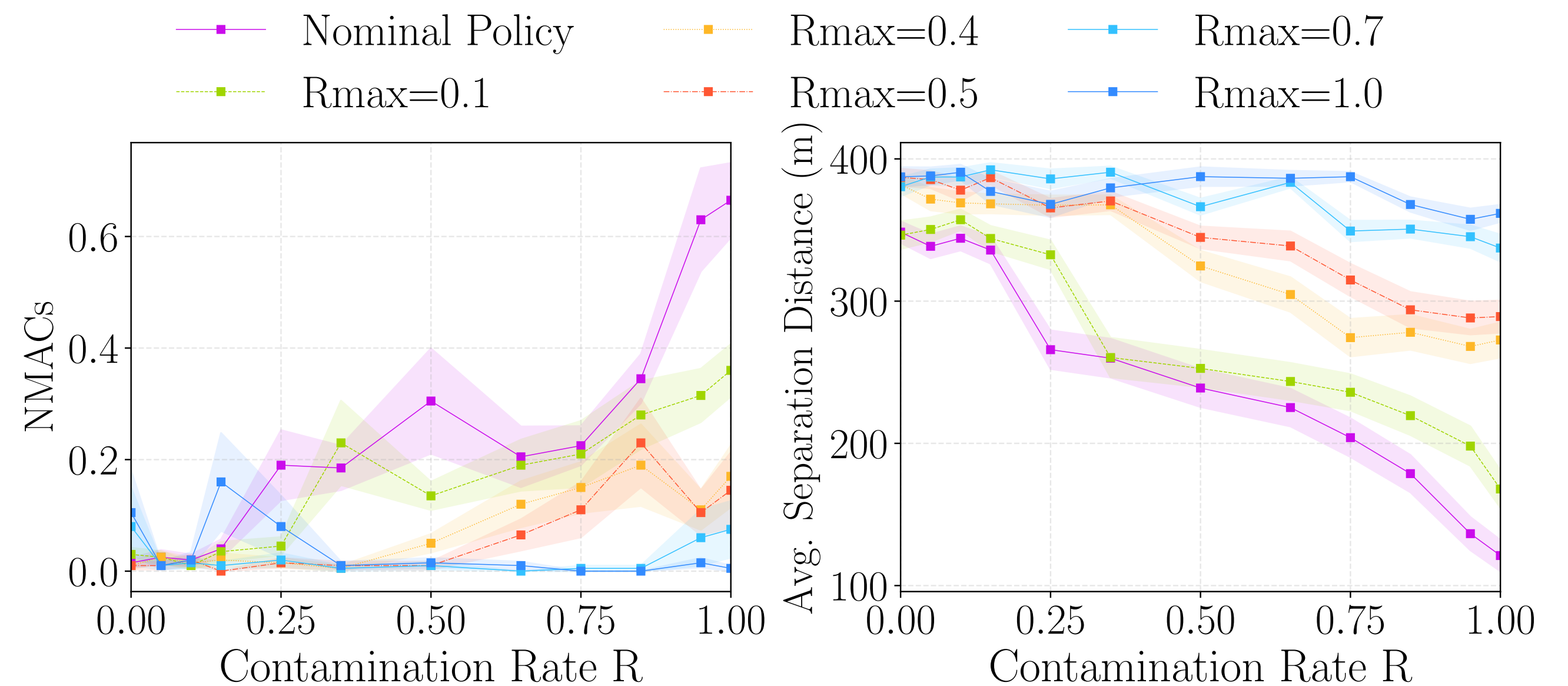
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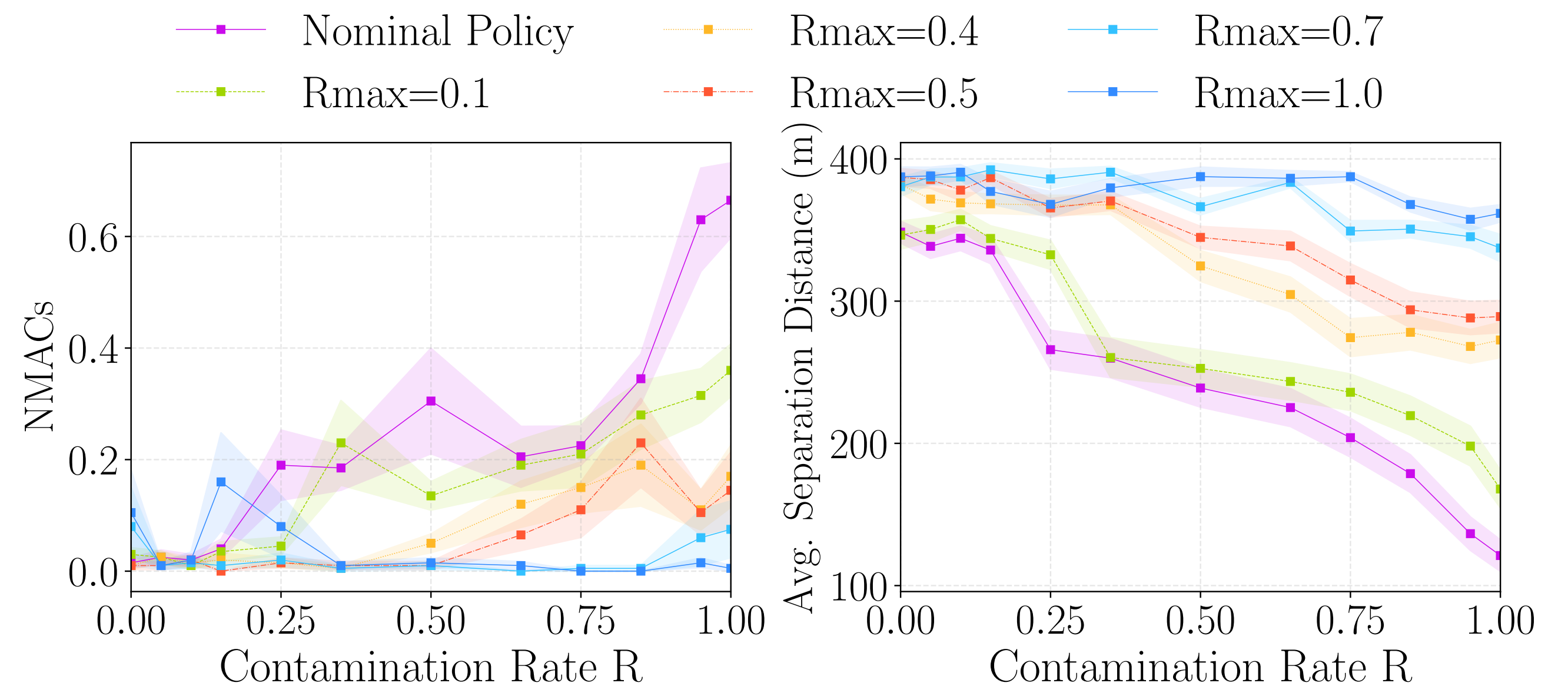


04 RESULTS

The advantage grows with what the filter assumes

$$R_{\max} = 0.1 - 0.5$$

Little benefit. The assumed bound is too small to surface the danger.



04 RESULTS

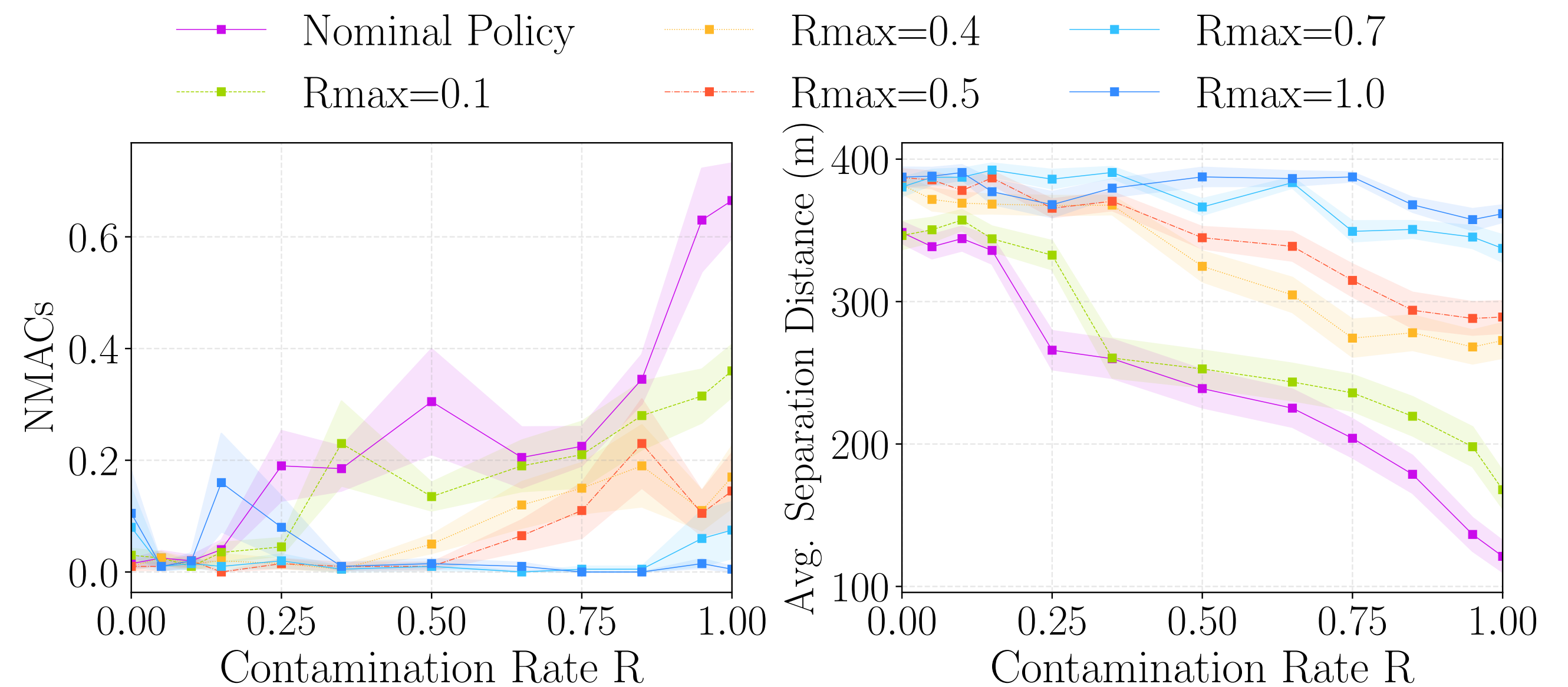
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NMACs are near zero; separation holds around 380 m as nominal policy collapses to 130 m.



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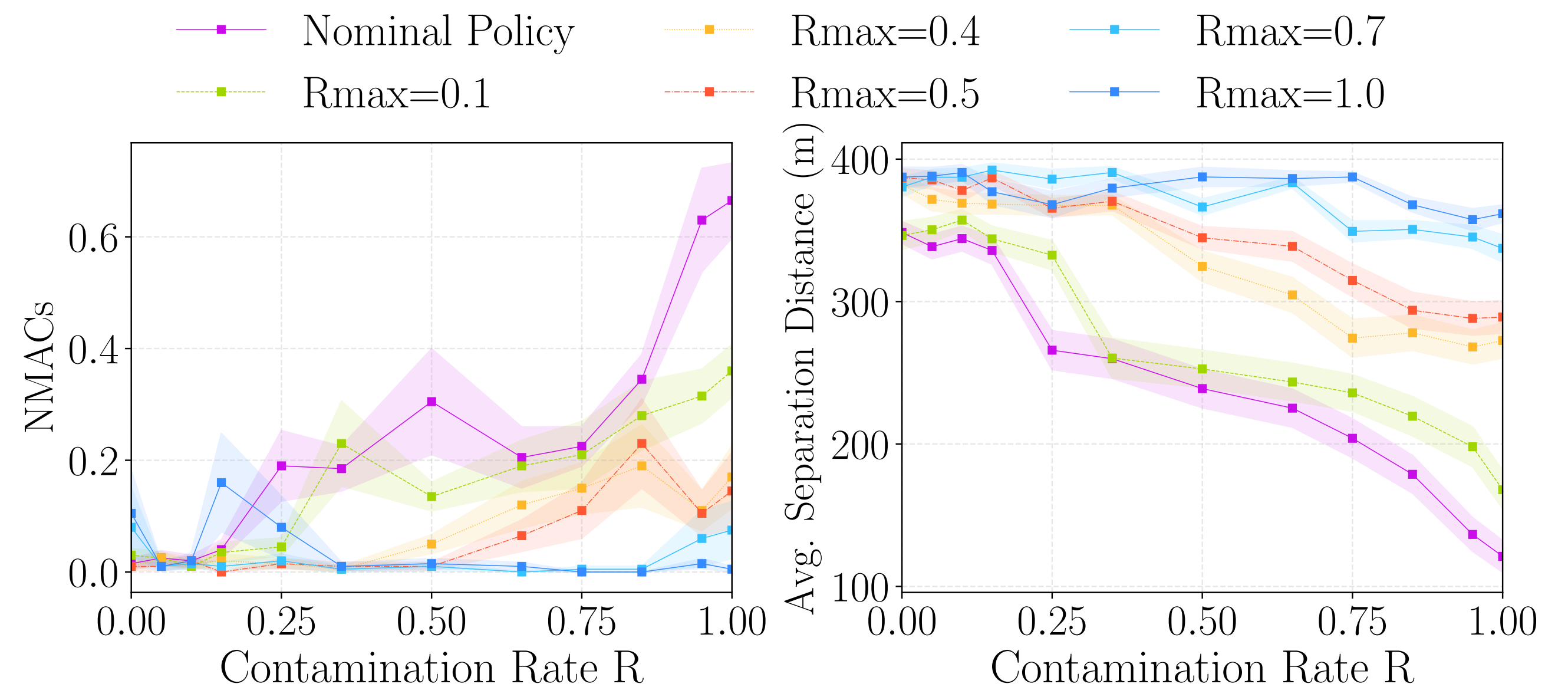
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The filter never observes the true R ; $R_{\max}$ is fixed before deployment.



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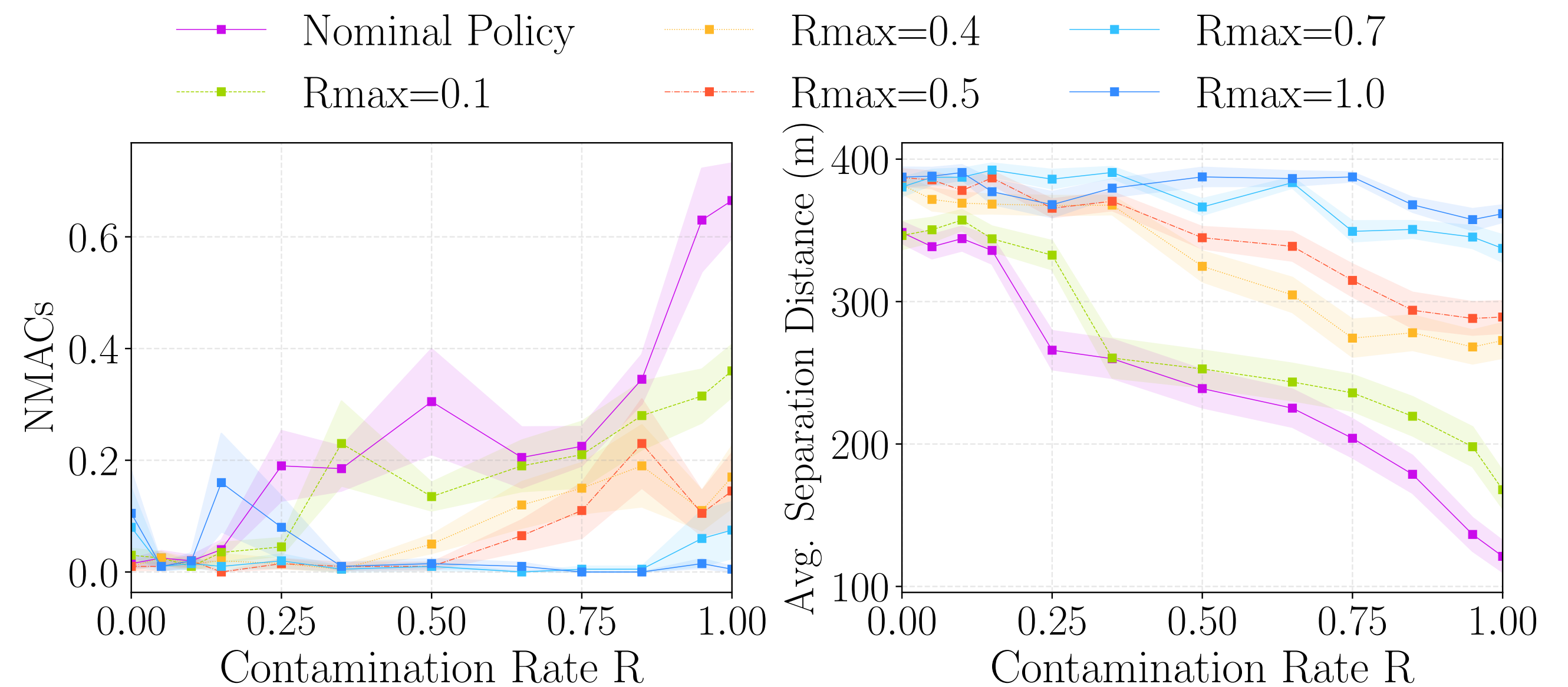
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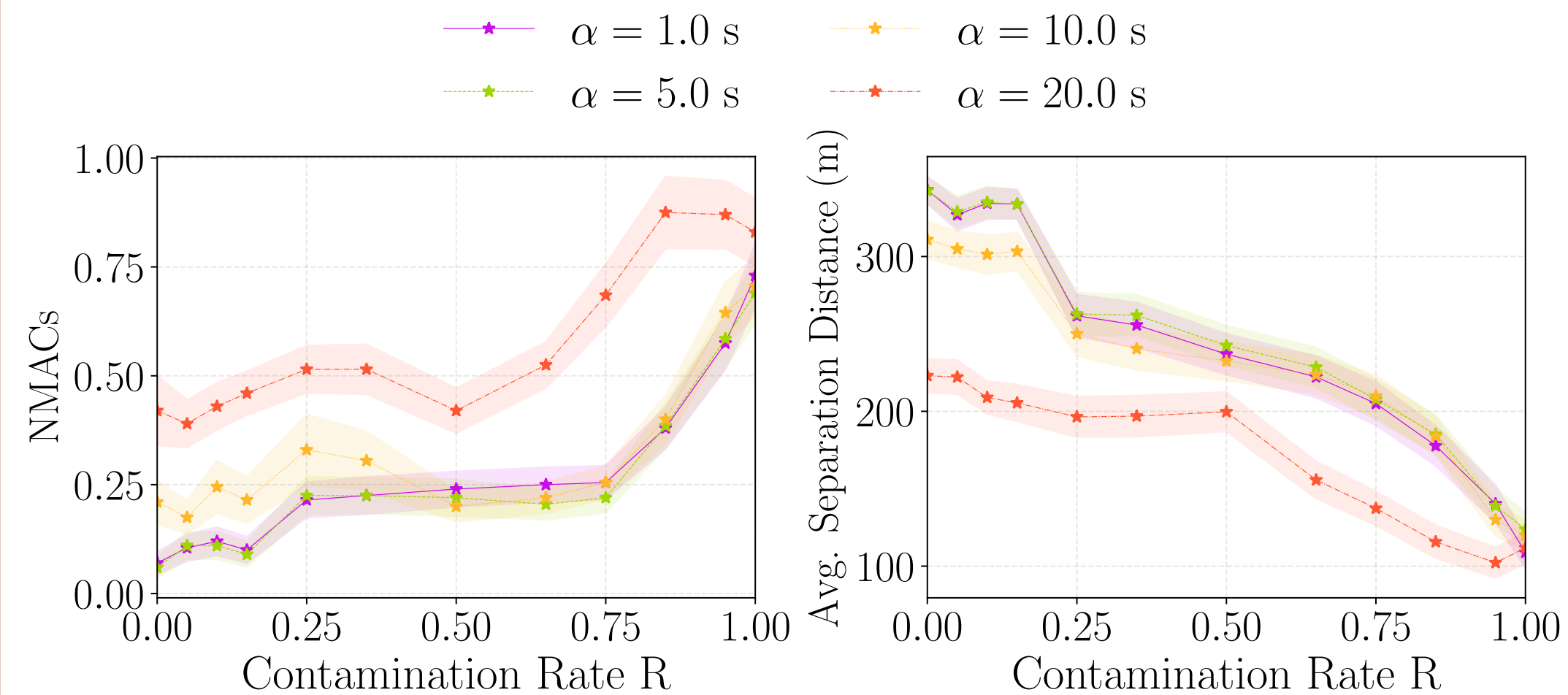
The filter is never told how bad the degradation really is.

Action filtering breaks as α grows; observation filtering does not

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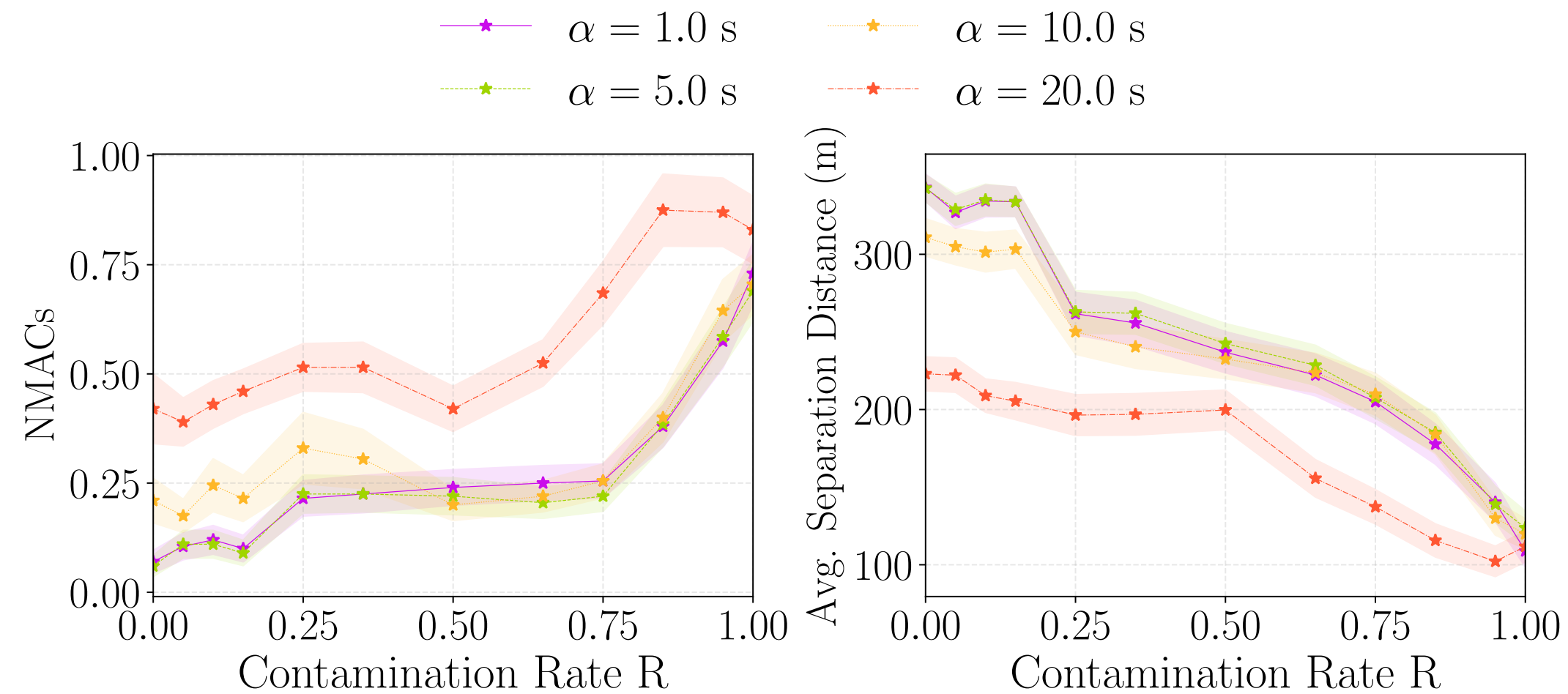


$\alpha = 20$ s more than doubles the NMACs.

04 RESULTS

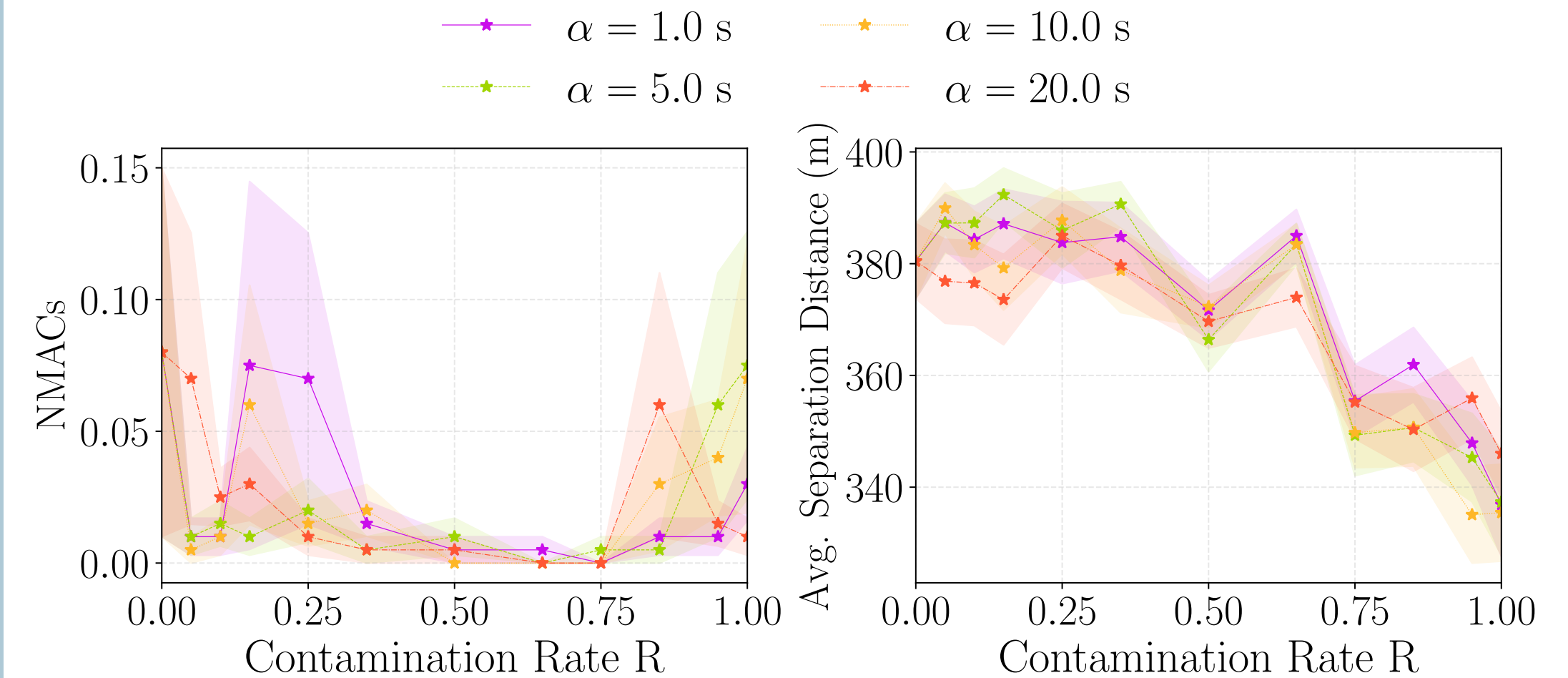
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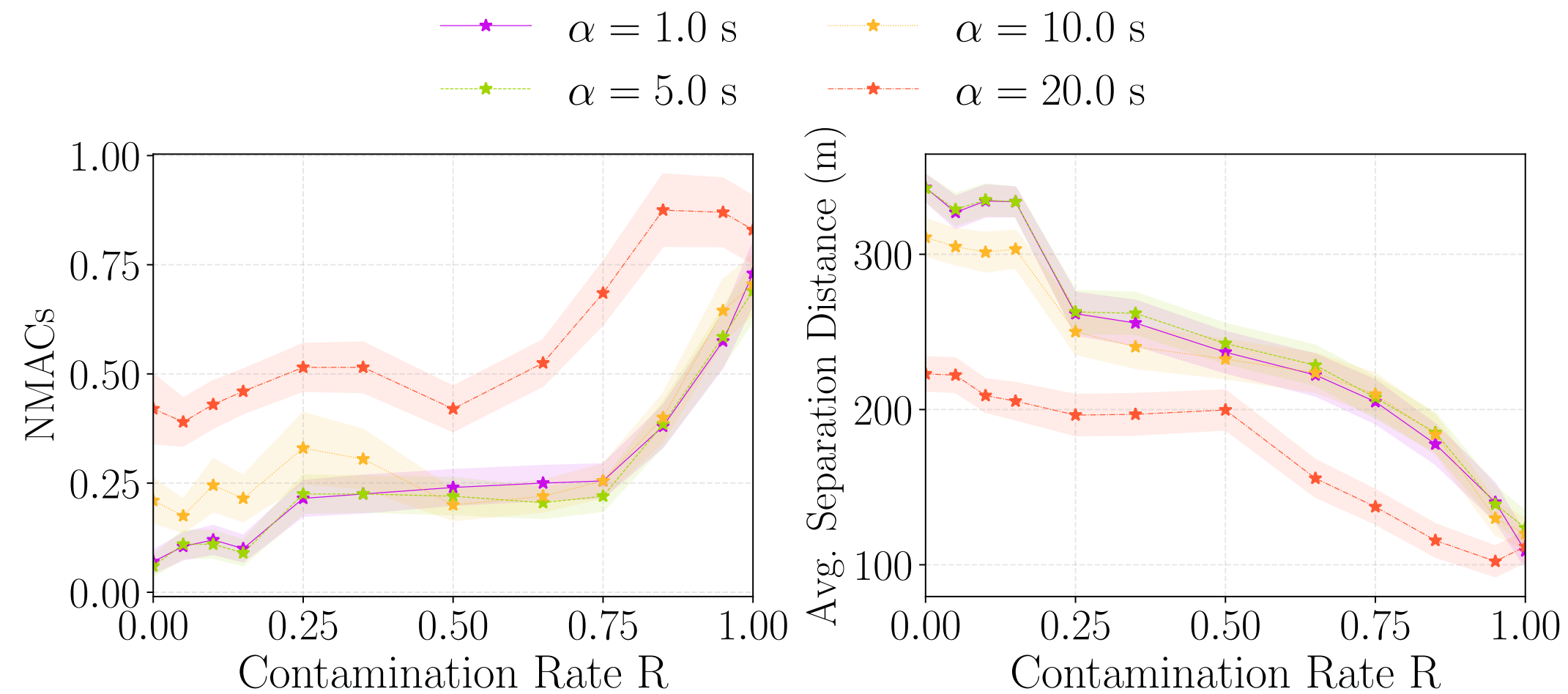


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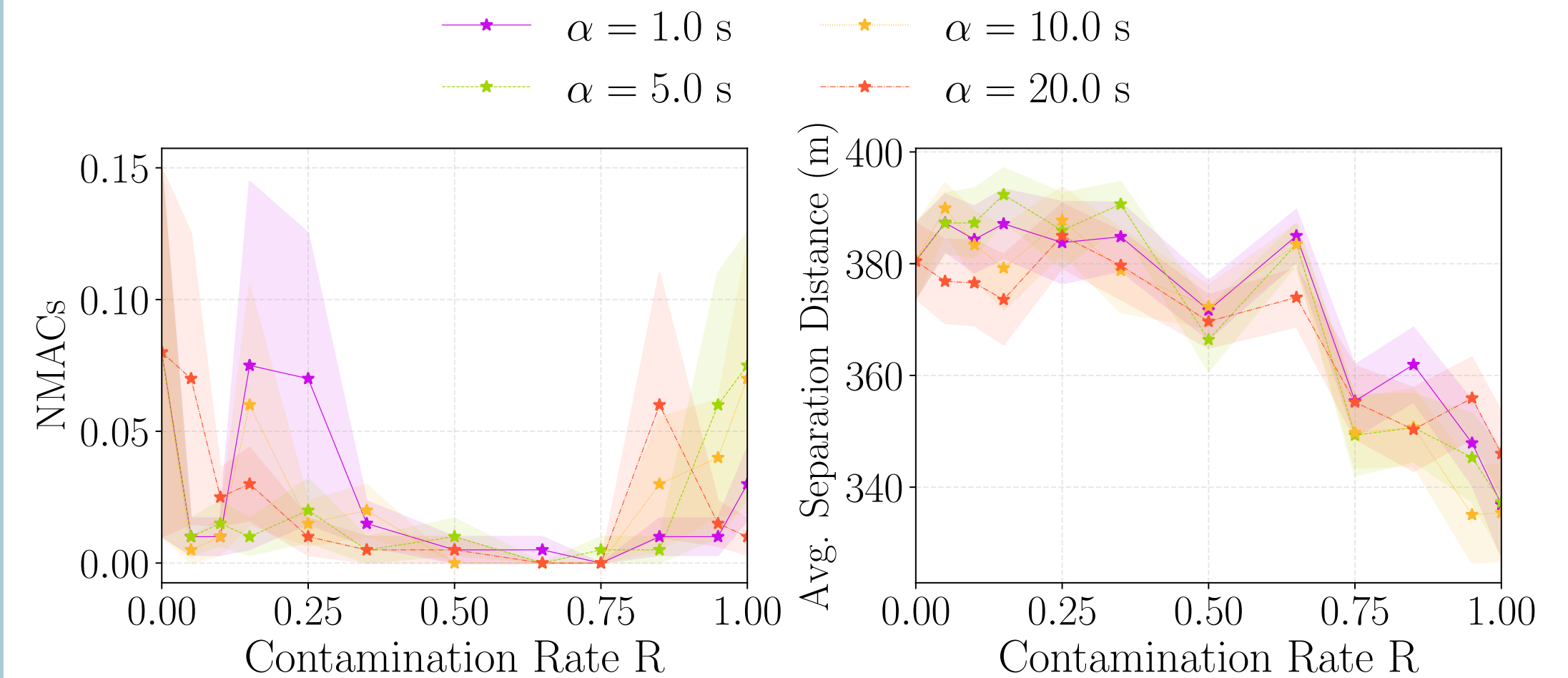
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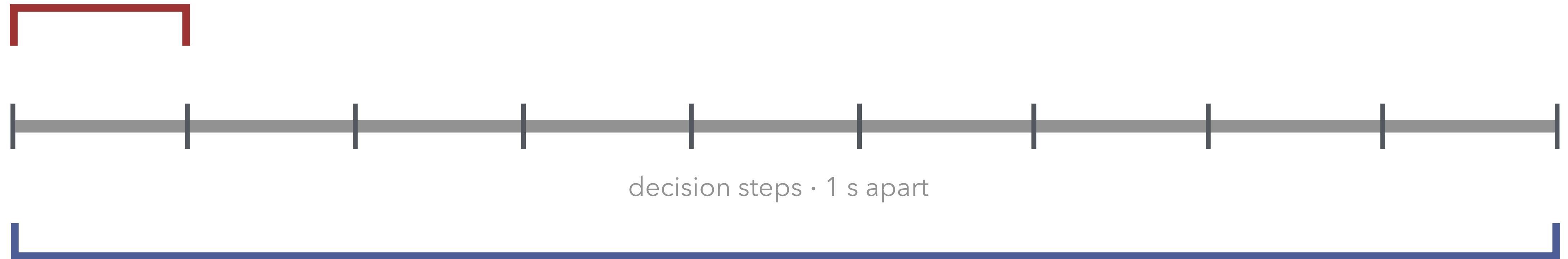


All α values' effects seem to coincide.

α is a barrier-function parameter. It matters only where the barrier can veto the policy's action.

The barrier looks one step ahead; the policy looks further

The CBF condition asks about one step



The trained policy learned to resolve the encounter over many steps

Action filtering replaces multi-step reasoning with a single-step test.

06 TAKEAWAYS

Preserve the trained policy's decision authority

When a learned controller has internalized safety behavior,
informing it outweighs overriding its decision.

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THE COST

Conservatism, e.g., earlier and more frequent slowing down.

Thank you!

Questions?

Runtime Safety Filtering for Learned Small UAS
Separation Policies under GNSS Degradation

Alex Zongo · Peng Wei

Department of Mechanical and Aerospace Engineering
George Washington University, Washington, DC, USA.

Contact: a.zongo@gwu.edu

Preprint: arXiv:2607.10014